

Foundation Engineering
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Module - 01
Lecture - 04
Shallow Foundation

So, friends I again welcome you for this lecture series on shallow foundation. So, far we have discussed the Terzaghi bearing capacity equation where half bearing capacity equation considering all these say factors inclination factors and dap factors. And the modifications in the bearing capacity, parameter, parameters bearing capacity factors like N_c N_q N_γ we have also seen the Skempton, bearing capacity parameters for the cohesive soils. And we have discussed several solved problems so, as to use how to use, so as to make use of these equations for various shapes and to determine the unknown parameters. Now, the parameters which are required are the strength parameters and the bearing capacity factors.

Now, a strength parameters c and ϕ can be determined in laboratory by conducting laboratory test like triaxial test or may be directional test or sometimes unconfirmed compression test. The N_q N_γ and N_c parameters are the functions of ϕ and by using equations those developed by either Mayer Half or Terzaghi or Henson or Wersik we can find out those parameters and substitute in the bearing capacity equation. We have also discussed the procedure which is suggested in IS 6 4 0 3 1981 which is nothing but the procedure given by Brinch Hansen and in which the effect of water table correction is also taken into account.

Now, there are few methods which are available to determine ultimate bearing capacity of foundations based on the field test. So, in field, we normally conduct plate load test extended validation test and if required for a special cases and if the requirement is necessary then we also conduct static cone penetration test. And then from those test we also determine the parameters strength parameters or sometimes be directly determine parameter N_γ and from N_γ we find out ϕ and then other parameters are determined.

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Ultimate Bearing Capacity of Footings Based on Standard Penetration Resistance (N) Values

So, one such method is, the ultimate bearing capacity of footings based on extended penetration resistance value. As far as the procedure is concerned, and that is already covered in the x geo technical, explanation by a Professor Mahindra Singh. In this lecture series what we do for the, this method is very suitable for the case of granular soils and mostly in granular soils the stress conditions are such that we get c equal to 0.

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Granular Soils ($c = 0$)

The average of corrected N values between the level of base of footing and a depth equal to 1.5 to 2.0 times the width of footing below the base, is determined for each of the locations.

The minimum of the average of corrected N values for different boreholes is used in the design.

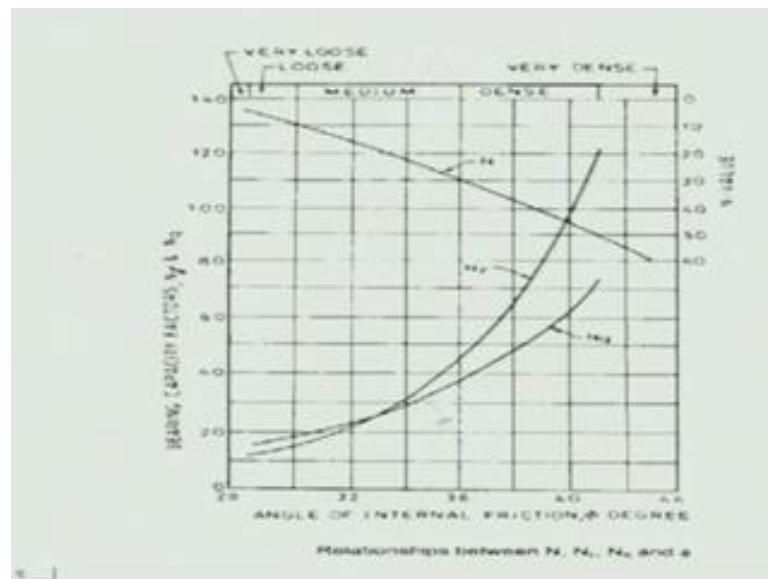
The relation between N and Φ established by Peck et al., (1974) is given in a graphical form in the next figure

So, we also sometimes call these as the cohesion less soils and we find out the N value as PT extended penicillin test value N at different depths. And that N value is corrected for

overburden and dilatancy. Normally the corrected N values between the level of base of footing and a depth equal to 1.5 to 2 times the width of footing below the base is determined for each locations. And as we know that these standard penicillin tests are conducted in the boreholes and we advanced borehole may be up to 12 meter 15 meter and at each 1.5 meter depth we conduct this test.

So, these values are observed and observed values then corrected for overburden or dilatancy wherever required depending upon the water table or the type of soil. The minimum of the average of corrected N values for different boreholes is used in the design. Now, in our particular project normally depending upon the requirement 4 5 boreholes at least are conducted and the average corrected values are determined for a depth equal to 1.5 to 2 times the width of the footing below the base and the minimum of the average of corrected N values is used in the design. Peck et al has given a relation between the standard penetration test N and phi in the graphical form which I am going to show in the next figure.

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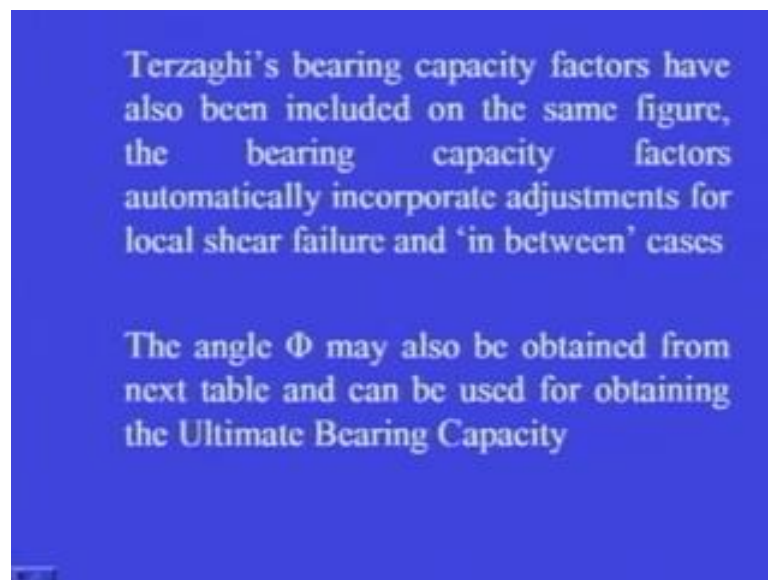


Now, this is the figure in which N values are given and corresponding to these N values phi value is also given. So, corrected N for the corrected N values let us say corrected N values are 20. So, corresponding phi will be between 32 to 34 degrees it is around 33 degrees. Now, from the N value it can be seen that the sand can be classified as very loose or loose or medium or dense or very dense. Now, if the sand is very loose naturally

there will be local shear failure possibility of local shear failure is more than in the case of very dense sand there is a possibility of general shear failure.

So, either we take ϕ value from here or then N_c N_q N_γ parameters can be determined from the Terzaghi table or directly from this chart in which the intermede the values are covered from local shear failure case to general shear failure case this is the chart given by Peck et al. So, here for the given value of N we can directly find out what is the value of N_γ ? And what is the value of N_q ? So, Terzaghi bearing capacity factors have also been included on the same figure as we have seen the bearing capacity factors automatically incorporate.

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Adjustments for local shear failure and a in between cases between local shear to general shear, because no guidance is given for such values. The angle ϕ may also be obtained from the next table and can be used for obtaining the ultimate bearing capacity.

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N Value	ϕ^0	Relative Density (%)	Description
<4	25-30	0	Very loose
4-10	27-32	15	Loose
10-30	30-35	65	Medium
30-50	35-40	85	Dense
>50	38-43	100	Very dense

So, these are the correlations which are given for the granular soil we call cohesion less soils also. Now, if we find that the corrected N values is less than 4 then phi can be taken between 25 to 30 degrees and in that case relative density is 0 and it means the soil is sand is in the very loose condition. Similarly, if it is between 4 to 10 then phi can be taken as 27 to 32 relative density is around 15 percent it is described as loose sand. If it is 10 to 30 we can take 30 to 35 relative density 65 percent and it is described as medium sand. Similarly, 30 to 50 35 to 40 degrees we can take phi value then relative density is around 85 degree or 85 percent and it is dense sand. If the N value is 50 greater than 50 then we say that it is the case of refusal and mostly this we get in the case of very dense sand in which phi value is of the order of 38 to 43 degrees and relative density can be considered as 100 percent. So, if the N values are known we can directly find out the, or estimate the value of angle of shearing resistance.

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Teng's (1962) has developed the following empirical equations for the net ultimate bearing capacity, q_{um} of footings on granular soils.

For continuous or strip footings:

$$q_{um} = \frac{1}{60} \left[3N^2 BR_w + 5(100 + N^2) D_f R_w \right] \text{ t/m}^2$$

For square and circular footings:

$$q_{um} = \frac{1}{30} \left[N^2 BR_w + 3(100 + N^2) D_f R_w \right] \text{ t/m}^2$$

Teng's 1960 has developed the following empirical equations for the net ultimate bearing capacity of footing on granular soils. He has developed these for the continuous or strip footings as well as a square and circular footing. For the strip footings this q_{um} can be determined by $\frac{1}{60} [3N^2 BR_w + 5(100 + N^2) D_f R_w]$ in tonne per meter square. Now, we can convert this into kilonewton per meter square also. For square and circular footing this is $\frac{1}{30} [N^2 BR_w + 3(100 + N^2) D_f R_w]$ in tonne per meter square.

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Cohesive Soils

The unconfined compressive strength of clay may be obtained as

$$q_u = 2c_u = k' * N$$

where the value of coefficient k' may vary from a minimum of 12 to a maximum of 25.

Next table provides UCS based on N values

From q_u the net ultimate bearing capacity can be found following Skempton's approach.

The N values are also related to the unconfined compressive strength as well as. From unconfined compressive strength we can determine the undrained cohesion which can be used in the calculation of bearing capacity. The unconfined compressive strength of clay may be obtained as q_u equal to this is the undrained or unconfined compressive strength. Sometimes this undrained is, because if we conduct unconsolidated undrained test in triaxial then this is the strength in undrained condition for the fully saturated soil and that becomes equal to 2 times undrained cohesion and it is equal to $K \cdot N$ where the value of coefficient K may vary. It is from a minimum of 12 to a maximum value of 25. So, in next tables table provides UCS based on N value. Now, from q_u the net ultimate bearing capacity can be found following the Skempton's approach.

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Correlations with N for Cohesive Soils

N Value	UCS (kPa)	Consistency
<2	<25	Very soft
2-4	25-50	soft
4-8	50-100	Medium
8-16	100-200	Stiff
16-32	200-400	Very stiff
>32	>400	Hard

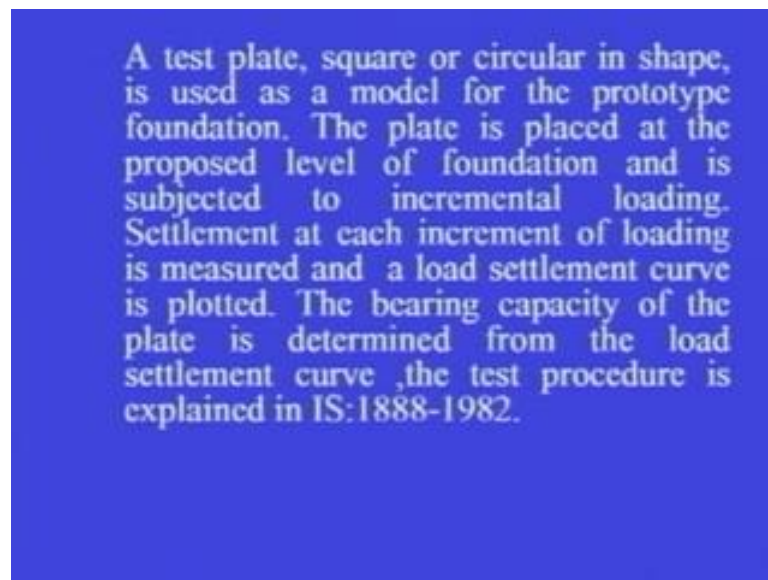
So, here these N values are also correlated to the unconfined compressive strength value. Here these are given in kilo Pascal and these are related to the consistency of soil. For example if we get very low value less than 2 then it is the consistency of the soil is very soft. And we can consider that the unconfined compressive strength in this case will be less than 25 kilo Pascal. If it is between 2 and 4 this is 25 to 50 kilo Pascal soft consistency; 4 to 8 50 to 100 kilo Pascal medium consistency; 8 to 16 100 to 200 kilo Pascal is stiff consistency; 16 to 32 200 to 400 kilo Pascal very stiff. And if it is greater than 32 then the unconfined compressive strength will be more than 400 kilo Pascal and it is a very hard clay.

