Module 4
Fasteners
Version 2 ME, IIT Kharagpur
Lesson 4
Design of bolted joints
Instructional Objectives

At the end of this lesson, the students should have the knowledge of

- Different types of stresses developed in screw fasteners due to initial tightening and external load.
- Combined effect of initial tightening and external load on a bolted joint.
- Leak proof joints and condition for joint separation.

4.4.1 Stresses in screw fastenings

It is necessary to determine the stresses in screw fastening due to both static and dynamic loading in order to determine their dimensions. In order to design for static loading both initial tightening and external loadings need be known.

4.4.1.1 Initial tightening load

When a nut is tightened over a screw following stresses are induced:

(a) Tensile stresses due to stretching of the bolt
(b) Torsional shear stress due to frictional resistance at the threads.
(c) Shear stress across threads
(d) Compressive or crushing stress on the threads
(e) Bending stress if the surfaces under the bolt head or nut are not perfectly normal to the bolt axis.

(a) Tensile stress

Since none of the above mentioned stresses can be accurately determined bolts are usually designed on the basis of direct tensile stress with a large factor of safety. The initial tension in the bolt may be estimated by an empirical relation $P_1 = 284 d$ kN, where the nominal bolt diameter $d$ is given in mm. The relation is used for making the joint leak proof. If leak proofing is not required half of the above estimated load may be used. However, since initial stress is inversely proportional to square of the diameter $\sigma = \frac{284d}{\pi \frac{d^2}{4}}$, bolts of smaller diameter such
as M16 or M8 may fail during initial tightening. In such cases torque wrenches must be used to apply known load.

The torque in wrenches is given by $T = \frac{C}{P_1} \cdot d$ where, $C$ is a constant depending on coefficient of friction at the mating surfaces, $P_1$ is tightening up load and $d$ is the bolt diameter.

(b) Torsional shear stress

This is given by $\tau = \frac{16T}{\pi d_c^3}$ where $T$ is the torque and $d_c$ the core diameter. We may relate torque $T$ to the tightening load $P_1$ in a power screw configuration (figure-4.4.1.1.1) and taking collar friction into account we may write

$$T = P_1 \left( \frac{d_m}{2} \left( \frac{1 + \mu \pi d_m \sec \alpha}{\pi d_m - \mu \pi \sec \alpha} \right) + \frac{\mu_c d_{cm}}{2} \right)$$

where $d_m$ and $d_{cm}$ are the mean thread diameter and mean collar diameter respectively, $\mu$ and $\mu_c$ are the coefficients of thread and collar friction respectively and $\alpha$ is the semi thread angle. If we consider that

$$d_{cm} = \frac{(d_m + 1.5d_m)}{2}$$

then we may write $T = C \cdot P_1 \cdot d_m$ where $C$ is a constant for a given arrangement.

As discussed earlier similar equations are used to find the torque in a wrench.
(c) Shear stress across the threads

This is given by \( \tau = \frac{3P}{\pi d_c b n} \) where \( d_c \) is the core diameter and \( b \) is the base width of the thread and \( n \) is the number of threads sharing the load.

(d) Crushing stress on threads

This is given by \( \sigma_c = \frac{P}{\frac{\pi}{4}(d_o^2 - d_c^2)n} \) where \( d_o \) and \( d_c \) are the outside and core diameters as shown in figure- 4.4.1.1.

(e) Bending stress

If the underside of the bolt and the bolted part are not parallel as shown in figure- 4.4.1.2, the bolt may be subjected to bending and the bending stress may be given by

\[ \sigma_B = \frac{x E}{2L} \]

where \( x \) is the difference in height between the extreme corners of the nut or bolt head, \( L \) is length of the bolt head shank and \( E \) is the young’s modulus.

4.4.1.2F- Development of bending stress in a bolt

4.4.1.2 Stresses due to an external load

If we consider an eye hook bolt as shown in figure- 4.4.1.2.1 where the complete machinery weight is supported by threaded portion of the bolt, then the bolt is...
subjected to an axial load and the weakest section will be at the root of the thread. On this basis we may write

\[ P_2 = \frac{\pi}{4} d_e^2 \sigma_t \]

where for fine threads \( d_e = 0.88d \) and for coarse threads \( d_e = 0.84d \), \( d \) being the nominal diameter.

\[ T = \frac{n \pi}{4} d_e^2 \tau \frac{PCD}{2} \]

where \( n \) is the number of bolts sharing the load, \( \tau \) is the shear yield stress of the bolt material. If the bolt is subjected to both tensile and shear loads, the shank should be designed for shear and the threaded portion for tension. A diameter slightly larger than that required for both the cases should be used and it should be checked for failure using a suitable failure theory.

