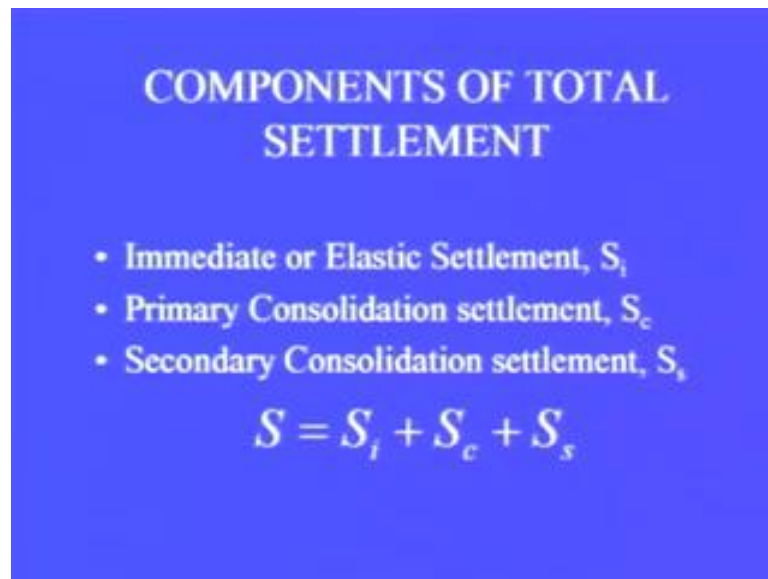


Foundation Engineering
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Module – 01
Lecture - 05
Shallow Foundation

Welcome to the lectures on shallow foundation, in the last lecture we were discussing about the settlement of shallow foundations. We discussed the, a detrimental effects due to the settlements of foundations like, there if there is differential settlement. Then there may be cracking there may be angular distortion, and there may be tilting. And we have seen that leaning tower Pisa is the classical example of tilting. Now, we have also discussed about the type of settlement and in that, we discuss that the total settlement comprises of 3 settlements.

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**COMPONENTS OF TOTAL
SETTLEMENT**

- Immediate or Elastic Settlement, S_i
- Primary Consolidation settlement, S_c
- Secondary Consolidation settlement, S_s

$$S = S_i + S_c + S_s$$

One is known as, immediate or elastic settlement, we designated by S_i . Primary consolidation settlement, that is S_c and secondary consolidation settlement that is S_s . So, this total settlement of the structure can be written as S_i plus S_c plus S_s .

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Computation of Elastic Settlement

- Based on theory of elasticity
- Janbu et al (1956) method of determining settlement under undrained condition

Now, in order to compute elastic settlement, which is of the immediate nature and due to the elastic compression of the soil mass we have methods available based on theory of elasticity and the method that is suggested by Janbu et al.

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The net elastic settlement, S_i for a flexible surface foundation based on theory of elasticity may be obtained as

$$S_i = q_n B \frac{(1 - \mu^2)}{E_s} I_f$$

Now, the net elastic settlement S_i for a flexible surface foundation, based on theory of elasticity can be determined by this equation S_i equal to $q_n B \frac{1 - \mu^2}{E_s}$ upon I_f . Now, here this q_n is the net load intensity at the level of the foundation. B is the width of the foundation, that is flexible foundation then μ is the

Poisson ratio of the soil. And for different type of soils in different conditions, different values have been suggested or otherwise we can determine this value by triaxial test in the undrained condition.

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The net elastic settlement, S_i for a flexible surface foundation based on theory of elasticity may be obtained as

$$S_i = q_n B \frac{(1 - \mu^2)}{E_s} I_f$$

Then we have E_s as the modulus of elasticity of the soil, and again for this we can go for the laboratory method. Or the methods which are based on the field test like Standard penetration test or the plate load test or the pressure meter test or the static cone penetration test. Various researchers have given, values for E_s and those tables can be used which we discussed in the last lecture for estimating the value of E_s . Then the influence factor, we know that due to the pressure distribution in the case of rigid foundation resting on clay. Or the flexible foundation resting on clay or on the sand the pressure distribution varies.

And hence the values of the settlement at the center of the footing, at the corner of the footing are different for the flexible foundation and for the rigid foundation and also for different shapes of the foundations. So, these values have been suggested by various researchers and especially by Vavills and those tables we have discuss in the last class. And we can use those tables for obtaining the value of I_f and when we substitute all these we get settlement known as the immediate or elastic settlement.

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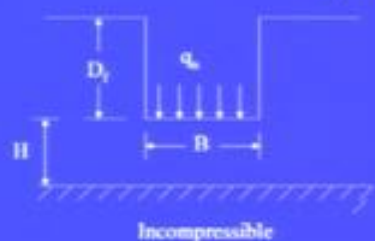
The net elastic settlement, S_i for a flexible surface foundation based on theory of elasticity may be obtained as

$$S_i = q_n B \frac{(1 - \mu^2)}{E_s} I_f$$

As we discussed that the in the case of sands, mostly the settlement is of the immediate nature. Because the permeability of the sand is far far greater than the permeability of clay and hence whatever settlement takes place, that takes place, immediately or during the loading itself. So, in that case this method is very useful and we can determine this immediate elastic settlement.

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Janbu, Bjerrum and Kjaemsli's Method of Determining Elastic Settlement under Undrained Condition

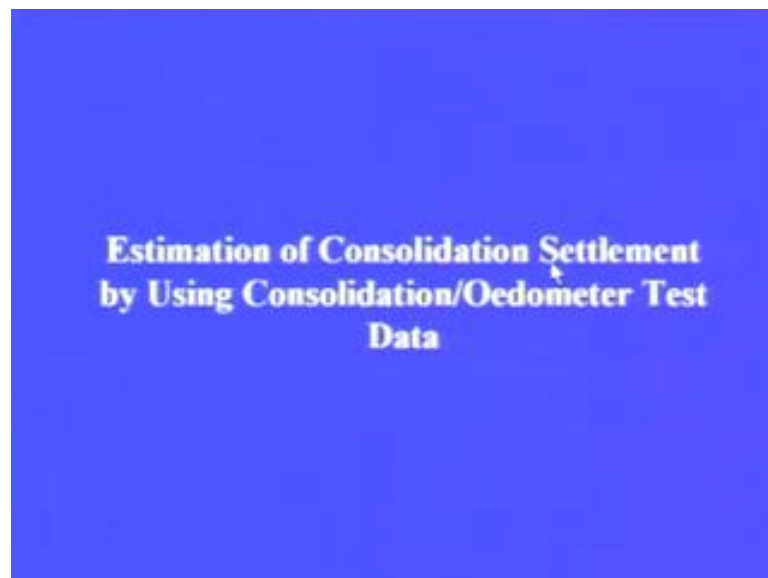
$$S_i = q_n B \frac{\mu_0}{E_s} \mu_1$$


The diagram shows a rectangular foundation of width B and depth D_f embedded in soil. A uniform load q_n is applied to the top surface of the foundation. The soil below the foundation is labeled "Incompressible".

This immediate elastic settlement can also, be determined by method given by Janbu et al. Let us consider a foundation as shown in this figure; it is placed at a depth of D_f

below the ground surface. And the foundation is loading this soil by a load intensity of q_n , on the area are the strip of footing that is of the dimension B . And there is a compressible layer, that is of depth z and below that there is an incompressible layer. Then the elastic settlement can be given as q_n into $B \mu_0 \mu_1$ upon E_s whereas, μ_0 and μ_1 are the parameters, which can be obtained by the charts provided by Janbu et al. Now, this μ_0 is a function of D_f by B whereas, μ_1 is the function of H upon B for different shapes of footing like square footing, strip footing, circular footing and rectangular footing. So, using that chart, we can obtain value μ_1 and then when we substitute in this equation we get elastic settlement.

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Now, in order to determine consolidation settlement, we use the data obtained by the consolidation test or Oedometer test.

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The consolidation settlement of saturated compressible stratum occurs due to expulsion of pore water on account of gradual dissipation of excess pore water pressure induced by an imposed total stress.

In one dimensional compression, change in thickness, ΔH per unit of original thickness, H of the stratum is equal to change in volume, ΔV per unit of original volume, V .