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Another test which we normally use in the case of again granular soil which is most suitable for granular soil we that test is plate load test. And from the plate load test data we can find out ultimate bearing capacity of footings.

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Now, in the plate load test or test plate, square or circular in shape, is used as a model for the prototype foundation. The plate is placed at the proposed level of foundation and is subjected to incremental loading. Settlement at each increment of loading is measured

and a load settlement curve is plotted. The bearing capacity of the plate is determined from the plate load settlement curve, and the test procedure is explained in IS 1888 1982.

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Briefly, the test Procedure is explained as below:

- Rough mild steel plates 30 cm, 60 cm or 75 cm size, square in shape, are used. The smaller sizes are used in dense or stiff soils and larger sizes in loose or soft soils. A pit of dimensions not less than five times the width of the plate is excavated up to proposed depth of foundation and the test plate is seated at the center over a fine sand layer of maximum thickness 5mm.

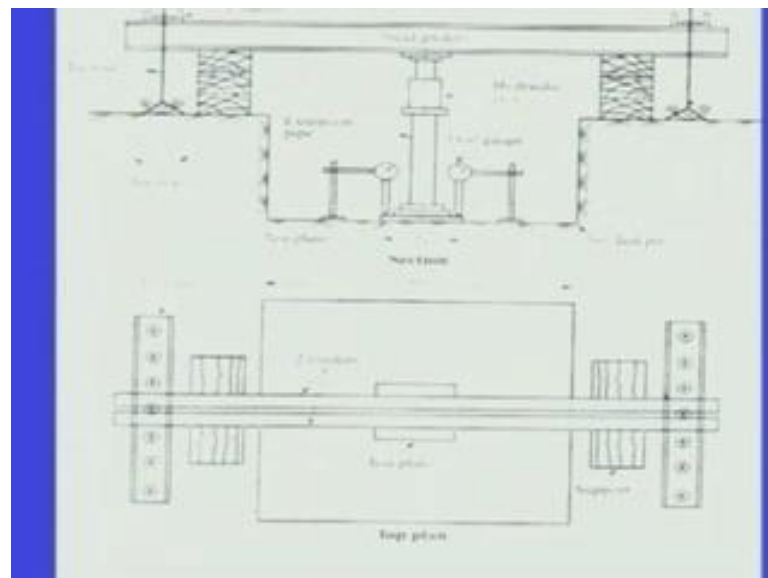
Briefly I will discuss the procedure here and although the procedure must have been describe by Professor Mahindra Singh. So, briefly I am going to discuss this procedure which is explained below. Rough mild steel plates 30 centimeter 60 centimeter or 75 centimeter in size, square in shape, are used. The smaller sizes are used in dense or stiff clays and larger sizes in loose or soft soils. A pit of dimensions not less than 5 times the width of the plate is excavated up to the proposed depth of foundation. And the test plate is seated at the center over a fine sand layer of maximum thickness 5 millimeter.

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- If the water table is above the level of the test pit, water is carefully pumped out to bring down the water table to the level of foundation before seating the test plate.
- Loads on the test plate may be applied by gravity loading or reaction loading. For gravity loading, a platform is constructed on a vertical column resting on the plate. Loading on the plate is done by placing weighted sand bags on the platform. In reaction loading, the load is applied through proving ring and hydraulic jack by taking reaction against a fixed support. Next figure shows the plate load test set up.

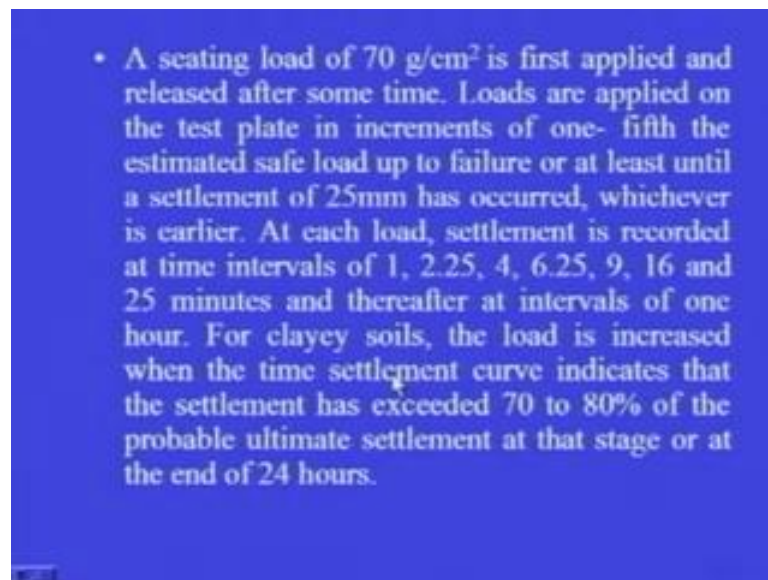
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Now, this particular figure, in this particular figure you can see that there is an excavation of the 5 times the width of the test plate. So, this is the test plate and 5 times the width the depth of the foundation is up to the level proposed level of foundation. Test plate is placed and over that column is there and from this column which is the extension pipe. The load is applied by hydraulic jack and the reaction is taken from these steel guarders while these guarders may be faced by anchors. So, the reaction is taken by the soil or the anchoring axial. Now, these are like ISHB or ISMB channels deformation of this plate due to the loading is determined or measured by the deformation dial gauges 4 dial gauges are used or sometimes at least 2 dial gauges are placed diametrically opposite to the test plate. The plan of this setup is shown in this figure. Now, these are anchors are fixed by nut and bold arrangement here.

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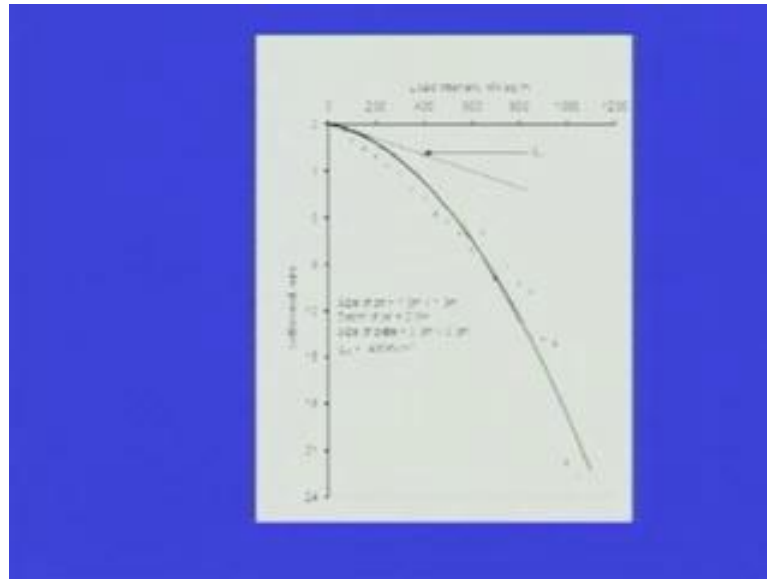
A seating load of 70 gram per centimeter square is first applied and released after sometime. Loads are applied on the test plate in increments of one-fifth the estimated safe load up to failure or at least until a settlement of 25 millimeter has occurred whichever is earlier. At each load settlement is recorded at time intervals of 1 minute, 2.25 minute, 4 minute, 6.25 minute, 9, 16 and 25 minutes and thereafter at intervals of 1 hour. For clayey soils the load is increased when the time settlement curve indicates that the settlement has exceeded 70 to 80 percent of the probable ultimate settlement at that stage or at the end of 24 hours. For soils other than clayey soils the load is increased when the rate of settlement drops to a value less than 0.02 millimeter per minute.

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- For soils other than clayey soils, the load is increased when the rate of settlement drops to a value less than 0.02 mm/min. The minimum duration for any load shall, however, be 60 min.
- Settlements are recorded through a minimum of two dial gauges mounted on independent datum and resting on diametrically opposite ends of the plate. Dial gauges with 25 mm travel and capable of measuring settlements to an accuracy of 0.01mm, are used.
- The load settlement curve for the test plate is plotted.

The minimum duration for any load shall; however, be 60 minute. Now, this as we know that the settlement depends on the type of soil in the case of coarse grain soils or the granular soils. The settlement takes place the rate of settlement is very high and settlement takes place quickly. Whereas, in the case of cohesive soils or in the case of fine grain soils the rate of settlement is very slow. So, it may take longer time. Settlements are recorded through a minimum of 2 gauge dial gauges mounted on independent datum and resting on diametrically opposite ends of the plate dial gauges with 25 millimeter travel. And capable of measuring settlements to an accuracy of 0.1 millimeter are used. The load settlement curve for the plate is then plotted.

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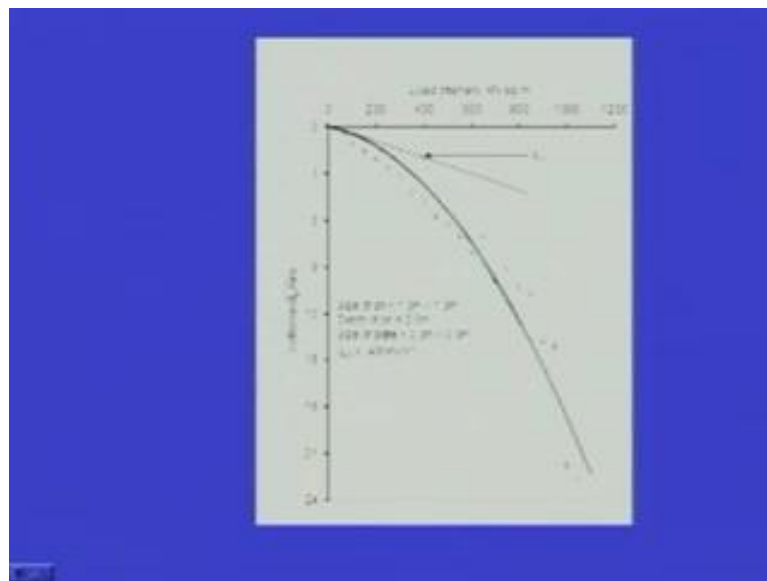
Now, here you can see this is the load intensity versus the settlement curve a typical curve for the plate load test data. Now, it is quite possible that these are all the object points and a best fit is plotted for this particular data. Now, from this plate load test data which is the load settlement either we can plot in terms of load and settlement or in the form of load intensity versus settlement. This is can be used to determine ultimate bearing capacity of the plate.

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The load settlement curve obtained from a plate load test can be used to determine ultimate and the safe bearing capacities of the foundation. Where the failure is easily identifiable by its distinct peak (general shear failure), the ultimate capacity, q_{up} of the test plate can be determined corresponding to the peak load intensity. Where the peak is not well defined, q_{up} is obtained by double tangent method as shown in previous figure.

The load settlement curve obtained from a plate load test can be used to determine ultimate and safe bearing capacities of the foundation. Where the failure is easily identifiable by its distinct peak that is normally in the case of general shear failure, the ultimate capacity of the plate can be determined corresponding to the peak load intensity where the peak is not well defined q_{up}. That is the ultimate capacity of the plate is obtained by double tangent method as shown in the previous figure.

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So, here if you see this figure, that this 1 tangent is drawn from the initial portion and another tangent is drawn from this portion. This straight line portion of the curve and where ever it intersect these 2 curve these 2 lines the 2 tangents intersect that corresponds to the ultimate bearing capacity of the plate.