**4.4.1.2.1F - An eye hook bolt**

Bolts are occasionally subjected to shear loads also, for example bolts in a flange coupling as shown in figure- 4.4.1.2.2. It should be remembered in design that shear stress on the bolts must be avoided as much as possible. However if this cannot be avoided the shear plane should be on the shank of the bolt and not the threaded portion. Bolt diameter in such cases may be found from the relation

\[ T = \frac{n \pi}{4} d_e^2 \tau \frac{PCD}{2} \]
4.4.1.3 Combined effect of initial tightening load and external load

When a bolt is subjected to both initial tightening and external loads i.e. when a preloaded bolt is in tension or compression the resultant load on the bolt will depend on the relative elastic yielding of the bolt and the connected members. This situation may occur in steam engine cylinder cover joint for example. In this case the bolts are initially tightened and then the steam pressure applies a tensile load on the bolts. This is shown in figure-4.4.1.3.1 (a) and 4.4.1.3.1 (b).
Initially due to preloading the bolt is elongated and the connected members are compressed. When the external load $P$ is applied, the bolt deformation increases and the compression of the connected members decreases. Here $P_1$ and $P_2$ in figure 4.4.1.3.1 (a) are the tensile loads on the bolt due to initial tightening and external load respectively.

The increase in bolt deformation is given by $\delta_b = \frac{P_b}{K_b}$ and decrease in member compression is $\delta_c = \frac{P_c}{K_c}$ where, $P_b$ is the share of $P_2$ in bolt, $P_c$ is the share of $P_2$ in members, $K_b$ and $K_c$ are the stiffnesses of bolt and members. If the parts are not separated then $\delta_b = \delta_c$ and this gives

$$\frac{P_b}{K_b} = \frac{P_c}{K_c}$$

Therefore, the total applied load $P_2$ due to steam pressure is given by

$$P_2 = P_b + P_c$$

This gives $P_b = P_2 K$, where $K = \frac{K_b}{(K_b + K_c)}$. Therefore the resultant load on bolt is $P_1 + KP_2$. Sometimes connected members may be more yielding than the bolt and this may occur when a soft gasket is placed between the surfaces. Under these circumstances

$K_b \gg K_c$ or $\frac{K_c}{K_b} << 1$ and this gives $K \approx 1$. Therefore the total load $P = P_1 + P_2$

Normally $K$ has a value around 0.25 or 0.5 for a hard copper gasket with long through bolts. On the other hand if $K_c \gg K_b$, $K$ approaches zero and the total load $P$ equals the initial tightening load. This may occur when there is no soft gasket and metal to metal contact occurs. This is not desirable. Some typical values of the constant $K$ are given in table 4.4.1.3.1.
<table>
<thead>
<tr>
<th>Type of joint</th>
<th>K</th>
</tr>
</thead>
<tbody>
<tr>
<td>Metal to metal contact with through bolt</td>
<td>0-0.1</td>
</tr>
<tr>
<td>Hard copper gasket with long through bolt</td>
<td>0.25-0.5</td>
</tr>
<tr>
<td>Soft copper gasket with through bolts</td>
<td>0.50-0.75</td>
</tr>
<tr>
<td>Soft packing with through bolts</td>
<td>0.75-1.00</td>
</tr>
<tr>
<td>Soft packing with studs</td>
<td>1.00</td>
</tr>
</tbody>
</table>

### 4.4.1.3.1T

#### 4.4.2 Leak proof joint

The above analysis is true as long as some initial compression exists. If the external load is large enough the compression will be completely removed and the whole external load will be carried by the bolt and the members may bodily separate leading to leakage.

Therefore, the condition for leak proof joint is \[ \frac{P_1}{K_c} > \frac{P_b}{K_b} \]. Substituting \( P_b = P_2 K \) and \[ \frac{K_c}{K_b} = \frac{1-K}{K} \] the condition for a leak proof joint reduces to \( P_1 > P_2 (1-K) \). It is therefore necessary to maintain a minimum level of initial tightening to avoid leakage.

#### 4.4.3 Joint separation

Clearly if the resultant load on a bolt vanishes a joint would separate and the condition for joint separating may be written as \( P_1 + KP_2 = 0 \).

Therefore if \( P_1 > KP_2 \) and \( P_1 < A_b \sigma_{ytb} \), there will be no joint separation. Here \( A_b \) and \( \sigma_{ytb} \) are the bolt contact area and tensile yield stress of the bolt material respectively and condition ensures that there would be no yielding of the bolt due to initial tightening load.
The requirement for higher initial tension and higher gasket factor (K) for a better joint may be explained by the simple diagram as in figure- 4.4.3.1.

\[ \phi = \tan^{-1}(K) \]

\[ P = P_1 + KP_2 \]

Leakage starts here at \( P = P_2^* \)

More external load sustained before leakage for higher K

4.4.3.1F – Force diagram for joint separation

4.4.4 Problems with Answers

Q.1: 12 M20 x 2.5C bolts are used to hold the cylinder head of a reciprocating air compressor in position. The air pressure is 7 MPa and the cylinder bore diameter is 100 mm. A soft copper gasket with long bolts is used for sealing. If the tensile yield stress of the bolt material is 500 MPa find the suitability of the bolt for the purpose. Check if the joint is leak proof and also if any joint separation may occur.