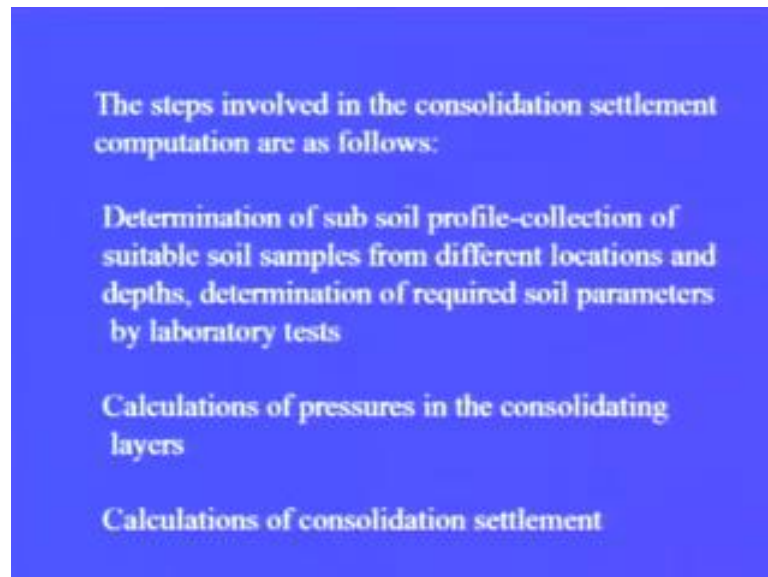
Now, as you must have learn in the soil mechanics course, that the consolidation settlement of saturated compressible stratum, occurs due to expulsion of pore water on account of, gradual dissipation of excess pore water pressure, induced by an imposed total stress. In one dimensional compression change in thickness ΔH per unit of original volume H of the stratum is equal to the change in volume, ΔV per unit of original volume. So, using this data what we can do? We can obtain the parameters and then we can calculate consolidation settlement.

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The change in volume is a consequence of a decrease in in the void ratio, Δe as volume of soil solids remains unchanged and change in volume takes place due to readjustment of soil particles.

The change in volume is a consequence of, decrease in the volume of voids that is void ratio Δe . As volume of soil solids remain unchanged and the change in volume takes place due to readjustment of the particles. As water escapes out from the voids, these soil solids are readjusted and we get a compression.

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Now, in order to determine the consolidation settlement the steps, involved in the consolidation settlement are as follows. Determination of sub soil profile collection of suitable soil samples from different locations and depths, and determination of required soil parameters by laboratory tests. So, what we do? If we want to determine consolidation settlement of a compressible layer we will have to first get the profile sub soil profile of the area.

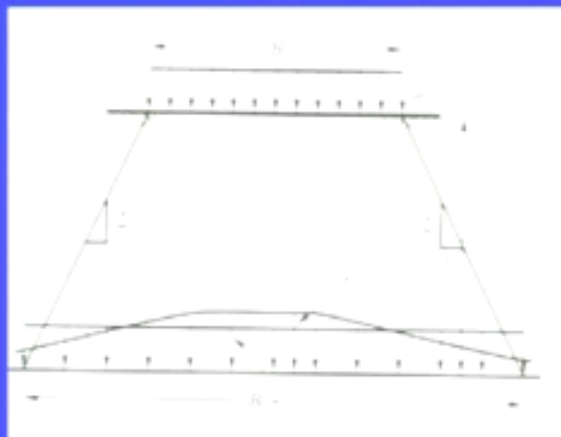
Now, what for that what we do? We go for boreholes we advance boreholes up to the required depth, and then we collect undistorted and distorted samples. And on undistorted samples, we conduct consolidation test and obtained the consolidation parameters, which are for the calculation of settlement. Then one once that strata is known and if we know the load which is applied by the footing, on to the sub soil we can also determine the pressures in the consolidating layers. And then finally, we calculate the consolidation settlement.

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Once we have the knowledge of the soil profile, location of water table and index properties of different strata, the initial effective stresses due to overburden at the mid depth of individual layers can be very easily calculated for the simple static case of hydrostatic pressure.

Once we have the knowledge of soil profile, location of water table and index properties of different strata. The initial effective stresses due to overburden at the mid depth of individual layers, can be very easily calculated for the simple static case of hydrostatic pressure.

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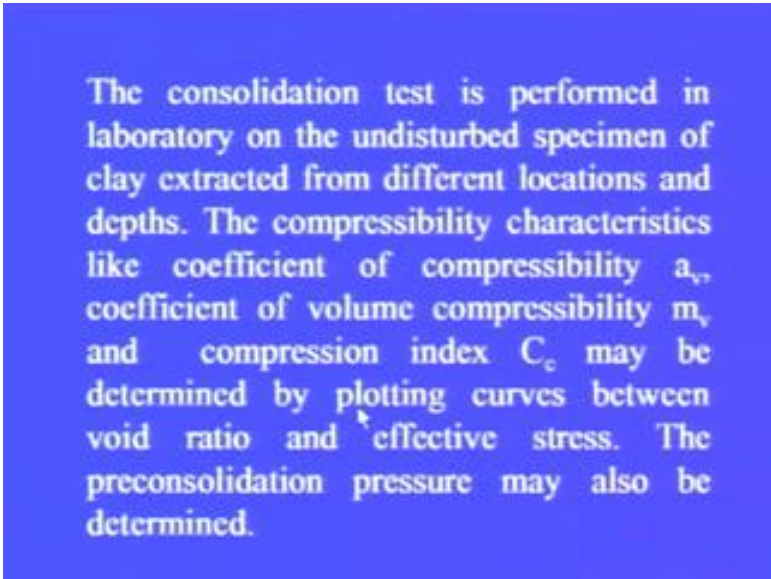


In the last class, we also discuss the methods to determine the stresses, at different levels, due to the foundation loading. Now, we have methods given by Bussyneck, we have methods given by a Westergaard. So, by using Bussyneck method or by using

Westergaard, which is normally preferred in the sedimentary soil deposits. We can determine, what is the increase in stress at the particular level? Now, this particular normally, we consider at the mid depth of the consolidating layer. Now, there is an method approximate method, given that is known as 2 vertical is to 1 horizontal distribution of pressure, the which we discussed in the last lecture. Now, here there is a loaded area of width B , and load intensity Q is applied to the soil, then if you want to determine the stress increase. Due to this stress at a level z depth below the ground surface, then what we will have, to we will have to consider this to vertical is to 1 horizontal load distribution. And then the loaded area at that particular depth will, become equal to the width of B plus Z and hence what we can do?

We can determine this in is increase in stress, as B into Q into the dimension in the other direction. In the case of strip footing, it is 1 in the case of rectangular footing it is length L and in the case of square footing this is width B . So, from that, we can distribute this load total load B into Q into whatever is the dimension in this direction, divided by B plus z into 1 or the dimension in the other direction depending upon the shape of footing. And hence, we calculate this value of the mean stress, increase in stress, due to the foundation loading. Now, this is the graph or the curve, which we obtain either by the Bussyneck method or by the Westergaard method whereas, this uniform stress intensity we get by 2 is to 1 method.

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The consolidation test is performed in laboratory on the undisturbed specimen of clay extracted from different locations and depths. The compressibility characteristics like coefficient of compressibility a_v , coefficient of volume compressibility m_v and compression index C_c may be determined by plotting curves between void ratio and effective stress. The preconsolidation pressure may also be determined.

The consolidation test is performed, in laboratory on the undisturbed specimen of clay from different locations and depths. The compressibility characteristics like coefficient of compressibility a_v coefficient of volume compressibility m_v and compression index C_c may be obtained by plotting curves, between void ratio and effective stress. The preconsolidation pressure may also be determined from this data.

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Settlement calculation from e-log σ' curve

The volume of solids V_s is assumed unity and void volume equal to e_0 -the void ratio of soil before compression. If e_f is the void ratio after the primary compression is complete, the decrease in volume is $\Delta e = (e_0 - e_f)$. Then ΔH , the change in thickness in height of consolidating layer or its settlement is given by the equation

$$\frac{\Delta H}{H} = \frac{\Delta e}{1 + e_0} H_0$$

Now, as far as the consolidation, has it concern you must have been studied it in the soil mechanics course, but for the benefit, we I simply give you salient features of the consolidation test. What we actually do? We take out an undistorted sample from the field, and then that undistorted sample from the field is transferred to the consolidating ring consolidation test in the consolidation test operators. We have a consolidation ring of the standard size normally it is of the diameter 75 millimeter and thickness 20 millimeter. After transferring that, in the consolidation ring we keep this consolidation ring in the consolidation setup and then we saturate the soil sample. We know that the consolidation theory given by Terzaghi is valid only for the saturated clays.