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In case of granular soils, the bearing capacity increases with the size of footing. The angle of shearing resistance of the soil can be worked back with the help of ultimate bearing capacity of the plate, q_{ap} .

For square plate, N_γ may be determined from following equation

$$q_{ap} = 0.4 \gamma B_p N_\gamma$$

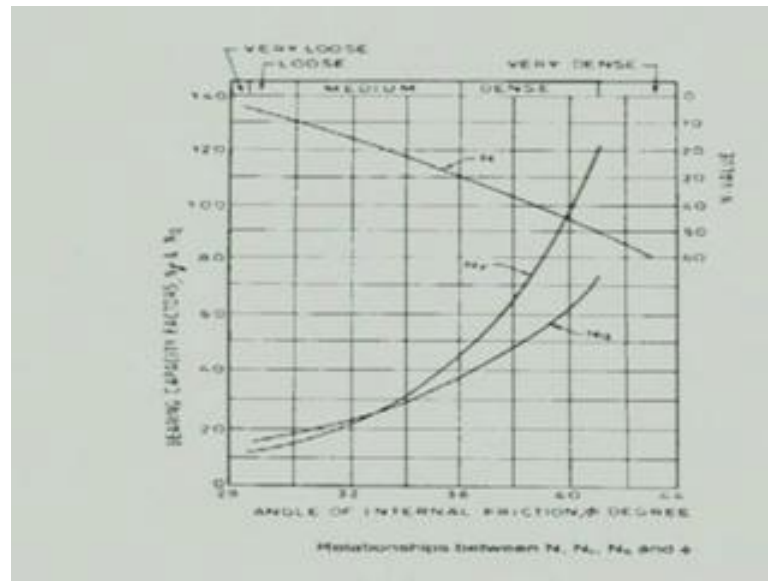
(since there is no surcharge on the test plate)

Once N_γ is known, Φ and N_q may be obtained by Peck et al. (1974) graph. The bearing capacity of actual foundation may be obtained by Terzaghi's equation.

In case of granular soils, the bearing capacity increases with the size of the footing. The angle of shearing resistance of the soil can be worked back with the help of ultimate bearing capacity of the plate. As we know that the ultimate bearing capacity of the square foundation is given by c and $c + q_0$ and $q + 0.5 \cdot 0.4 \gamma B$ and γ . Now, in this case for in the case of plate load test we had already removed the overburden.

So, q_0 and $q + 0.5 \cdot 0.4 \gamma B$ it vanishes and it is the case of c equal to 0. So, c and $c + q_0$ also vanishes and we are left with ultimate bearing capacity of the plate as $0.4 \gamma B N_\gamma$. Now here this is the width of the footing here B_p is the width of the plate. So, since there is no surcharge on the test plate this equation can be used. Once N_γ is known ϕ and N_q may be obtained by Peck et al graphs which we have seen earlier. The bearing capacity of actual foundation may be obtained by Terzaghi equation.

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Now, this the graph for your reference projected again. In case of cohesive soils the bearing capacity does not vary with the size of the footing.

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In case of cohesive soils, the bearing capacity does not vary with the size of footing. Therefore ultimate bearing capacity of the foundation, q_{uf} is taken as ultimate bearing capacity of the plate, q_{up} .

Therefore ultimate bearing capacity of the foundation that is Q_{uf} is taken as ultimate bearing capacity of the test plate itself.

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Results of plate load test need to be interpreted with caution. Some of the important considerations are given as follows:

- In no case shall a test plate smaller in width than 30 cm be used, because experimental evidence has indicated that the load- settlement behaviour of the soil is qualitatively different for smaller widths of the test plates compared to that of larger widths.

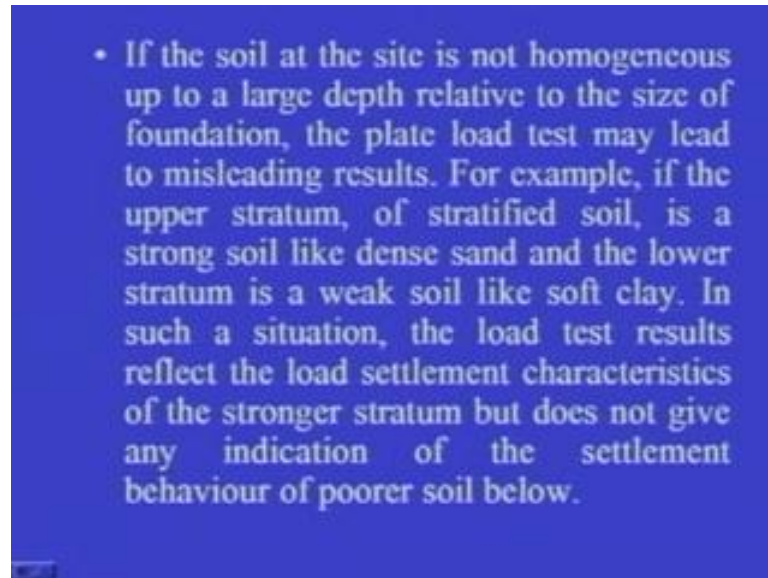
Results of plate load test need to be interpreted with caution. Some of the important considerations are given as follows: In no case shall a test plate smaller in width than 30 centimeter be used. Because experimental evidence has indicated that the load settlement behaviour of the soil is qualitatively different for smaller widths of the test plate compared to that of larger widths.

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It has been found that in the case of granular soils, the settlement of a foundation can not exceed about four times the settlement of a plate of 30 cm width, howsoever large it may be.

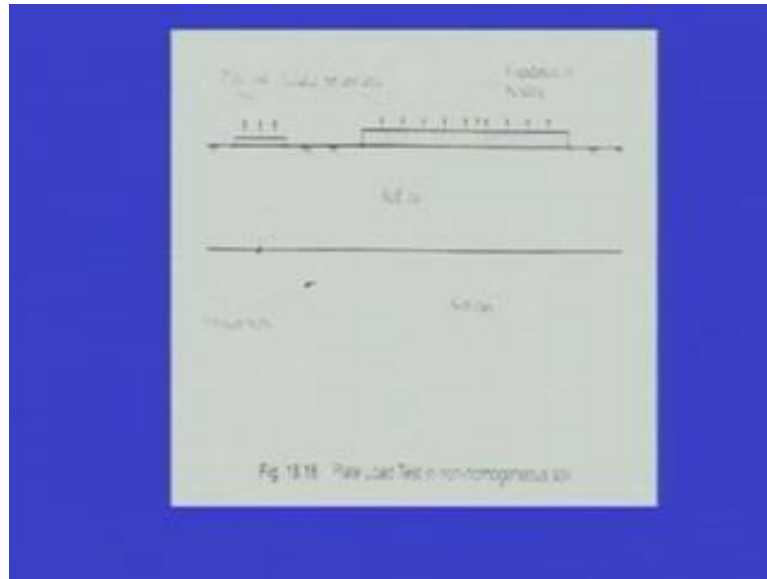
It has been found that in the case of granular soils, the settlement of a foundation cannot exceed about 4 times the settlement of a plate of 30 centimeter width, howsoever large it may be.

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If the soil at the site is not homogeneous up to a large depth relative to the size of the foundation, the plate load test may lead to misleading results. For example, if the upper stratum of stratified soil is a strong soil like dense sand and the lower stratum is a weak soil like soft clay in such a situation. The load test results reflect the load settlement characteristics of the stronger stratum, but does not give any indication of the settlement behaviour of the poorer soil below.

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Now, this figure shows that if you have 2 test plates. This is of the smaller size and this is the larger size. Then the special bulb for this smaller size and if suppose these 2 are resting on to soils one is soft soil or stiff soil at the top and the soft soil at the bottom. Then the special bulb extends on the in this upper stratum and we will be getting load settlement behaviour of the upper stratum only whereas, the size of the foundation is far larger than the size of the test plate. Now, in that case the special bulb for the same intensity it also goes beyond the boundary of this upper stratum. So, it also penetrates in the lower stratum now, in the case of this the load characteristics of this particular stratum are not accounted for heavy conduct test on the smaller size plate. So, we will have to be very cautious.

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- The foundation being of a much larger width, its bulb of pressure of the same load intensity as that of the test plate will extend into weaker stratum. Hence the extrapolated settlement of the foundation will be much smaller than the actual settlement, leading to unsafe design. A plate load test has, therefore, to be supplemented by adequate soil exploration through a borehole, which will reveal any non-homogeneity of the strata, up to a depth of about 1.5 to 2.0 times of the structure.

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- The effect of capillarity in a sand bed is to increase its effective vertical stress or its stiffness. A test plate resting on a capillary sand bed undergoes smaller settlement than a plate on dry or submerged sand bed. When the results of a load test where the plate is resting on a capillary sand bed are used to estimate the settlement of a foundation resting at the same elevation but with the natural water table rising up to the level of foundation, it will result in severe underestimate of the settlement. Practically a plate load test should be performed at the water table level if it is within 1 m below the foundation.

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- A plate load test is of short duration. The settlement measured is only the immediate settlement. In granular soils, immediate settlement can be taken as total settlement, while in cohesive soils, consolidation settlement, which constitutes most part of total settlement, can not be predicted through this test. Hence the plate load test is not of much relevance in clayey soils for which the settlement criterion is very important in the determination of the allowable bearing pressure of a foundation.

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**Ultimate Bearing Capacity of
Footings Based on Static Cone
Penetration Resistance CPT (q_c)
Values**

So, to very cautious when we interpret the plate load test data. Now, another test which is preferred is the static cone penetration test by which we find out CPT values termed as q_c values and ultimate bearing capacity of footing can be determined from these q_c values.

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Bearing Capacity of Granular Soil

As per Schmertmann(1978), the bearing capacity factor N_γ for use in the Terzaghi's Bearing capacity equation can be determined as follows,

$$N_\gamma = 1.25q_c$$

where q_c = cone point resistance in kg/cm^2 ,
averaged over a depth equal to 1.5 to
2.0 times width below foundation.

With the known value of N_γ , Φ and bearing capacity factor N_q and hence Ultimate Bearing Capacity can be determined.

For the granular soil, as per Schmertmann the bearing capacity factor N_γ for use in the Terzaghi's bearing capacity equation can be determined as follows. N_γ can be taken as 1.25 times q_c where q_c is the cone point resistance in kg per centimeter

square average over a depth equal to 1.5 to 2 times width below the foundation. With the known values of $N \gamma \phi$ and bearing capacity factor n_q and hence ultimate bearing capacity can be determined.

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Bearing Capacity of Granular Soil
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where q_c = cone point resistance in kg/cm^2 , averaged over a depth equal to 1.5 to 2.0 times width below foundation.
With the known value of N_γ , Φ and bearing capacity factor N_q and hence Ultimate Bearing Capacity can be determined.

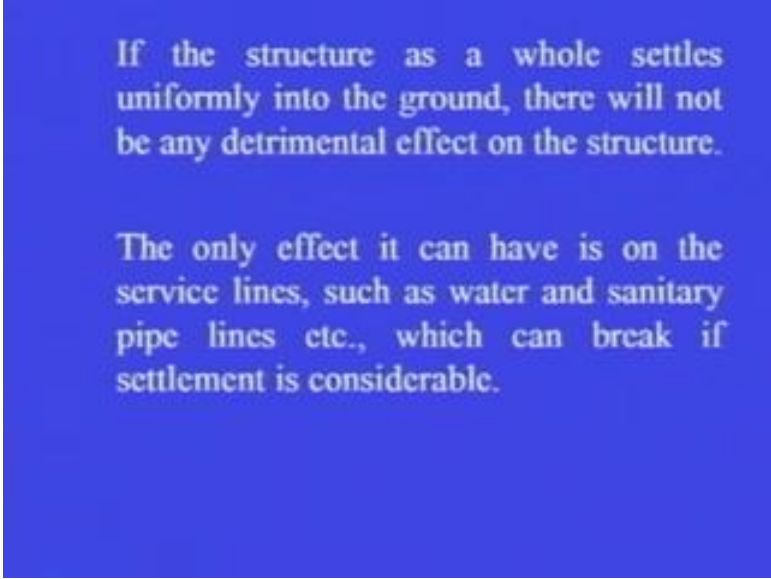
In the case of clay soils, the undrained shear strength c_u under ϕ equal to 0 condition may be related to the static cone point resistance q_c as q_c equal to $N_k c_u$ plus p_0 . Where N_k is the cone factor which is approximately 20 for both normally and over consolidated clays and p_0 is equal to the total overburden pressure represented as σ_0 also.