A.1:

According to Indian Standard Thread designation M20 x 2.5C indicates a metric bolt of nominal diameter 20 mm and a course pitch of 2.5 mm. Some typical bolt dimensions are quoted in table-4.4.4.1 as recommended by I.S. 4218-1978 (Part VI) :
<table>
<thead>
<tr>
<th>Designation</th>
<th>Pitch (mm)</th>
<th>Minor Diameter (mm)</th>
<th>Stress area (mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Bolt</td>
<td>Nut</td>
</tr>
<tr>
<td>M2</td>
<td>0.40</td>
<td>1.509</td>
<td>1.567</td>
</tr>
<tr>
<td>M5</td>
<td>0.8</td>
<td>4.019</td>
<td>4.134</td>
</tr>
<tr>
<td>M10</td>
<td>1.25</td>
<td>8.466</td>
<td>8.647</td>
</tr>
<tr>
<td>M16</td>
<td>1.5</td>
<td>14.160</td>
<td>14.376</td>
</tr>
<tr>
<td>M20</td>
<td>1.5</td>
<td>18.160</td>
<td>18.376</td>
</tr>
<tr>
<td>M24</td>
<td>2</td>
<td>21.546</td>
<td>21.835</td>
</tr>
</tbody>
</table>

4.4.4.1T-

Based on this for M20 x 2.5C bolt the initial tightening load is given by $P_1 = 284 \times d$ which is 56.8 kN.

External load on each bolt $P_2 = \frac{\pi \times (0.1)^2 \times 7 \times 10^6}{12}$ i.e. 4.58 kN.

From section 4.4.1.3 the constant $K = 0.5$-0.75. Taking an average value of $K = 0.625$ the total resultant load $P$ is given by $P = 56.8 + 0.625 \times 4.58 = 59.66$ kN.

From the table above, the stress area for M20 x 2.5C bolt is 245 mm². The stress produced in the bolt $= \frac{59.66 \times 10^3}{245 \times 10^{-6}} = 243 \text{ MPa}$.

The stress is within the yield stress of the material and gives a factor of safety of $\frac{500}{243} \approx 2$.

Test for leak proof joint

Refer to section 4.4.2. The condition for leak proofing is $P_1 > P_2 (1-K)$. $P_2 (1-K) = 1.717$ kN which is much less than $P_1 = 56.8$ kN. Therefore the joint is leak proof.

Test for joint separation

Two conditions are $P_1 > K P_2$ and $P_1 < A \sigma_y$. $K P_2 = 2.86$ kN which is much less than $P_1 = 56.8$ kN and $A \sigma_y = 245 \times 10^{-6} = 122.5$ kN which is much higher than $P_1 = 56.8$ kN. Therefore the joint separation will not take place.
Q.2: In a steam engine the steam pressure is 2 MPa and the cylinder diameter is 250 mm. The contact surfaces of the head and cylinder are ground and no packing is required. Choose a suitable bolt so that the joint is leak proof. Assume number of bolts to be used is 12.

A.2:

Let the nominal diameter of the bolt to be chosen is \( d \) mm. The initial tightening load = 248d kg i.e. 2.48d kN.

The external load per bolt = \( \frac{\pi}{4} \times (0.25)^2 \times 2 \times 10^6 \div 12 = 8.18 \) kN. Now the condition for leak proofing is \( P_1 > P_2 (1-K) \). Here for ground surfaces \( K=0.1 \).

Therefore

\[ 2.48d = 8.18 \times 0.9 \]

This gives \( d = 2.97 \) mm. This is the minimum requirement and we take \( d = 10 \) mm. We also check for yielding \( \frac{(P_1 + K P_2)}{A_b} < \sigma_{ty} \).

Here, \( A_b \) from the table-4.4.1 is 58 mm\(^2\) and therefore

\[ \frac{(2.48 \times 10 + 0.1 \times 8.18) \times 10^3}{58} = 442 \text{ MPa} \]

which is well within the range. It therefore seems that from strength point of view a smaller diameter bolt will suffice. However, the choice of M10 x 1.5C would provide a good safety margin and rigidity.

4.4.5 Summary of this Lesson

In this lesson stresses developed in screw fastenings due to initial tightening load and external load have been discussed along with relevant examples. Following this combined effect of initial tightening and external load on bolts is discussed and the condition for the bolted parts not to separate is derived. Condition for leak proof joints and joint separation have also been discussed.
4.4.6 Reference for Module-4