So, we saturate the soil sample and then after saturation is achieved, we apply a load increment and in that load increment, we get the compression of that consolidating layer at different time intervals. Like starting from time t equal to 0, to time t equal to 0.25 minutes, then time t equal to 0 point 36 minutes. And likewise up to 24 hours we keep on measuring the compression. And after that, we after that compression is achieved we

increase the load intensity to another loading increment, like. We go as 50 kilo Newton per square, then 100 kilo Newton per meter square 200 kilo Newton per meter square 400 kilo Newton per meter square 800 kilo Newton per square.

And if required 1600 kilo Newton per meter square, it has been observed from the test that this consolidation test is valid only for the large increment ratio and that increment ratio should be at least 1. That is why we preferred 0 25 50 100 200, so, that the load increment ratio is at least 1. Now, at all stress increment we find out the compression of the soil, of that 20 millimeter thick soil layer which is which we have already placed in the consolidation ring. And from this data, we can obtain coefficient of consolidation or coefficient of compressibility compression index or we develop our relationship, between e versus effective stress.

Now, in order to determine, value of e there are 2 methods available. 1 is known as height of solids method, another is known as a change in voids ratio method. So, from that we develop our relationship between e versus σ_{bar} , similarly, in order to get coefficient of consolidation. We have either Taylors method square root of a time fitting or a secondary method by which square root of log of the then using those methods we can determine coefficient of consolidation. But here in the calculation of ultimate settlement or total settlement we are interested in a_v , that is coefficient of compressibility. My; that is coefficient of volume change, and the compression index and using that, we can determine the settlement. So, we develop our relationship between, wide ratio and effective stress. Once that relationship is known using that relationship we can find out the consolidation settlement, of the actual soil layer using those parameters.

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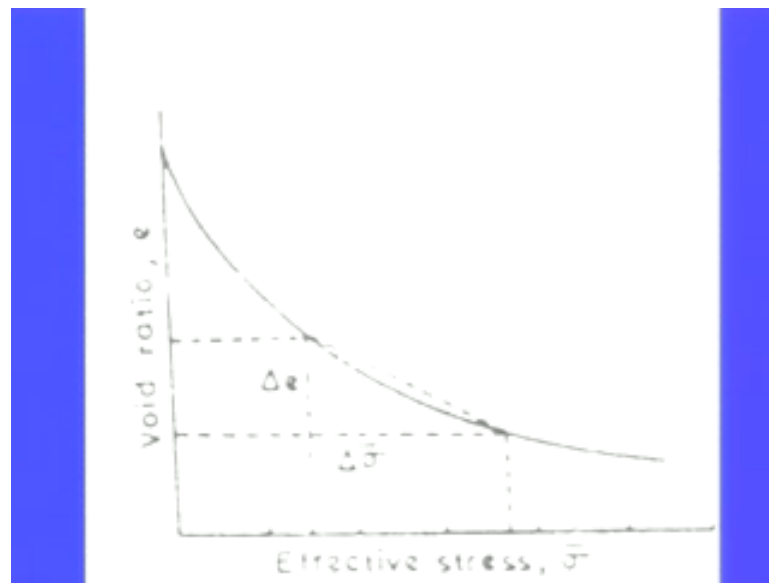
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$$\frac{\Delta H}{H} = \frac{\Delta e}{1 + e_0} H_0$$

So, the volume of solids V_s is assumed unity and void volume, equal to e_0 the void ratio of soil before compression. If e_f is the void ratio after the primary compression is complete the decrease in volume is Δe that is e_0 upon e_f e_0 minus e_f . Then ΔH the thickness change in thickness in the height of consolidating layer or its settlement is given by ΔH upon H equal to Δe upon $1 + e_0$ into H_0 . Now, here this e_0 is corresponding to the stress σ_0 a dash that is the effective overburden pressure at the middle of the consolidating layer. And e_f is the void ratio, after the application of the load or when we include $\sigma_0 + \Delta \sigma$ and that $\Delta \sigma$ is determined by the 2 is to 1 method

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This is that void ratio versus effective stress relationship, which we get from the consolidation test. So, from this at different stresses we find out what is the void ratio? Either using height of solids method or change in void ratio method, and then we plot our relationship. Now, as can be seen from here that this is the void ratio corresponding to the initial condition and this is the void ratio corresponding to the final condition. So, and this $\Delta \sigma \bar{}$ is the increase in stress from $\sigma_0 \bar{}$ to this $\sigma_f \bar{}$ that is the effective stress after the load has applied. Now, this slope of this curve is nothing, but the coefficient of compressibility a_v . Now, for the stress range, which we which are encountered in field, what we can do? We can consider this segment. The change in void from this to this that is equal to Δe divided by $\Delta \sigma \bar{}$ or the $\Delta \sigma \bar{}$ effective stress, we call it as the coefficient of compressibility.

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$$\Delta H = S_c = \frac{\Delta e}{1 + e_0} H_0$$

From $e-\sigma'$ curve arithmetically, the slope of the curve for the pertinent stress range, that is, the coefficient of compressibility a_v , can be used in settlement computation,

$$a_v = \frac{\Delta e}{\Delta \sigma'} \text{ and } S_c = \frac{a_v}{1 + e_0} H_0 \Delta \sigma'$$

And from that coefficient of compressibility, we can determine the settlement. So, this ΔH equal to nothing, but the consolidation settlement of the layer, that will be given by Δe upon $1 + e_0$ into H_0 . Where H_0 is the thickness of the compressible layer e_0 is the initial void ratio. And this Δe can be determined if we read values of a void ratio at σ_0' effective stress and $\sigma_0' + \Delta \sigma'$. And whatever is the difference we substituted here, and then we calculate consolidation settlement. Now, from this $e-\sigma'$ curve arithmetically the slope of the curve for the pertinent stress range, that is the coefficient of compressibility a_v can be used in the settlement computation. So, this a_v is Δe divided by $\Delta \sigma'$. So, this Δe can be written as $a_v \Delta \sigma'$. Now, when we substitute in this equation, we will get S_c equal to a_v upon $1 + e_0$ into $H_0 \Delta \sigma'$.

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The term given below is known as coefficient of volume change or volume compressibility

$$\frac{a_v}{1+e_0} = m_v = \frac{\Delta e}{\Delta \sigma'} \frac{1}{1+e_0}$$

Therefore,


$$S_c = m_v H_0 \Delta \sigma'$$

The term given below is known, as coefficient of volume change or volume compressibility that is coefficient of compressibility divided by the initial volume, 1 plus e 0. So, this a_v upon 1 plus e 0 is m_v and that is equal to Δe upon $\Delta \sigma'$ 1 upon 1 plus e 0. Now, from this we can get this Δe as m_v into $\Delta \sigma'$ 1 plus e 0 and when we substitute here in the consolidation equation, then this S_c equal to $m_v H_0 \Delta \sigma'$. So, this expression can also be used to determine consolidation settlement.

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Settlement calculation from e-log σ' curve

If e is plotted against log σ' , the slope of the virgin compression curve (straight line portion) is called the compression index, C_c



This particular data, of which we obtain from the consolidation test, can also be plotted in different form in the form of e versus \log of σ dash curve. And this 1 such curve is shown here now. From here when we start that comp consolidation test at different σ dash we obtain value of e and we keep on plotting these values. Now, it is possible that after a particular stress has reached we can unload this and we allow this soil to expand and that expansion curve is shown by this line. It can be seen from here, that it does not follow the path of the compression curve. So, this is the expansion line there will always be permanent displacements or deformations which takes place due to readjustment of the particles. So, on the elastic compression or the elastic rebound, we obtain here when we unloaded.

And after unloading, it we can again reload, by the same intensity of load, and then we plot the e \log σ bar curve. You will find that after this particular pressure, has reached the at the pressure more than this the shape of the curve or the nature of the curve, it merges with the nature as if the soil has not been unloaded. So, here I am trying to explain the difference, between the normally consolidated soil and the over consolidated soil. Now, this is the curve for the normally consolidated soil and normally consolidated soils are those which have never experienced a pressure, which is existing at present. Now, in this particular case, we can see if we have the load the void ratio and σ bar curve for a particular soil, then this particular soil has already, experienced load corresponding to this particular stress.

Now, when we unload, it and when we load it reload it again, then we can say that this particular curve from here to here belongs to the over consolidated clays. And after that it merges with the normally consolidated clays. So, over consolidate clays are those clays which have been subjected to the pressure intensity, larger than the present pressure intensity. So, here from these 2 we can obtain the compression index C_c as well as recompression index C_r . Now, this recompression index is the average slope of this curve of the expansion as well as recompression. So, here this compression index is nothing, but the slope of the virgin compression curve, for the case of the normally consolidate clays. Whereas this slope is the slope of the recompression curve now, this you must have studied in the soil mechanics course.