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SETTLEMENT OF SHALLOW FOUNDATIONS

So, ultimate bearing capacity of foundations can also be determined from the field test. And in order to design the foundation, we also need to know the settlement of shallow foundation. Because the design criteria say that the bearing capacity of the foundations should be sufficient. So, that there is no shear failure of the soil and the settlement should be within permissible limits. So, I am going to discuss now, to determine settlement of shallow foundations. Now, first of all let us see what are the effects of settlement on the structure.

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If the structure as a whole settles uniformly into the ground, there will not be any detrimental effect on the structure.

The only effect it can have is on the service lines, such as water and sanitary pipe lines etc., which can break if settlement is considerable.

If the structure has as a whole settles uniformly into the ground there will not be any detrimental effect on the structure. The only effect it can have is on the service lines such as water and sanitary pipe lines which can break if settlement is considerable.

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Several structures in Mexico city have undergone enormous settlements, as large as 2m, but are still functional because the settlement has been uniform.

Such uniform settlement is possible only if the subsoil is homogenous and the load distribution is uniform.

Several structures in Mexico City have undergone enormous settlements of the order of as large as 2 meter, but are still functional, because the settlement has been uniform. Such uniform settlement is possible only if the subsoil is homogeneous and the load distribution is uniform.

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However, the differential settlement should not exceed the permissible limits.

A structure is said to undergo differential settlement if one of its part settles more than the other.

Angular distortion is the ratio of the differential settlement between two columns to the spacing between them.

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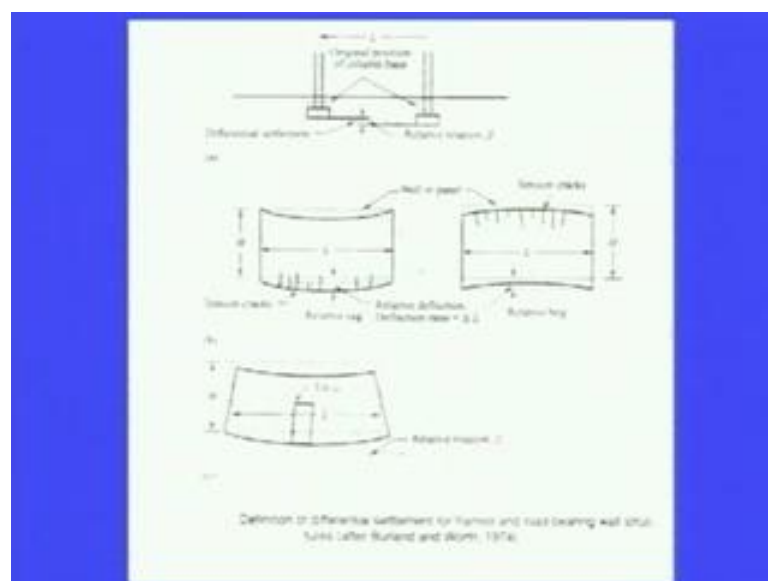
Angular distortion is the ratio of the differential settlement between 2 columns to the spacing between them.

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Tilt occurs when the entire structure rotates as a consequence of non-uniform settlement.
A classic example of tilt is the leaning tower of Pisa.
Definition of differential settlement for framed and load-bearing wall structures (after Burland and Worth, 1974) are shown in the next figure.

Tilt occurs when the entire structure rotates as a consequence of a non-uniform settlement. A classical example of tilt is the leaning tower of Pisa. Definition of differential settlement for framed and load bearing wall structures are shown in the next figure which are given by Burland and Worth 1974.

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Now, you can see from here that there are 2 columns resting on these 2 footings. Now this column has settled less than this column. And hence, the differential settlement will be the settlement of this column minus the settlement of this column whereas; the rotation will be given by the difference in this settlement divided by the length between these columns. So, that is the relative rotation. Now, due to this, there may be shaking of this wall or may be something like this and there may be cracks which will appear on the wall panel. Similarly, there may be relative heaving like this then tension cracks will get developed here on the top portion. And there may be relative rotation of this particular structure also. So, these are the definitions of the differential settlement the rotation and the tilt.

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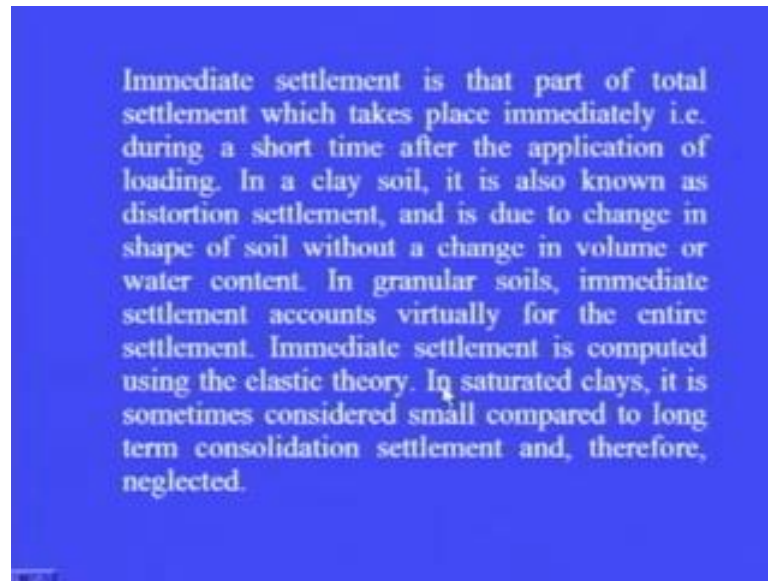
COMPONENTS OF TOTAL SETTLEMENT

- Immediate or Elastic Settlement, S_i
- Primary Consolidation settlement, S_c
- Secondary Consolidation settlement, S_s

$$S = S_i + S_c + S_s$$

The components of total settlement are immediate or elastic settlement we represent it by S_i primary consolidation settlement we represent it by S_c and secondary consolidation settlement which is something like creep behaviour we indicate it by S_s . So, the total settlement is equal to S_i plus S_c plus S_s . Now, in some of the soils you will find that we get only S_i in some of the soils we find that there is only S_c , but for most some of the soils which is rare most part of the settlement is the secondary consolidation settlement.

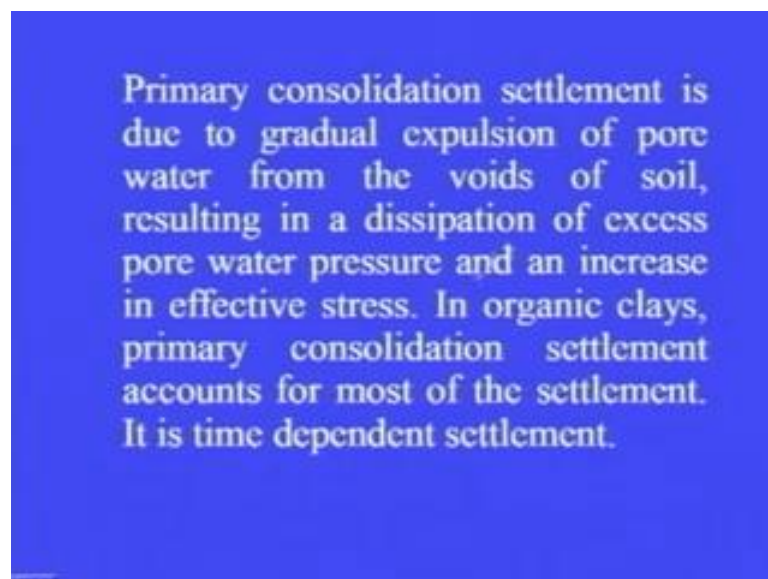
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Immediate settlement is that part of total settlement which takes place immediately i.e. during a short time after the application of loading. In a clay soil, it is also known as distortion settlement, and is due to change in shape of soil without a change in volume or water content. In granular soils, immediate settlement accounts virtually for the entire settlement. Immediate settlement is computed using the elastic theory. In saturated clays, it is sometimes considered small compared to long term consolidation settlement and, therefore, neglected.

Immediate settlement is that part of total settlement which takes place immediately that is during a short time after the application of loading. In a clay soil it is also known as distortion settlement and is due to change in shape of soil without a change in volume or water content. In granular soils immediate settlement accounts virtually for the entire settlement there is very less consolidation settlement. Immediate settlement is compared is computed using the elastic theory. In saturated clays it is sometimes considered small compared to long term consolidation settlement and therefore, neglected.

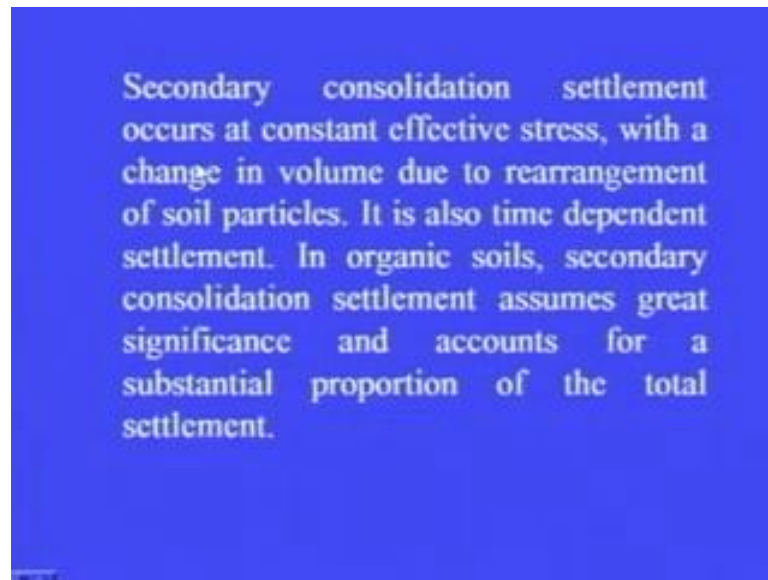
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Primary consolidation settlement is due to gradual expulsion of pore water from the voids of soil, resulting in a dissipation of excess pore water pressure and an increase in effective stress. In organic clays, primary consolidation settlement accounts for most of the settlement. It is time dependent settlement.

Primary consolidation settlement is due to gradual expulsion of pore water from the voids of soil resulting in a dissipation of excess pore water pressure. And an increase in effective stress in organic clays, primary consolidation settlement accounts for most of the settlement. It is of time dependent settlement.

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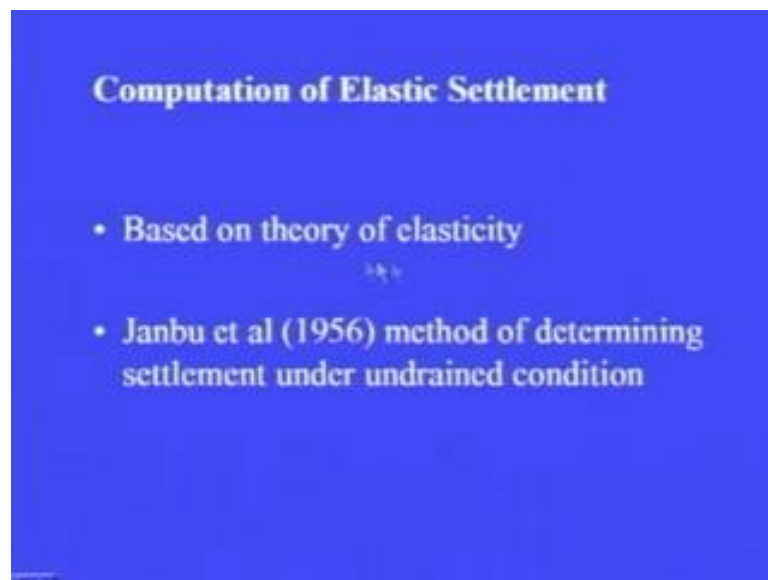
Secondary consolidation settlement occurs at a constant effective stress, with a change in volume due to rearrangement of soil particles. It is also time dependent settlement. In organic soils secondary consolidation settlement assumes great significance and accounts for a substantial proportion of the total settlement.

