COURSE OUTLINE:

The main purpose of this course is to provide important workhorses of commutative algebra assuming only basic course on commutative algebra. Special efforts are made to present the concepts at the center of the field in a coherent, tightly knit way, streamlined proofs and a focus on the core results. Virtually all concepts and results of commutative algebra have natural interpretations. It is the geometric viewpoint that brings out the true meaning of the theory.

ABOUT INSTRUCTOR:

Dilip P. Patil received B. Sc. and M. Sc. in Mathematics from the University of Pune in 1976 and 1978, respectively. From 1979 till 1992 he studied Mathematics at School of Mathematics, Tata Institute of Fundamental Research, Bombay and received Ph. D. through University of Bombay in 1989. Currently he is a Professor of Mathematics at the Departments of Mathematics, Indian Institute of Science, Bangalore and at present he is a Visiting Professor at the Department of Mathematics, IIT Bombay. He has been a Visiting Professor at Ruhr-Universität Bochum, Universität Leipzig, Germany and several universities in Europe and Canada. His research interests are mainly in Commutative Algebra and Algebraic Geometry.

COURSE PLAN:

Week 01: Noether’s Normalisation Lemma — Classical Version (Part -1)
Week 02: Noether’s Normalisation Lemma — Classical Version (Part -2)
Week 03: Dimension of Graded Rings and Modules
Week 04: Digression on Basic Concepts
Week 05: Dimension Theorem
Week 06: Krull’s Principal Ideal Theorem and its Generalisation
Week 07: Digression on the Language of Algebraic Geometry
Week 08: Regular Local Rings
Week 09: Homological Dimension of Modules and Global Dimension of Rings
Week 10: Homological Characterisation of Regular Local Rings
Week 11: Discrete Valuation Rings
Week 12: Dedekind Domains