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$$C_c = \frac{\Delta e}{\log \frac{\sigma_f}{\sigma_0}}$$

A general equation for computing consolidation settlement may therefore be written as follows,

$$S_c = C_c \frac{H_0}{1 + e_0} \log \frac{\sigma_f}{\sigma_0} = C_c \frac{H_0}{1 + e_0} \log \frac{\sigma_0 + \Delta \sigma}{\sigma_0}$$

So, from the $e \log \sigma$ worker of the normally, consolidate clays we can obtain compression index as Δe upon \log of σ_f dash divided by σ_0 dash. Now, from this, we can express this Δe in terms of C_c compression index. And hence, the general equation for computing consolidation settlement may therefore, be written as S_c equal to $C_c H_0$ upon $1 + e_0$ \log of σ_f dash divided by σ_0 dash.

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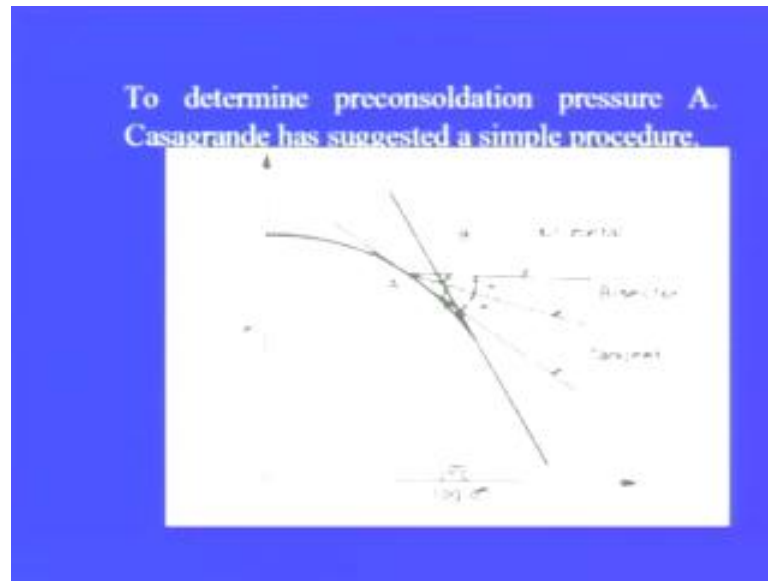
Thus the settlement can be computed by using Δe and a_v (or m_v) or C_c as input. While a_v and m_v are to be obtained for a particular pressure range, C_c is a constant, independent of stress increment.

The equation (with C_c) can be used for only if the soil is normally consolidated. If the soil is pre-consolidated, the soil will not be under virgin compression, when loaded, it will undergo recompression. It becomes, therefore, necessary to find out whether the soil is normally consolidated or pre-consolidated.

Thus the settlement can be computed by using Δe or a_v or m_v or C_c as input. While a_v and m_v are to be obtained for a particular pressure range, C_c is a constant, which is

independent of the stress increment for normally, consolidated clays only. The equation with C_c can be used for only, if the soil is normally, consolidated if the soil is pre-consolidated the soil will not be under virgin compression. When loaded it will undergo recompression it becomes therefore, necessary to find out whether the soil is normally, consolidated or pre-consolidated.

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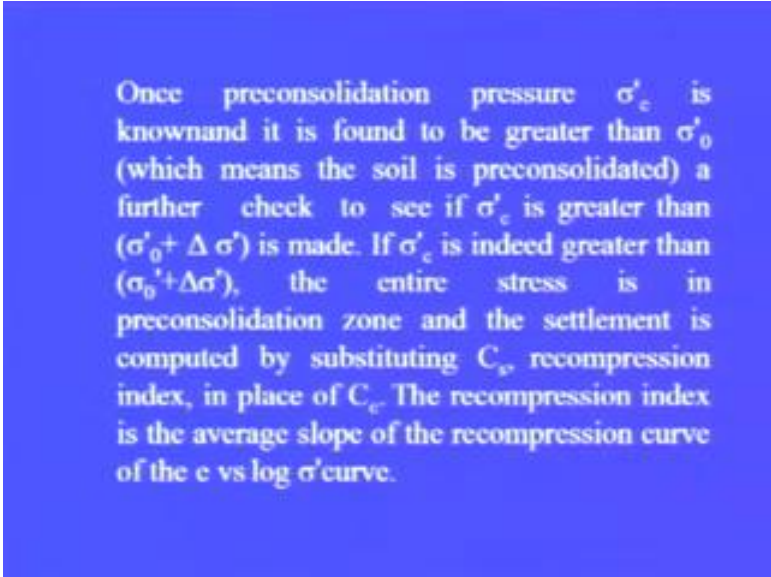


So, for that a method is given by A. Casagrande to determine, whether the soil will behave as normally, consolidated clay or the soil will behave as the pre-consolidated clay. So, from the same e \log of σ_v curve, we can obtain the preconsolidation pressure or over consolidation pressure. And then decide whether the soil will behave, for that particular stress range as the normally, consolidated or the pre-consolidated clay. Method is very simple, now, once we plot that e \log of σ_v curve. Now, from in this curve, we find out a point which has the maximum curvature and from that point let us say that point here is O point 8. We draw a horizontal line and tangent is drawn to this e \log σ_v curve from this point A. After drawing this tangent, we obtain the angle between the horizontal and tangent. Now, then we draw an angle bisector of this angle passing through point A.

Now, we have this as the angle bisector, then we extend the straight line portion of the normally consolidated soil. And when we extend it back wherever, it intersects the angle bisector, that is the point corresponding to preconsolidation pressure or over

consolidation, pressure that is σ_c . Now, the soil if the pressure range is on the side from here, to σ_c the soil will behave as the pre-consolidated clay. And for the pressure range more than σ_c it will behave as the normally consolidated clay. So, in this range we will have to use coefficient of recompression whereas, in this range we will have to use coefficient of compression to determine consolidation settlement and that may be, may become more clear by the next explanation.

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Once preconsolidation pressure σ'_c is known and it is found to be greater than σ'_0 (which means the soil is preconsolidated) a further check to see if σ'_c is greater than $(\sigma'_0 + \Delta\sigma')$ is made. If σ'_c is indeed greater than $(\sigma'_0 + \Delta\sigma')$, the entire stress is in preconsolidation zone and the settlement is computed by substituting C_r , recompression index, in place of C_c . The recompression index is the average slope of the recompression curve of the e vs $\log \sigma'$ curve.

Once preconsolidation pressure, σ_c is known and it is found to be greater than σ_0 , which means the soil is pre-consolidated a further check to see, if σ_c is greater than $\sigma_0 + \Delta\sigma$ is made. If σ_c is indeed greater than $\sigma_0 + \Delta\sigma$ also the entire stress range is in the preconsolidation zone. And the settlement is computed by substituting coefficient of recompression C_r or recompression index in place of C_c . The recompression index is the average slope of the recompression curve of e versus \log of σ curve.

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Now, here again the same trans, slide is projected now, this can be made more clear once we get sigma C dash bar reconsolidation pressure. So, if sigma C 0 bar is less than, this it means this is in the preconsolidation range and sigma 0 bar plus delta sigma bar again, that is also less than this. It means, this total stress range is less than sigma C bar and hence the, this is the case of pre-consolidated clay.

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The settlement is given by,

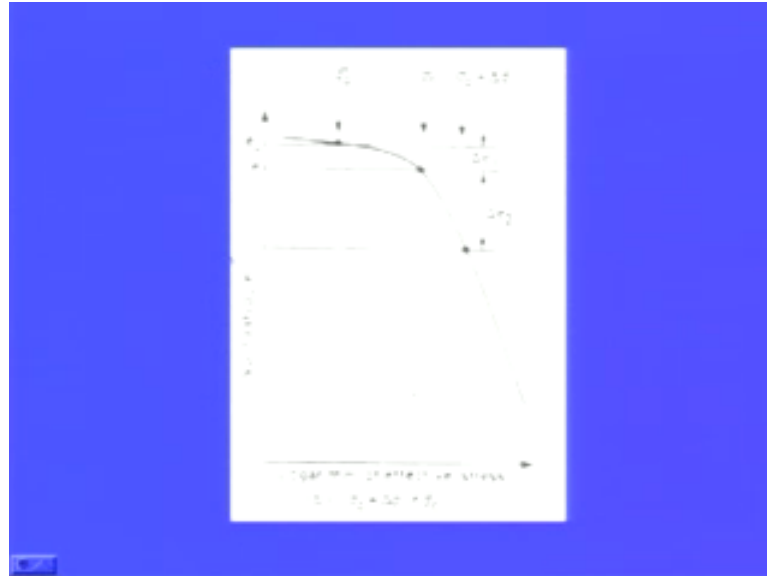
$$S_c = C_r \frac{H_0}{1+e_0} \log \frac{\sigma'_0 + \Delta\sigma'}{\sigma'_0}$$

When the increase in stress extends beyond the preconsolidation pressure into the virgin compression region, the settlement is determined in two parts.