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Now, in order to determine this settlement various methods are available. So, we are going to discuss now, the methods for computing settlement.

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Computation of elastic settlement now, this elastic settlement can be determined based on the theory of elasticity or a procedure which is given by Janbu et al for determining settlement under undrained condition.

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The net elastic settlement, S_i for a flexible surface foundation based on theory of elasticity may be obtained as

$$S_i = q_n B \frac{(1 - \mu^2)}{E_s} I_f$$

The net elastic settlement S_i for a flexible surface foundation based on theory of elasticity may be obtained as S_i equal to $q_n B \frac{1 - \mu^2}{E_s}$ into factor.

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where

S_i = elastic settlement
 B = width of foundation
 E_s = modulus of elasticity of soil
 μ = Poisson's ratio
 q_n = net foundation pressure
 I_f = influence factor

The influence factor depends on the shape and rigidity of foundation. Values of I_f are given in next table for flexible and rigid foundations.

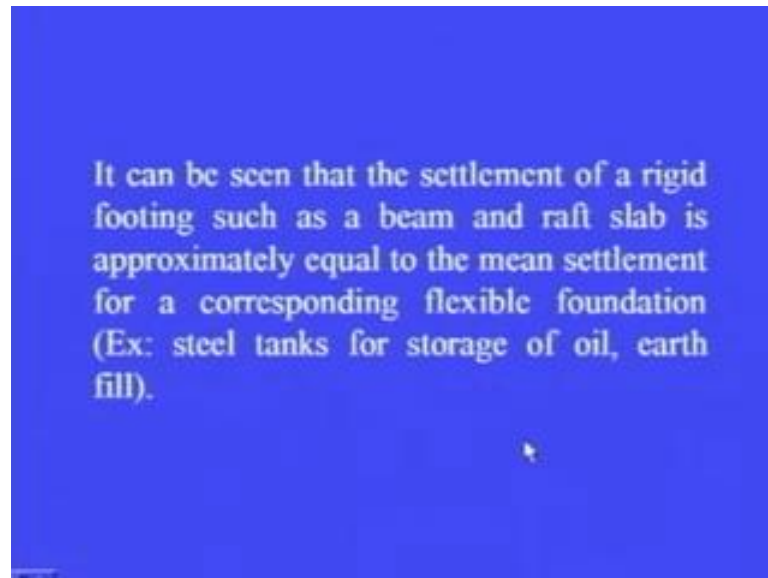
If where this S_i is the elastic settlement; B is the width of foundation; E_s is the modulus of elasticity of the soil; μ is the Poisson's ratio; q_n is the net foundation pressure. So, that is equal to the gross pressure minus γD_f ; I_f is the influence factor. The influence factor depends on the shape and rigidity of foundation values of I_f are given in the next table for flexible and rigid foundations.

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Influence Factor I_f (Bowles, 1988)				
Shape	I_f (Flexible foundation)			I_f (Rigid foundation)
	Centre	Corner	Average	
Circle	1.00	0.64	0.85	0.86
Square	1.12	0.56	0.95	0.82
Rectangle				
L/B = 1.5	1.36	0.68	1.20	1.06
2.0	1.52	0.76	1.31	1.20
5.0	2.10	1.05	1.83	1.70
10.0	2.52	1.26	2.25	2.10
100.0	3.38	1.69	2.96	3.40

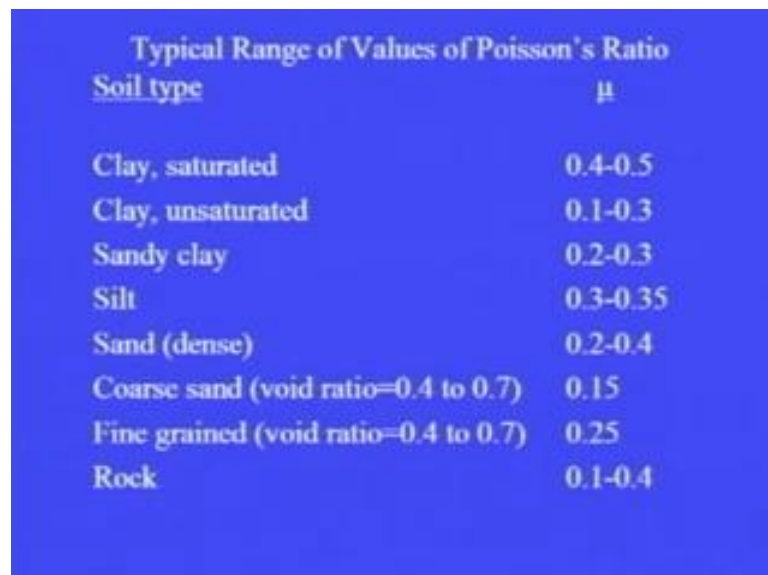
Now, these are the influence factor given by Bowles 1988, for different shapes for flexible foundations as well as for rigid foundation. Now, the I_f for flexible foundations at the centre of the footing at the corner and the average values are also presented in the table. Now, let us say for the case of a circle circular foundation at the centre it is 1 at the corner it is 0.64 and hence average we can take 0.85. If the foundation is flexible, but for the case of rigid foundation it is considered taken as 0.86. Similarly, for the square foundation these values are 1.12, 0.56, 0.95, 0.82 for rectangle foundations of different resource of L by B starting from 1.5 to 100 these values are given in this table. For example if L by B equal to 10 then at the centre if we are determining the settlement at the centre that I_f is taken as 2.52; at the corner it is 1.62, but as average we can considered as 2.25 if the foundation is flexible and 2.1 if the foundation is rigid similarly for other values of L by B.

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It can be seen that, the settlement of a rigid footing such as a beam and raft slab is approximately equal to the mean settlement for a corresponding flexible foundation. For example, steel tanks for storage of oil or earth fill are the examples of the flexible foundations.

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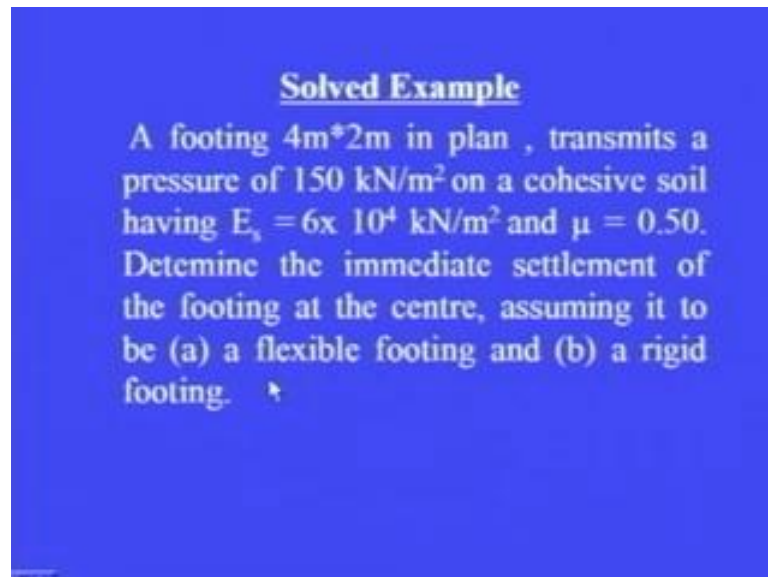


Soil type	μ
Clay, saturated	0.4-0.5
Clay, unsaturated	0.1-0.3
Sandy clay	0.2-0.3
Silt	0.3-0.35
Sand (dense)	0.2-0.4
Coarse sand (void ratio=0.4 to 0.7)	0.15
Fine grained (void ratio=0.4 to 0.7)	0.25
Rock	0.1-0.4

Typical range of values of Poisson's ratio or dependent on the type of soil and it varies from 0.1 to 0.5. Now, for the clay which is in saturated condition this value is taken as 0.4 to 0.5; 0.5 is the maximum for the undrained condition. For clay unsaturated it can be

taken between 0.1 and 0.3; for sandy clay 0.2 to 0.3; for silt 0.3 to 0.35; for dense sand point 0.2 to 0.4. For coarse sand with void ratio between 0.4 to 0.7 can be taken as 0.15; for fine grained sand void ratio between 0.4 to 0.7. It can be taken as 0.25 and in the case of rock it can be taken between 0.1 to 0.4, depending upon the quality of the rock.

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Solved Example

A footing 4m*2m in plan , transmits a pressure of 150 kN/m² on a cohesive soil having $E_s = 6 \times 10^4$ kN/m² and $\mu = 0.50$. Determine the immediate settlement of the footing at the centre, assuming it to be (a) a flexible footing and (b) a rigid footing. *

Now, we will consider 1 solved problem which will demonstrate to how to calculate the immediate settlement? A footing of 4 meter by 2 meter in plan transmits a pressure of 150 kilo Newton per meter square on a cohesive soil having modulus of elasticity of the soil E_s as 6 into 10 to the power of 4 kilo Newton per meter square. And μ equal to 0.5 determine the immediate settlement of the footing at the centre, assuming it to be a flexible footing and then or rigid footing.

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$$S_i = q_n B \frac{(1-\mu^2)}{E_s} I_f$$

For $L/B = 4/2 = 2$ from table $I_f = 1.52$ for a flexible footing and 1.20 for a rigid footing

(a) $S_i = 150 \times 2 \times \frac{(1-0.5^2)}{6 \times 10^4} 1.52 = 5.7 \text{ mm}$

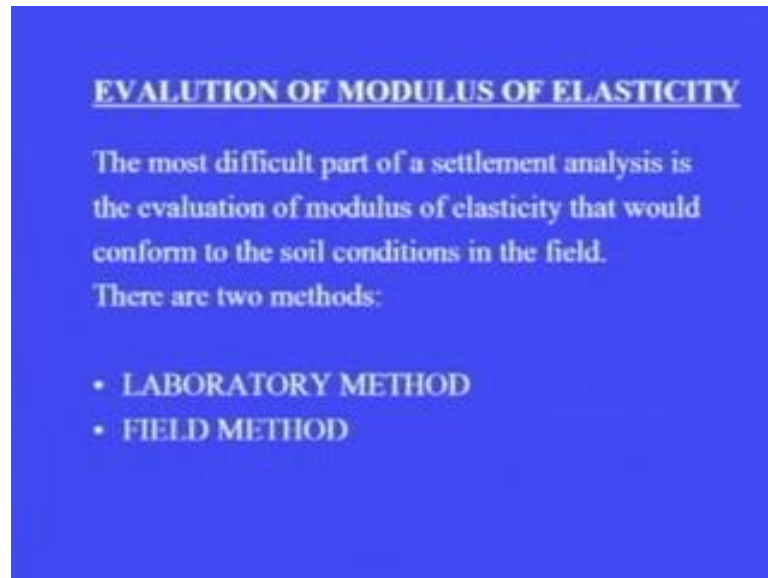
(b) $S_i = 4.5 \text{ mm}$

If we use the rigid factor of 0.8 as recommended by IS: 8009, Part 1(1976),

$$S_{i(\text{rigid footing})} = 0.8 \times 5.7 = 4.56 \text{ mm}$$

So, we know that this S_i is given by $q_n B \frac{1 - \mu^2}{E_s} I_f$. Now here q_n is given b is given μ is also given E is given only thing is we will have to select a value of I_f . So, for L by B ratio of 2 from table which I have shown it earlier we can find out that this I_f is 1.52 for a flexible footing and 1.2 for a rigid footing. So, when we substitute this value of I_f here we can find out immediate settlement for the flexible as well as for the rigid footing. So, it comes out to be 5.7 millimeter for the flexible footing and 4.5 millimeter for the rigid footing. If you use the rigidity factor of 0.8 as recommended by IS 8009 part 1 1976 then the S of the immediate settlement of the footing, if we multiply with the flexible 0.8 into 5.7 it comes out to be 4.56. So, these 2 values you can see are comparable.