Then the settlement is given by Sc equal to Cr H 0 upon 1 plus e 0 log of sigma 0 bar dash plus delta sigma dash divided by sigma 0 dash. Now, when the increase in stress

extends, beyond the preconsolidation pressure, in to the virgin compression region the settlement is determined in 2 parts.

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Now, let us consider another case σ_0 , this is σ_c that is the preconsolidation pressure and σ_0 is less than σ_c . So, the original overburden pressure are initial overburden pressure is less than preconsolidation pressure, but when we apply a load intensity of $\Delta \sigma$ at that middle of the clay, layer. Then if $\sigma_0 + \Delta \sigma$, becomes more than σ_c then it is in the range of the normally, consolidate clay. So, in such cases the settlement is determined in 2 parts either we can find out the change in void ratio from σ_0 to σ_c and substitute in the settlement equation. We will get settlement of this particular layer, we substitute this as Δe_1 . And in the next part from σ_c to $\sigma_0 + \Delta \sigma$ we get this Δe_2 . And for both these we can calculate settlement and then when we sum up we get the settlement of the consolidating layer. Or otherwise what we can do?

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a) for the stress increase from σ_0' to σ_c' on the recompression curve

$$S_{c1} = C_r \frac{H_0}{1+e_0} \log \frac{\sigma_c'}{\sigma_0'}$$

b) for the stress increase from σ_c' to $(\sigma_0' + \Delta \sigma')$ on the virgin curve

$$S_{c2} = C_c \frac{H_0}{1+e_0} \log \frac{\sigma_0' + \Delta \sigma'}{\sigma_c'}$$

For the stress increase from σ_0' to σ_c' on the recompression curve, we find out the recompression index and using this recompression index we calculate settlement S_{c1} . For the part which is in the preconsolidation range. And for the stress increase from σ_c' to $(\sigma_0' + \Delta \sigma')$ on the virgin compression curve, we calculate this. S_{c2} compression index H_0 upon $1 + e_0$ log σ_0' plus $\Delta \sigma'$.

Now, if we can see from here that this is the final stress and this is the initial stress for the preconsolidation range. This σ_c' is final stress, and for an initial stress is σ_0' whereas, for the normally, consolidated range $\sigma_0' + \Delta \sigma'$ is the final stress and σ_c' or σ_c' is the initial stress. So, we will have to keep these things in mind and we can calculate for S_{c1} and S_{c2} and when we sum up we get the consolidation settlement of the compressible layer.

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Solved Example

A footing, 2 m square, rests on a soft clay soil with its base at a depth of 1.5 m from ground surface. The clay stratum is 3.5 m thick and is underlain by a firm sand stratum. The clay soil has the following properties:

$$w_L = 30\%, \quad w_n = 40\%, \quad G_s = 2.70,$$
$$\Phi_u = 0^\circ, \quad c_u = 0.5 \text{ kg/cm}^2$$

Now, this can be explained by a solved example. A footing 2 meter square rests on a soft clay soil, with its base at a depth of 1.5 meter from ground surface. The clay stratum is 3.5 meter thick and is underlain by a firm sand stratum; the clay soil has the following properties. Liquid limit as 30 percent, natural water content as 40 percent, specific gravity of soil solids is 2.7 Φ_u that is 0, because this is the case of clay and c_u equal to 0.5 kg per centimeter square.

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It is known that the clay stratum is normally consolidated. Using Skempton's equation, determine the net safe bearing capacity of the footing. Compute the settlement that would result if this load intensity were allowed to act on the footing. Natural water table is quite close to the ground surface.

It is known that the clay stratum is normally consolidated. Using Skempton's equation determine the net safe bearing capacity of the footing, compute the settlement that would result if this load intensity were allowed to act on the footing, natural water table is quite close to the ground surface.

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Solution:

$$D_f/B = 1.5/2 = 0.75 < 2.5$$

Hence from Skempton equation,

$$N_c = 5.0(1 + 0.2 D_f/B)(1 + 0.2 B/L) = 6.9$$

$$q_{ult} = c_u N_c = 5 * 6.9 = 34.5 \text{ t/m}^2$$

$$q_{ns} = 34.5 / 3 = 11.5 \text{ t/m}^2$$

$$\gamma_{sat} = [(G_s + e)/(1 + e)] \gamma_w$$

$$e = w_n G_s = 0.4 * 2.7 = 1.08$$

$$\gamma_{sat} = 1.82 \text{ t/m}^3 \text{ and } \gamma' = 1.82 - 1 = 0.82 \text{ t/m}^3$$

Now, using Skempton's equation, we can find out the net ultimate bearing capacity of the foundation. In order to get that we first of all find out what is D_f by B . In this particular case this D_f by B is equal to 1.5 divide by 2 that is 0.75 that is less than 2.5. Now, when it is less than 2.5 then N_c is given by this expression, this we have already, discussed in the lecture, N_c equal to 5 plus 1 plus 0.2 D_f by B 1 plus 0.2 B upon L . When we substitute these dimensions, we will get this N_c equal to 6.9. And net ultimate bearing capacity is, for the case of clay soils in which ϕ equal to 0 is $c_u N_c$. So, N_c we obtain from here, c_u is given, so, 5 into 6.9 that is 34.9, 34.5 ton per meter square. Now, q net safe can be obtain, if we know net ultimate bearing capacity if we divide it by factor of safety, we get this as 11.5 ton per meter square. Now, in order to determine the overburden stress, we need to know the value of saturated unit weight of the soil. So, for that this saturated unit weight can be determine by this formula G_s plus e upon 1 plus e , whole multiplied by unit weight of water γ_w . Now, this e can be determined, for a saturated soil as water content into the specific gravity of soil solids. So, here water content is 40 percent, 0.4 into 2.7 the void ratio will be 1.08. And hence γ , if we substitute this void ratio here and unit weight of water. We get γ saturated,

saturated unit weight of soil, solid soil as 1.82 ton per meter cube. And submerged unit weight, if simply we deduct minus 1 that is gamma saturated minus gamma w, that is equal to 0.82 ton meter cube.

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For a normally consolidated clay,

$$S_c = C_c \frac{H_0}{1 + e_0} \log \frac{\sigma'_0 + \Delta \sigma'}{\sigma'_0}$$

$$C_c = 0.009(w_L - 10) = 0.18$$

Effective pressure due to overburden at 2.5m
(middle of consolidating clay layer)

$$\sigma'_0 = 0.82 * 2.5 = 2.05 \text{ t/m}^2$$

Assuming a load spread of 2 : 1

$$\Delta \sigma = 11.5 * 2^2 / 3^2 = 5.1 \text{ t/m}^2$$

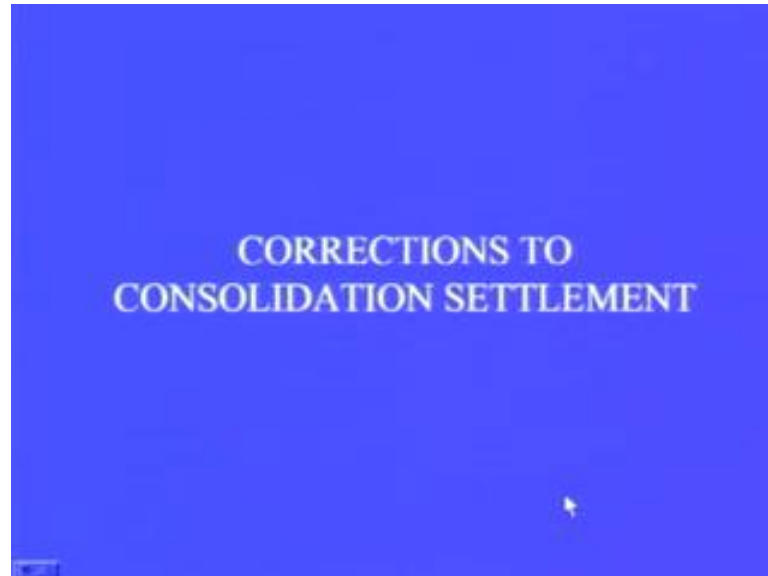
$$S_c = 0.18 \frac{2000}{1 + 1.08} \log \frac{2.05 + 5.1}{2.05} = 94 \text{ mm}$$

Now, for a normally, consolidated clay S_c will be given by $C_c H_0$ upon $1 + e_0$ log to the base 10, $\sigma'_0 + \Delta \sigma'$ divided by σ'_0 . Where this compression index can also be determine by imperial correlation, which says that C_c equal to $0.009 WL$ minus 10 . So, in the absence of the consolidation test data, there are many correlations given by various researchers, by which we can determine compression index also. Now, a popular relationship is C_c equal to $0.009 WL$ minus 10 , when we substitute liquid limit of the soil then we of get this compression index as 0.18 .