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EVALUATION OF MODULUS OF ELASTICITY

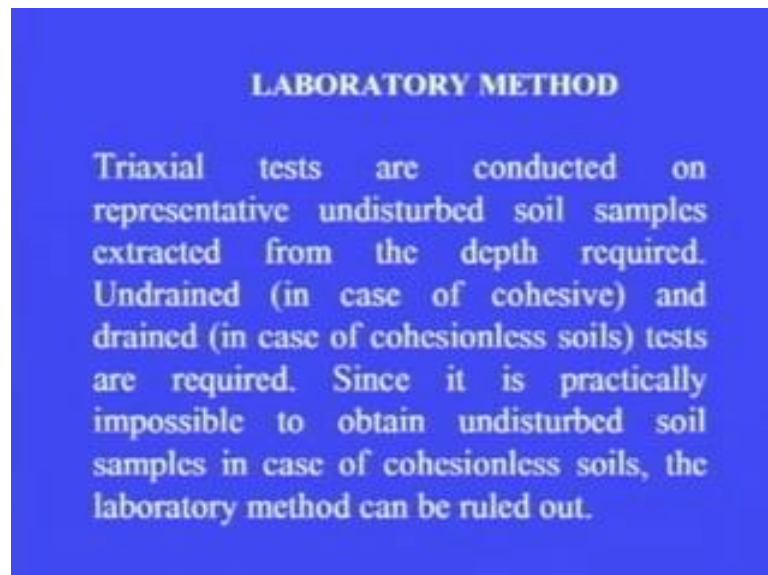
The most difficult part of a settlement analysis is the evaluation of modulus of elasticity that would conform to the soil conditions in the field.

There are two methods:

- LABORATORY METHOD
- FIELD METHOD

Evaluation of modulus of elasticity, the most difficult part of a settlement analysis is the evaluation of modulus of elasticity that would conform to the soil conditions in the field.

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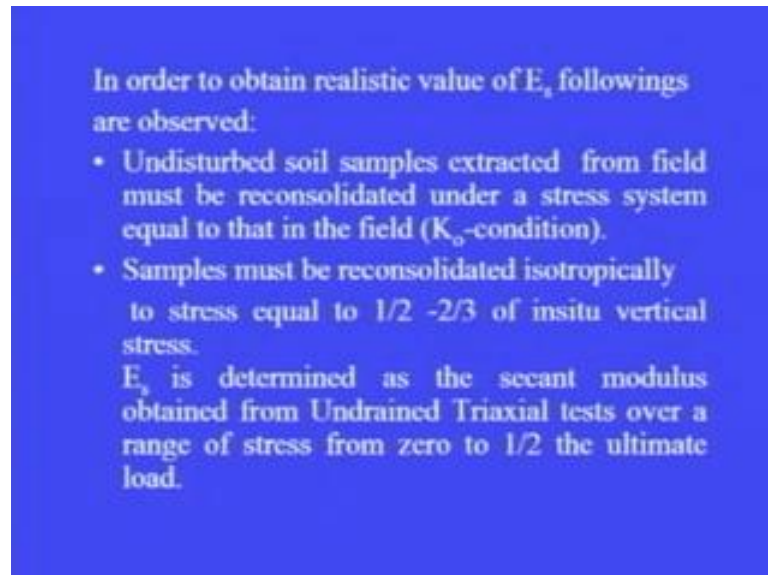
LABORATORY METHOD

Triaxial tests are conducted on representative undisturbed soil samples extracted from the depth required. Undrained (in case of cohesive) and drained (in case of cohesionless soils) tests are required. Since it is practically impossible to obtain undisturbed soil samples in case of cohesionless soils, the laboratory method can be ruled out.

There are 2 methods of a level one by laboratory and another by field and a data laboratory method, Triaxial tests are conducted on representative undisturbed soil samples extracted from the depth required. Undrained; in case of cohesive and drained in case of cohesion less soils tests are conducted. Since it is practically impossible to obtain

undisturbed soil samples in case of cohesion less soils the laboratory method can be ruled out.

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In order to obtain realistic value of E_s followings are observed:

- Undisturbed soil samples extracted from field must be reconsolidated under a stress system equal to that in the field (K_0 -condition).
- Samples must be reconsolidated isotropically to stress equal to $1/2$ - $2/3$ of insitu vertical stress.

E_s is determined as the secant modulus obtained from Undrained Triaxial tests over a range of stress from zero to $1/2$ the ultimate load.

In order to obtain realistic value of E_s following are observed. Undisturbed soil samples extracted from field must be reconsolidated under a stress system equal to that in the field so, that we can simulate k naught condition. Samples must be reconsolidated isotropically to stress equal to half to two third of insitu vertical stress at that particular level from where the samples have been obtained. E_s is determined as the secant modulus obtained from undrained triaxial tests over a range of stress from 0 to half of the ultimate load.

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FIELD METHODS

- Plate Load Test (PLT)
- Standard Penetration Test (SPT)
- Static Cone Penetration Test (CPT)
- Pressure meter Test (PMT)
- Flat Dilatometer Test (DMT)

Many correlations between E_s and SPT or CPT are in use.

In the field method we have the methods available as plate load test, standard penetration test, static cone penetration test, pressure meter test and flat dilatometer test. Many correlations between E_s and SPT or CPT are in use.

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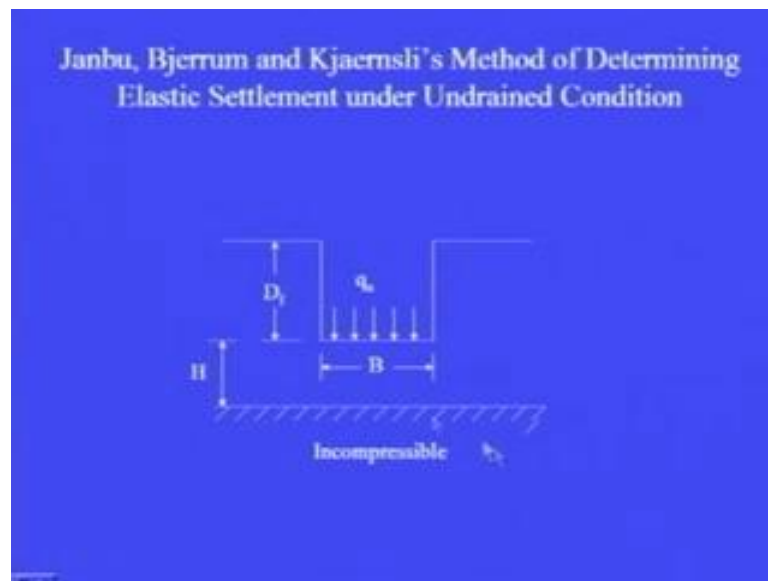
Equations for Computing E_s (kPa) by Making Use of SPT and CPT Values

Soil	SPT	CPT
Sand (Normally Consolidated)	$500*(N_{cor}+15)$ (35000 to 50000) $\log N_{cor}$	2 to 4 q_c $(1+Dr^2) q_c$
Sand (Saturated)	$250*(N_{cor}+15)$	
Sand (Over-consolidated)	-	2 to 4 q_c
Gravelly Sand And Gravel	$1200*(N_{cor}+6)$	-
Clayey Sand	$320*(N_{cor}+15)$	3 to 6 q_c
Silty Sand	$300*(N_{cor}+6)$	3 to 6 q_c
Soft Clay	-	3 to 6 q_c

These are the equations for computing E_s by making use of SPT and CPT values standard penetration test value and static cone penetration test value like for sand normally consolidated if SPT corrected N value is known. Then we can obtain this by five hundred into N corrected plus 15. Similarly, this can be taken as 35000 to 50000 log

of N corrected for the case of normally consolidated sand if CPT values are available. Then 2 to 4 times the q_c or CPT value in the case of saturated sand it can be taken as 250 multiply by N corrected plus 15 in the case of over consolidated sand it can be taken as 2 to 4 of q_c . If we have gravelly sand and gravels then we can use 1200 into N corrected plus 6 if we have got clayey sand. Then 320 into N corrected plus 15 or 3 to 6 times of q_c silty sand 300 into N corrected plus 6 or 3 to 6 times of q_c and if we have soft clay then 3 to 6 times of q_c .

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So, by this method we can determine E_s there is another method suggested by Janbu et al for determining elastic settlement under undrained condition. Now, this is it can shows a foundation which is a which is placed at a depth of D_f and the load applied to the soil is q_n and width V is the width of the footing. And H is the depth of the soil layer below the level of foundation the this strata below this is incompressible.

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Probably the most useful chart is that given by Janbu et al (1956) for the case of a constant E_s with respect to depth. The chart provides estimates of the average immediate settlement of uniformly loaded, flexible strip, rectangular, square or circular footings on homogeneous isotropic saturated clay. The equation for computing settlement is given by

Now, probably the most useful chart is that given by Janbu et al 1956 for the case of a constant E_s with respect to depth. The chart provides estimates of the average immediate settlement of uniformly loaded flexible strip rectangular square or a circular footings on homogeneous isotropic saturated clays the equation for computing settlement is given by S_i equal to $q_n B \mu_0 \mu_1$ upon E_s .

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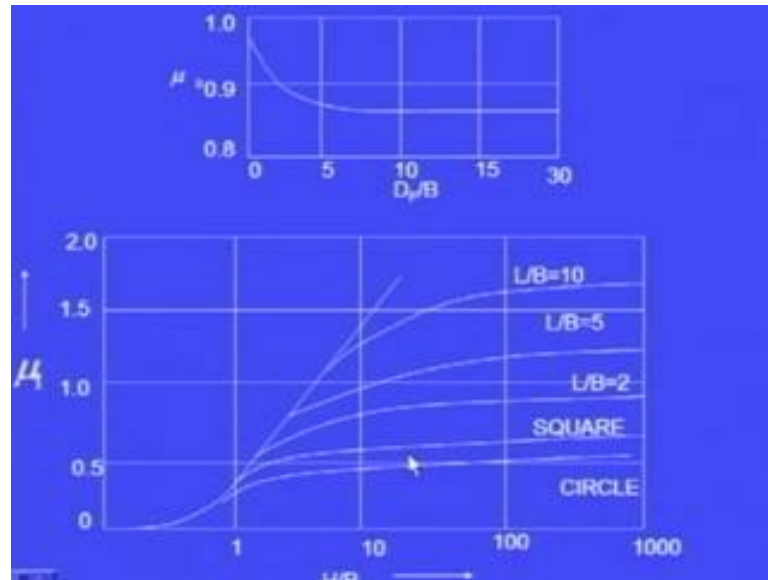
$$S_i = q_n B \frac{\mu_0}{E_s} \mu_1$$

In above equation, Poisson's ratio is assumed equal to 0.5. The factors μ_0 and μ_1 are related to the D_f/B and H/B ratios as shown in the next figure. The values of μ_1 are given for various L/B ratios. Rigidity and depth factors are required to be applied.

In the above equation Poisson's ratio is assumed equal to 0.5 because of the undrained condition. The factors μ_0 and μ_1 are related to the ratio D_f by B and H upon B

where H is the thickness of the soil layer below the foundation as shown in the next figure. The values of μ_1 are given for various values of L upon B ratios rigidity and depth factors are required to be applied.