So, in order to determine, effective pressure due to the overburden at 2.5 meter, which corresponds to the middle of consolidating layer that will be equal to effective unit weight that is the submerged unit weight 0.82 multiplied by the depth that is 2.5 equal to 2.05 ton per meter square. Now, assuming, a load spread of 2 vertical is to 1 to find out the increase in stress at the middle of the consolidating layer. We get $\Delta \sigma$ equal to 11.5 now, 11.5 is the net safe bearing capacity, which we have obtained earlier into this 2 square divided by 3 square. That is equal to 5.1 ton per meter square. So, by using the approximate approach of 2 is to 1 we can find out $\Delta \sigma$ now, when we

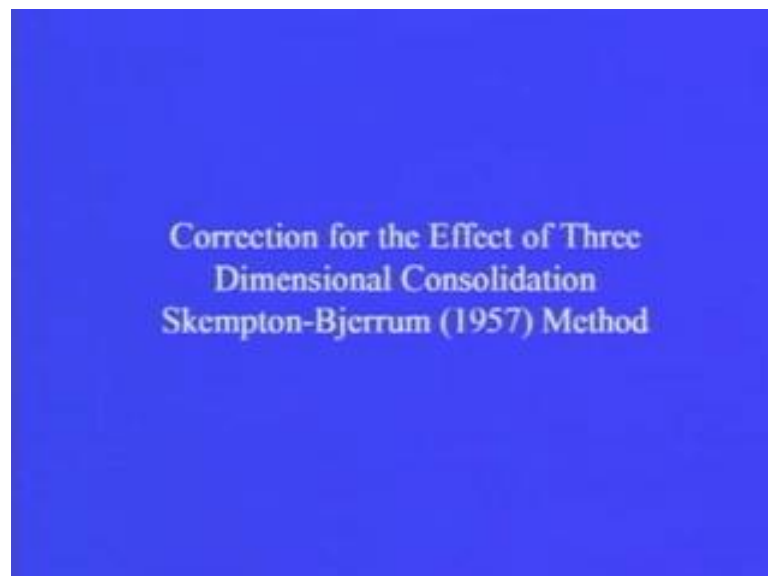
substitute all these values into consolidating consolidation equation we get consolidation settlement as 94 millimeter.

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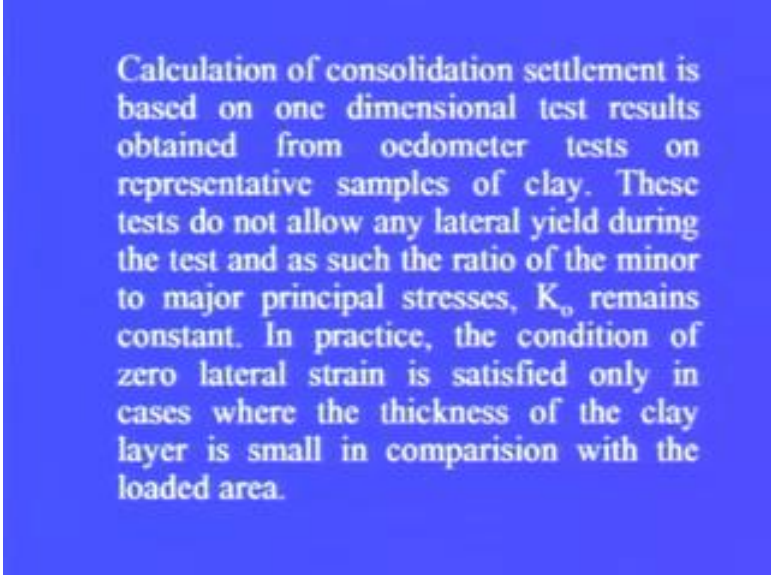
Now, whatever consolidation settlement or whatever settlement, we have discussed so far those settlements are to be corrected for three dimensional, consolidation. Now, here whatever, settlements we have determined that is for the 1 dimensional case, but actual in c 2 soil is confined from all the directions. So, that is the case of 3 dimensional consolidation.

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So, we will have to make corrections, on the settlement, which we obtain from 1 dimensional consolidation test data. A method is suggested by Skempton's.

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Calculation of consolidation settlement is based on one dimensional test results obtained from oedometer tests on representative samples of clay. These tests do not allow any lateral yield during the test and as such the ratio of the minor to major principal stresses, K_0 , remains constant. In practice, the condition of zero lateral strain is satisfied only in cases where the thickness of the clay layer is small in comparison with the loaded area.

Now, calculation of consolidation settlement is based on, 1 dimensional consolidation test results, obtained from oedometer tests on representative samples of clay. These test tests do not allow any lateral yield during the test and as such the ratio of minor to major major principal stresses, that is K_0 remains constant. In practice the condition of 0 lateral strain, satisfied only in case where the thickness of the clay layer is small in comparison with the loaded area.

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In many practical solutions, significant lateral strain will occur and the initial pore water pressure will depend on the INSITU stress condition and the value of pore pressure coefficient A , which will not be equal to unity as in the case of one dimensional test. In view of the lateral yield, the ratios of the minor and major principal stresses due to a given loading at a given point in a clay layer do not maintain a constant K_0 .

In many practical solutions significant lateral strain will occur and the initial pore water pressure will depend on the INSITU stress condition, and the value of pore pressure coefficient A . Which will not be equal to unity as in the case of 1 dimensional test in view of the lateral yield the ratios of the minor and major principal stresses dye to a given loading at a given point in a clay layer, do not remain maintain a constant K naught.

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The initial excess pore water pressure at a point P in the clay layer is given by the expression

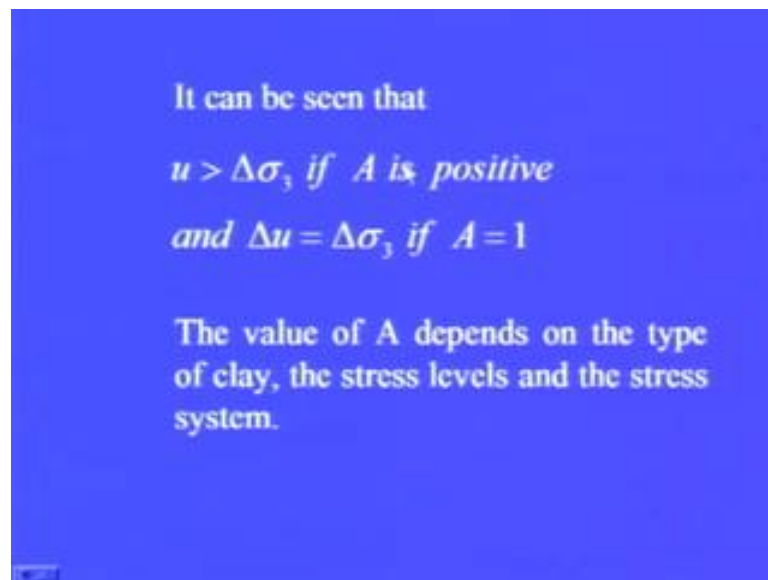
$$\Delta u = \Delta \sigma_3 + A(\Delta \sigma_1 - \Delta \sigma_3)$$

$$\Delta u = \Delta \sigma_1 \left[A + \frac{\Delta \sigma_3}{\Delta \sigma_1} (1 - A) \right]$$

where $\Delta \sigma_1$ and $\Delta \sigma_3$ are the total principal stress increments due to surface loading.

Now, this initial excess pore water pressure, at a point P in the clay layer is given by the expression $\Delta u = \Delta \sigma_3 + A(\Delta \sigma_1 - \Delta \sigma_3)$ this is the given equation given by Skempton. And Δu is the increase in pore water pressure, which we call as the excess pore water pressure, and this is the pore water pressure due to dissipation of which consolidation settlement takes place. And that will be equal to increase in the minor principal stress $\Delta \sigma_3$ and multiplied by a pore pressure coefficient A, multiplied by $\Delta \sigma_1 - \Delta \sigma_3$ that we can. We call it as increase in the deviatoric stress. So, this Δu can be written as $\Delta \sigma_1$ total multiplied by $A + \Delta \sigma_3$ upon $\Delta \sigma_1 - A$. Where $\Delta \sigma_1$ and $\Delta \sigma_3$ are the total principal stress, increments due to surface loading.

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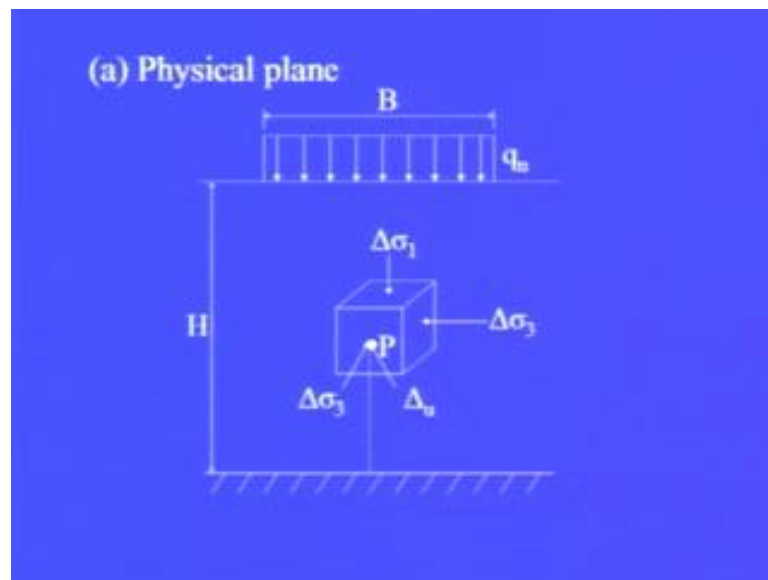
It can be seen that, u is greater than $\Delta \sigma_3$, if A is positive and Δu is equal $\Delta \sigma_3$ if A is equal to 1. The value of A depends on the type of clay the stress levels and the stress system, it also depends on the over consolidation ratio.

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The figures shown next present the loading condition at a point in a clay layer below the center line of circular footing showing conditions before loading, immediately after loading and after consolidation.

The figure shown, next present the loading condition at a point in a clay layer below the center line of circular footing showing conditions, before loading immediately after loading and after consolidation.

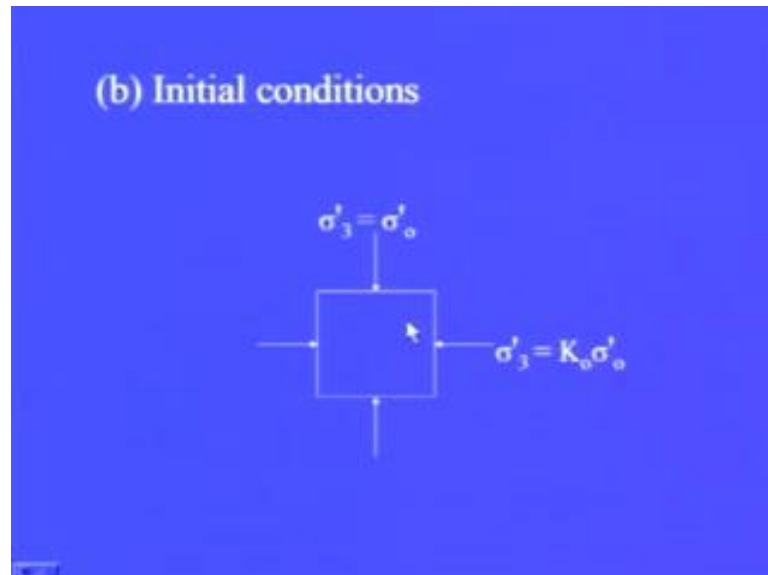
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Now, this is a point p which is consider in the consolidating layer of thickness H . Now, at this point P , if we consider a differential element, the then the stress conditions are $\Delta\sigma_1$, $\Delta\sigma_3$, $\Delta\sigma_3$ and the pore water pressure Δu . So, if a

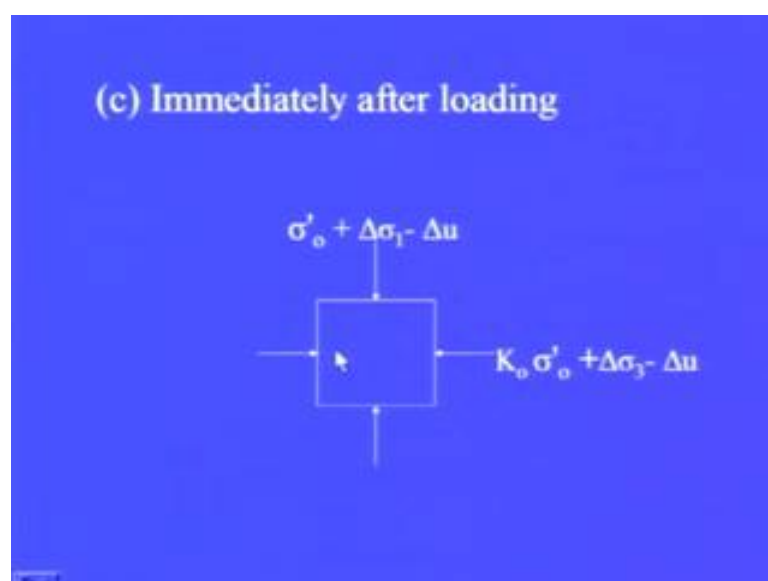
load is applied of net load intensity qn . So, this, the stress conditions at point P are as given below.

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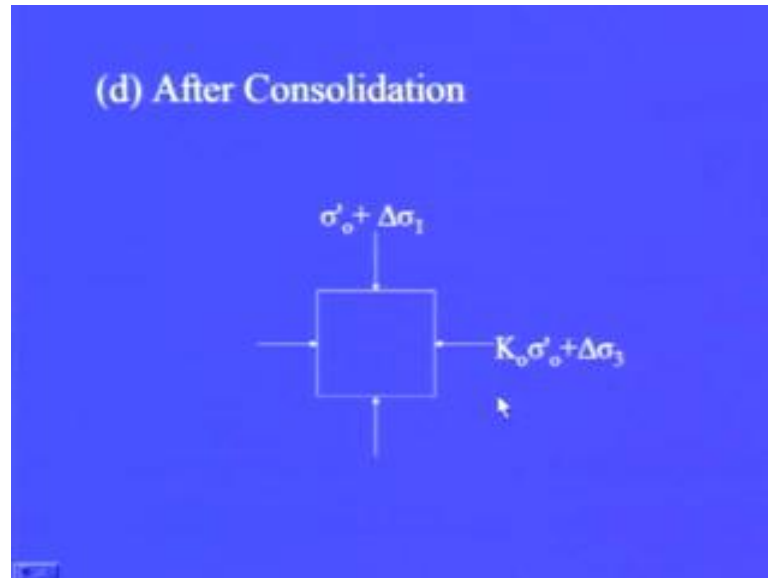
Now, initial conditions are σ_3 dash equal to σ_0 dash whereas, in the vertical direction. This can, we can determine as γ dash into the depth under consideration of the point P, below the ground surface. And σ_3 dash is equal to K not σ_0 dash that is the lateral stress.

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Now, immediately after loading there will be an increase in delta sigma 1. So, this will be sigma 0 dash plus delta sigma 1 minus delta u. And lateral stress will be K not delta sigma 0 dash plus delta sigma 3 minus delta u.

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After consolidation is over all the delta sigma u, which has got increased has got dissipated. And that is the excess pore water pressure. Now, after consolidation process over then this will, become sigma 0 dash plus delta sigma 1 k 0 delta sigma, sigma 0 dash plus delta sigma 3.

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By the one dimensional method, consolidation settlement S_{oc} is expressed as,

$$S_w = \int_0^H m_v \Delta\sigma_v dz$$

By the Skempton-Bjerrum method, consolidation settlement S_{oc} is expressed as,

$$S_w = \int_0^H m_v \Delta\sigma dz = \int_0^H m_v \Delta\sigma_v \left[A + \frac{\Delta\sigma_2}{\Delta\sigma_1} (1 - A) \right] dz$$

By the 1 dimensional method, consolidation settlement is expressed as, in terms of coefficient of volume change 0 to H $m_v \Delta \sigma_3 dz$, where $d dz$ is the differential layer of consolidation. By Skempton-Bjerrum method consolidation settlement is expressed as this in in place of $\Delta \sigma$. We substitute this as Δu and it will be equal to 0 to H $m_v \Delta \sigma_1 A$ plus $\Delta \sigma_3$ upon $\Delta \sigma_1$ $1 - A$ into dz .