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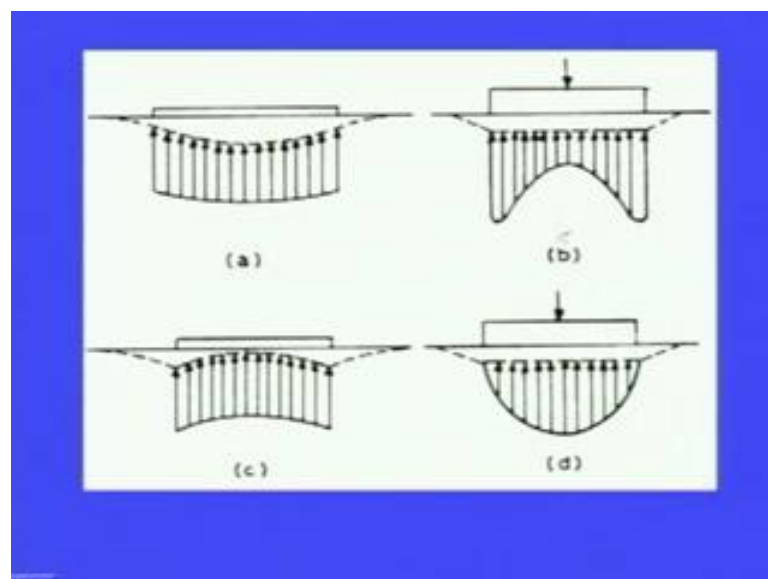
So, this is the figure this shows the relationship between μ_0 and D_f upon b this figure shows the relationship between μ_1 and H by B for different type of foundations like this is for the circular this is for the square these are for the rectangular when L by D ratio L by B is 2 L by B is 5 and L by B is 10. So, depending upon the H by B ratio and the type of foundation we can find out μ_1 from here and depending upon D_f by B ratio. And we can find out μ_0 here which can be used in the previous equation to determine immediate settlement.

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In flexible footing, the contact pressure, that is, the pressure at the interface between the footing and the soil, is uniformly distributed. A uniform pressure produces a dish shaped pattern of displacement as shown in Fig (a) in a clay soil. For a rigid footing, the settlement has to be more or less uniform over the area of contact. Since a uniform contact pressure produces a dish shaped settlement pattern in clay soil, the contact pressure must be more near the edges of the loaded area and less near the center (Fig b), in order to produce a uniform settlement.

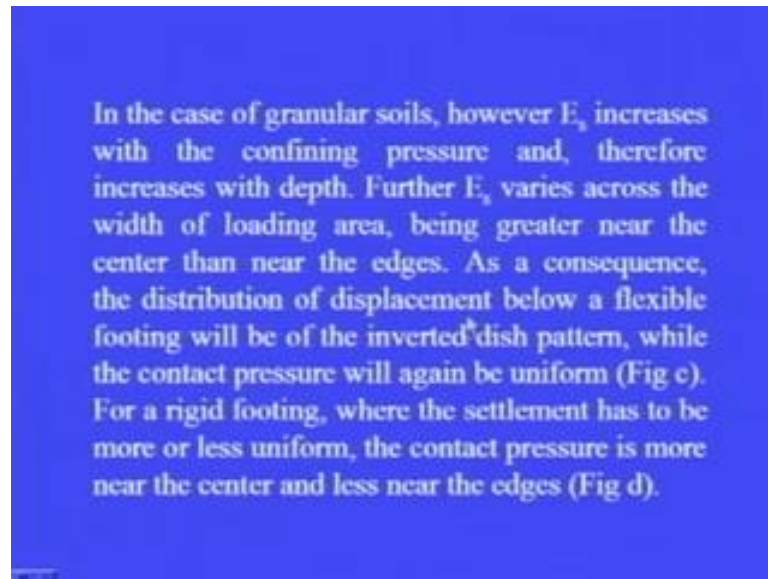
In flexible footing the contact pressure that is the pressure at the interface between the footing and the soil is uniformly distributed. And the soil is uniformly distributed a uniform pressure produces a dish shaped pattern of the displacement as shown in figure a which I am going to show it. Next in the clay soil for a rigid footing the settlement has to be more or less uniform over the area of contact. Since a uniform contact pressure produces a dish shaped settlement pattern in clay soil. The contact pressure must be more near the edges of the loaded area and less near the center in order to produce a uniform settlement.

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So, this is the case for the clays now, this is for the sand for the flexible and rigid footing.

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Now, in case of granular soil; however, E_s increases with the confining pressure. And therefore, increases with depth further E_s varies across the width of loading area being greater near the center than near the edges. As a consequence the distribution of displacement below a flexible footing will be of inverted dish pattern while the contact pressure will again be uniform as shown in figure c here. This is the figure then for a rigid footing where the settlement has to be more or less uniform the contact pressure is more near the center and less near the edges as shown in figure d.

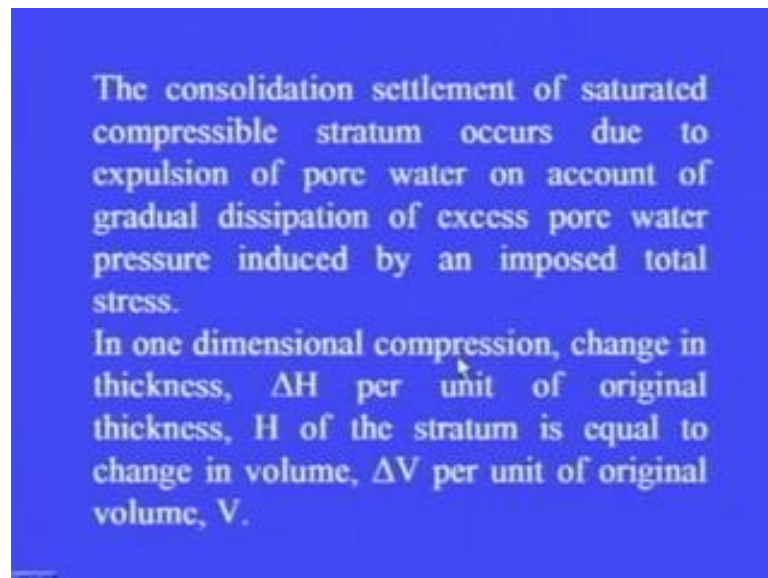
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**Estimation of Consolidation Settlement
by Using Consolidation/Oedometer Test
Data**

So, this is the figure for the rigid footing on granular soils Estimation of consolidation settlement by using consolidation or Oedometer test data.

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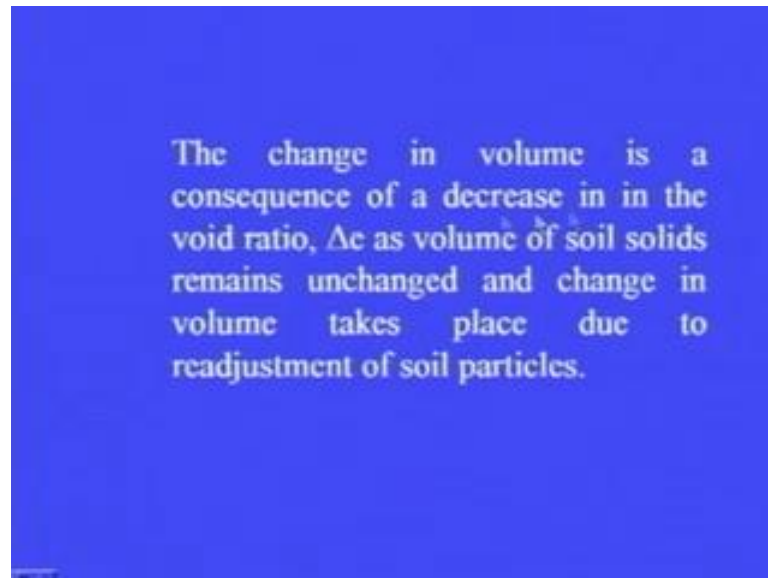


The consolidation settlement of saturated compressible stratum occurs due to expulsion of pore water on account of gradual dissipation of excess pore water pressure induced by an imposed total stress.

In one dimensional compression, change in thickness, ΔH per unit of original thickness, H of the stratum is equal to change in volume, ΔV per unit of original volume, V .

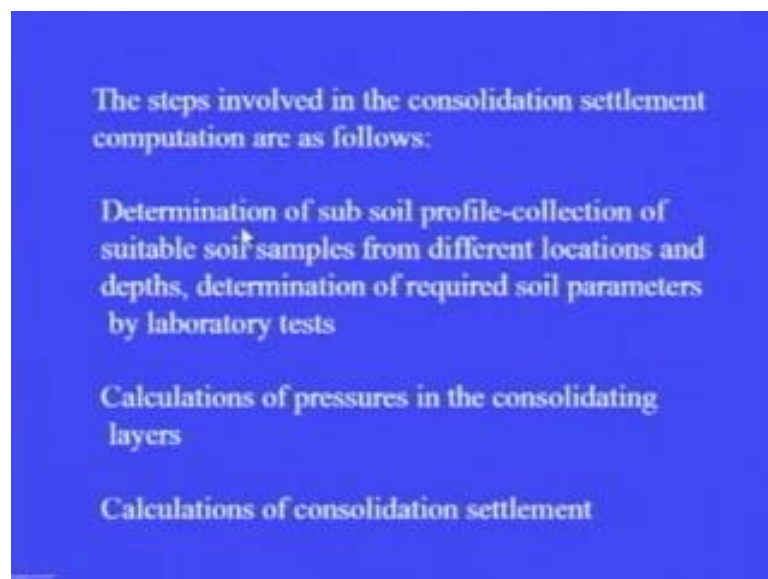
The consolidation settlement of saturated compressible stratum occurs due to expulsion of pore water on account of gradual dissipation of excess pore water pressure induced by an imposed total stress. In one dimensional compression the change in thickness Δh per unit of original thickness H of the stratum is equal to the change in volume ΔV per unit of the original volume V .

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The change in volume is a consequence of a decrease in the void ratio Δe as volume of the soil solids remains unchanged. And the change in volume takes place due to readjustment of the soil particles volume of solids will remain as it is.

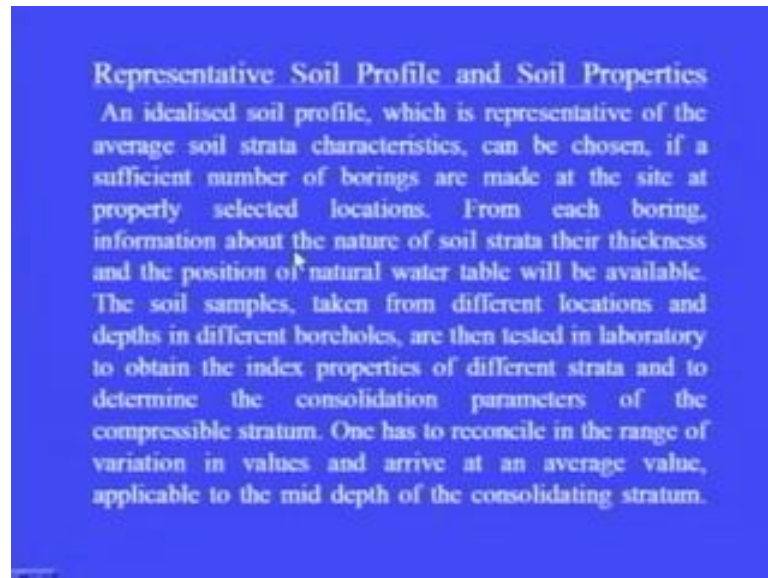
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So, using this concept we can determine the settlement the steps involved in the consolidation settlement computations are as follows. First of all we determine the subsoil profile. And in order to determine the subsoil profile collection of suitable soil samples from different locations and depths determination of required soil parameters by

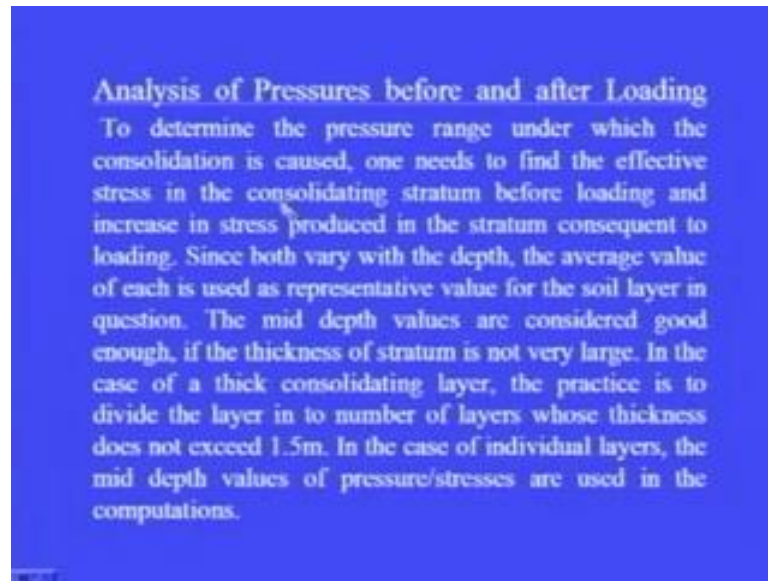
laboratory tests. Then calculation of pressures in the consolidating layers then the calculation of consolidation settlement.