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A settlement coefficient μ is used, such that

$$S_c = \mu S_{oc}$$

The expression for μ is

$$\mu = \frac{S_c}{S_{oc}} = \frac{\int_0^H m_v \Delta \sigma_1 \left[A + \frac{\Delta \sigma_3}{\Delta \sigma_1} (1 - A) \right] dz}{\int_0^H m_v \Delta \sigma_1 dz}$$

A settlement coefficient μ is used such that S_c equal to μ into S_{oc} which we determine from the method. The expression, for μ will then be equal to S_c upon S_{oc} . So, this will be equal to 0 to h $m_v \Delta \sigma_1$ in bracket multiplied by A plus $\Delta \sigma_3$ divided by $\Delta \sigma_1$, $1 - A$ into dz divided by 0 to H $m_v \Delta \sigma_1 dz$ where this we determine from the 1 dimensional consolidation equation.

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It can be assumed that m_v and A are const. with depth (sub layers can be used in the analysis), then μ can be written as,

$$\mu = A + (1 - A)\alpha$$

where, $\alpha = \frac{\int_0^H \Delta\sigma_3 dz}{\int_0^H \Delta\sigma_1 dz}$

It can be assume that m_v and A are constant, with depth. Sub layers can be used in the analysis. Then μ can be written as $\mu = A + (1 - A)\alpha$ where α factor is given, by $\int_0^H \Delta\sigma_3 dz$ divided by $\int_0^H \Delta\sigma_1 dz$.

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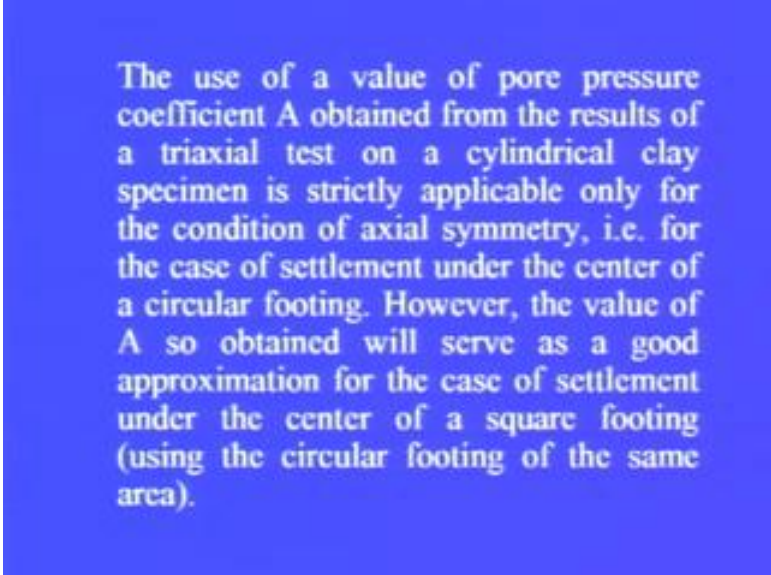
Taking Poisson's ratio as 0.5 for a saturated clay during loading under undrained conditions, the value of settlement coefficient depends only on the shape of the loaded area and the thickness of the clay layer in relation to the dimensions of the loaded area and Poisson's ratio can be estimated from elastic theory.

The value of initial excess pore water pressure (Δu) should correspond to the in-situ stress conditions.

Taking Poisson's ratio as 0.5 for a saturated clay, during loading under undrained conditions the value of settlement coefficient depends, only on the shape of the loaded area. And the thickness of the clay layer in relation to the dimensions of the loaded area,

and Poisson's ratio can be estimated from elastic theory. The value of initial excess, pore water pressure Δu , should correspond to the ((refer time: 45:59)) stress conditions.

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The use of a value of pore pressure coefficient A obtained from the results of a triaxial test on a cylindrical clay specimen is strictly applicable only for the condition of axial symmetry, i.e. for the case of settlement under the center of a circular footing. However, the value of A so obtained will serve as a good approximation for the case of settlement under the center of a square footing (using the circular footing of the same area).

The use of a value of pore pressure coefficient A , obtained from the results of a triaxial test on a cylindrical clay specimen is strictly applicable only, for the condition of axial symmetry. That is for the case of settlement under the center of a circular footing, however, the value of A . So, obtained will serve as a good approximation for the case of settlement under the center of a square footing using the circular footing of the same area.

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Under a strip footing plane strain conditions prevail, Scott(1963) has shown that the value of Δu approximate in the case of a strip footing can be obtained by using a pore pressure coefficient A_s as

$$A_s = 0.866A + 0.211$$

The coefficient A_s replaces A for the case of strip footing, the expression for α being unchanged.

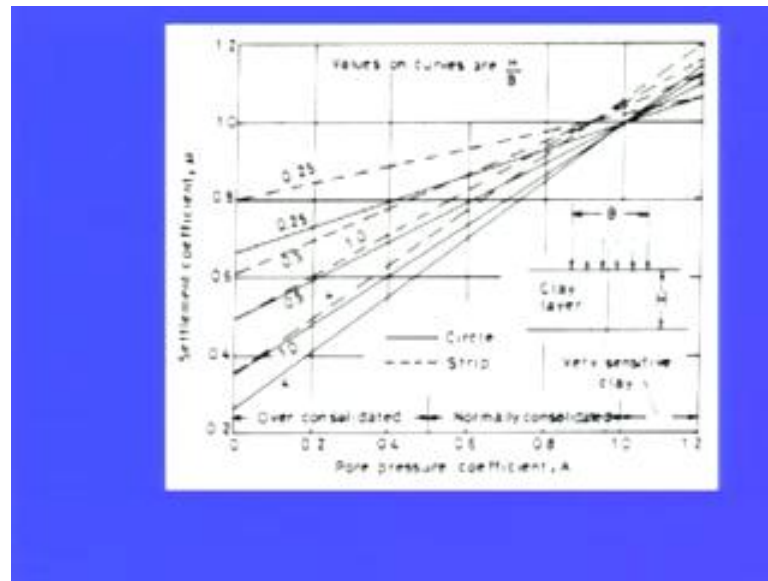
Under a strip footing plane strain conditions prevail. Scott 1963 has shown that, the value of Δu approximate in the case of a strip footing, can be obtained by using a pore pressure coefficient A as, A_s equal to $0.866A + 0.211$ the coefficient as, replaces A for the case of strip footing the expression for α being unchanged.

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The settlement coefficient μ as shown in next figure, is a function of the type of soil (or the A value) and the shape of foundation. This method is recommended for adoption by IS:8009 (Part I)-1976.

The settlement coefficient μ , as shown in next figure is a foundation of the type of soil or the A value and the shape of the foundation. This method is recommended for adoption by IS 8009 part I 1976.

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So, this value of μ , settlement coefficient μ can be obtained from this particular figure. Now, here this is the index figure in which this B is the width of the loaded area, H is the thickness of the clay layer and pore pressure coefficient A is given here ranging from 0.2 to 1.2 for various clays like. Over consolidated clay, from here to here for normally consolidated clay from 0.45 to 1 and for very sensitive clay 1 to 1.2. Now, this settlement coefficient is a function of the ratio H by B . So, these are given for different values of H by B , this settlement coefficient is also a function of the shape of the footing. So, for a circular footing, these are solid, solid lines are for the circular footing and dash lines are for the strip footing.

So, this particular chart can be used to determine value of the settlement coefficient μ , for different values of over consolidation pore pressure coefficient A . So, for we can make use of this for example, let us say we want to determine the value for a circular footing. So, depending upon the value of A , let us say value of A is 0.4. So, for the circular footing for H by B ratio equal to let us say 0.5 this is the H by ratio equal to 0 point 5 and from this, we can get this value of settlement coefficient. This settlement coefficient can be used to correct the settlement to take into account the 3 dimensional state of the stress. So, in today's lecture I have tried to explain the methods to determine consolidation settlement.

And then, this consolidation settlement is actually for the 1 dimensional consolidation condition whereas N_c conditions are always 3 dimensional. So, we will have to make corrections for 3 dimensional state of a stress and I have this discussed this method given by Skempton to find out the coefficient of a settlement. That is the settle settlement coefficient μ for different shapes of footing and for different value of H by B ratio. And if we know the value of A we can get this settlement coefficient and the settlement can be corrected. In the next lecture, I will further extend different other corrections, which are used in the settlement one dimensional consolidation settlement and then finally, how to obtain the settlement of the structure.

Thank you