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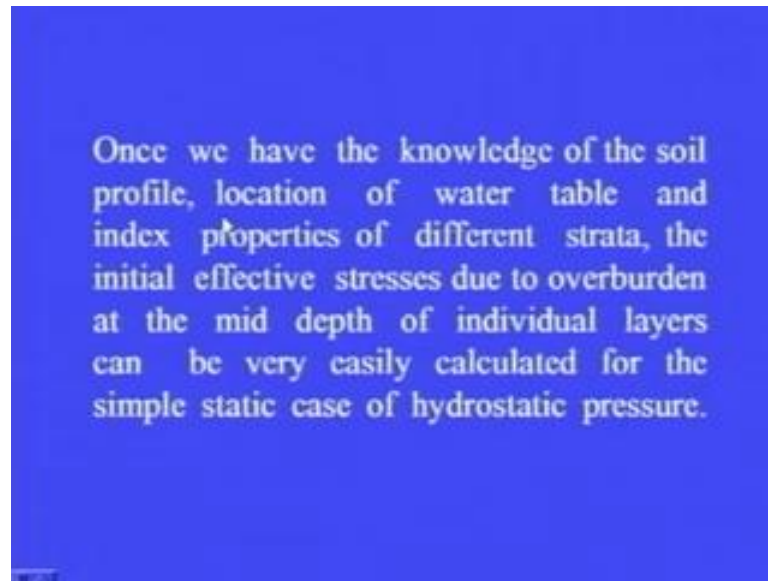
In order to determine this to find out this representative soil profile and soil properties what is done an idealized soil profile which is representative of the average soil strata ((refer time: 50:10)) characteristics can be chosen. If a sufficient number of borings are made at the site at properly selected locations from each boring information about the nature of soil strata their thickness and position of natural water table will be available. The soil samples taken from different locations and depths in different boreholes are then tested in laboratory to obtain the index properties of different strata and to determine consolidation parameters of the compressible stratum. One has to reconcile in the range of variation in values and arrive at an average value applicable to the mid depth of the consolidating stratum.

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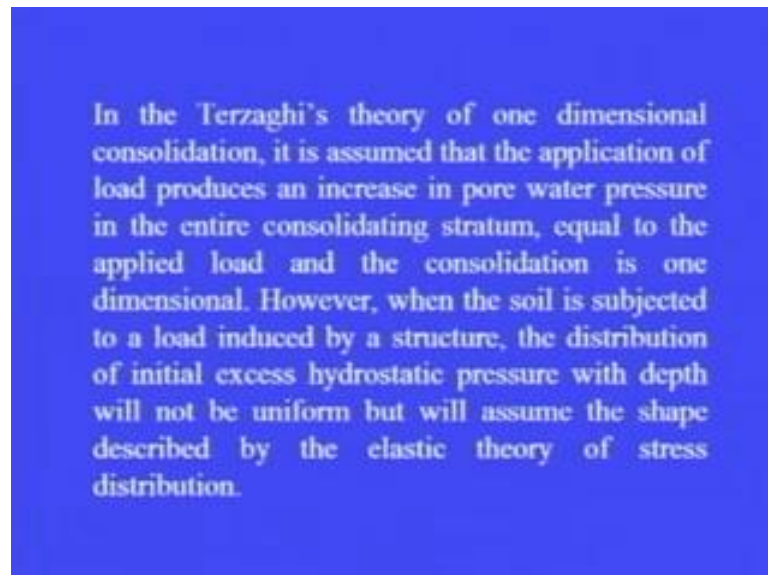
The second part is the analysis of pressure before and after loading. So, to determine the pressure range under which the consolidation is caused one needs to find the effective stress in the consolidating stratum before loading and increase in stress produced in the stratum consequent to loading. Since both vary with the depth the average value of each is used as a representative value for the soil layer in question. The mid depth values are considered good enough if the thickness of the stratum is not very large in the case of a thick consolidating layer. The practice is to divide the layer into number of layers whose thickness does not exceed 1.5 meter. In the case of individual layers the mid depth values of pressure or stress are used in the computations.

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Once we have the knowledge of the soil profile location of water table and the index properties of different strata. The initial effective stresses due to overburden at the mid depth of individual layers can be very easily calculated for the simple static case of hydrostatic pressure.

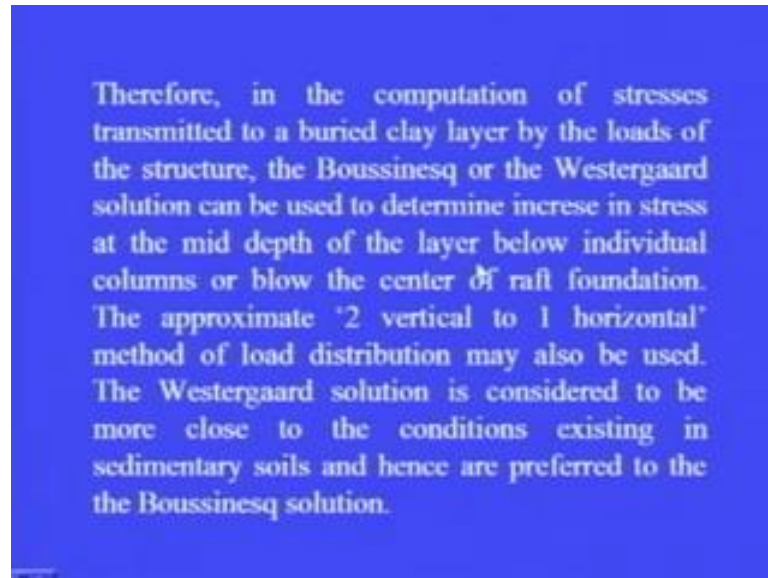
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In the Terzaghi's theory of 1 dimensional consolidation it is assumed that the application of load produces an increase in pore water pressure in the entire consolidating layer equal to the applied load and the consolidation is 1 dimensional. However, when the soil

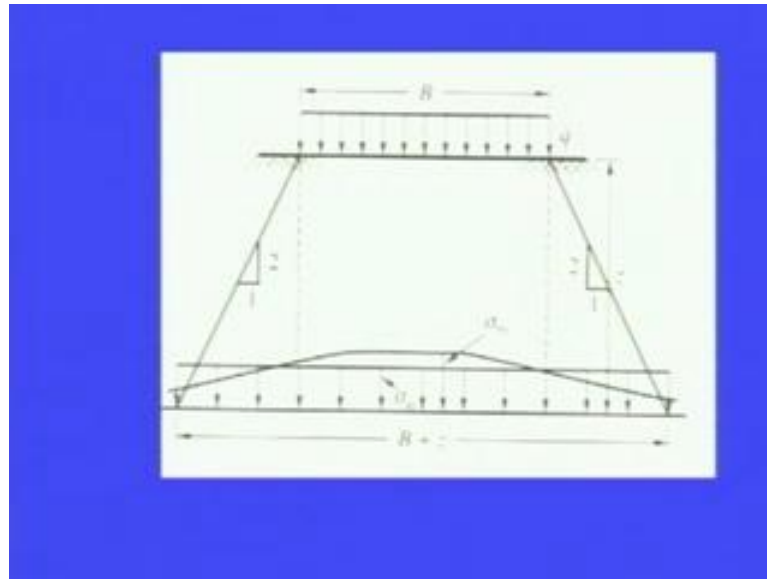
is subjected to a load induced by a structure the distribution of initial excess hydrostatic pressure with depth will not be uniform. But will assume the shape described by the elastic theory of stress distribution.

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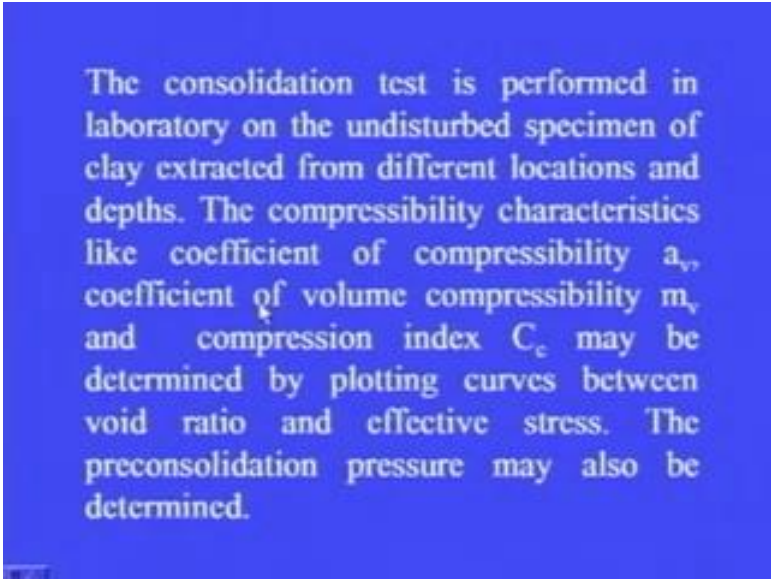
Therefore in the computation of stresses transmitted to a buried clay layer by the loads of the structure the Boussinesq or the Westergaard solution can be used to determine increase in stress at the mid depth of the layer below individual columns. Or below the center of raft foundation the approximate 2 vertical to 1 horizontal method of load distribution may also be used. The Westergaard solutions is considered to be more close to the conditions existing in sedimentary soils, and hence are preferred to the Boussinesq solution.

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As can be seen from this figure that there is a loaded area of width b and which is transmitting or load intensity of q to the soil here. Now, in order to find out the load increment due to this q at a depth equal to z below the ground surface we can use 2 vertical is to 1 horizontal distribution. And we can find out this average increase in stress by this 2 vertical and 1 horizontal distribution. So, the load this q is now, transferred from this load intensity q is transferred from here at width B to the width B plus z . So, in order to find out $\Delta \sigma$ or σ at this particular level, but we can do we can find it out like B into q into unity for the stiff footing divided by B plus z total divide by 1. That is the load increment or stress increment at this particular level. Actual load increment by Westergaard or Boussinesq method may of this type, but average value can we can obtain from 2 is to 1.

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The consolidation test is performed in laboratory on the undisturbed specimen of clay extracted from different locations and depths. The compressibility characteristics like coefficient of compressibility a_v , coefficient of volume compressibility m_v and compression index C_c may be determined by plotting curves between void ratio and effective stress. The preconsolidation pressure may also be determined.

The consolidation test is performed in laboratory on the undisturbed specimen of clay extracted from different locations and depths. The compressibility characteristics like coefficient of compressibility a_v coefficient of volume compressibility M_v . And compression index C_c may be determined by plotting curves between void ratio and effective stress the pre consolidation pressure may also be determined. So, in this lecture I have covered different field test by which we can determined ultimate bearing capacity of soils. Then different aspects of settlement like immediate, elastic settlement or consolidation settlement then the methods by which we can determine elastic settlement. And I have started with the determination of consolidation settlement which I will continue in the next lecture.

Thank you very much.