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Courses » Quantum Information and Computing

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## Unit 6 - Week 5

### Course outline

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Week 5

- Quantum Fourier Transform
- Period Finding and QFT
- Implementing QFT
- Implementing QFT-3 qubits (and more)
- Shor's Factorization Algorithm
- Shor's Factorization Algorithm- Implementation
- Shor's Algorithm- Continued Fraction
- Quiz : Week 5 - Assignment 5
- Week 5 - Assignment 5 Solutions

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### Week 5 - Assignment 5

The due date for submitting this assignment has passed. **Due on 2017-08-30, 23:59 IST**. As per our records you have not submitted this assignment.

In the following questions, **ONLY ONE** answer is correct. Choose the most appropriate one. (1X9=9 Marks)

1) Consider a function over a set of two integers  $\{0, 1\}$ . Let  $f(0) = 1$  and  $f(1) = 2$ . If  $\tilde{f}_0$  and  $\tilde{f}_1$  are the corresponding discrete Fourier transforms, then **1 point**

$\tilde{f}_0 = \frac{1}{\sqrt{2}}$

$\tilde{f}_0 = -\frac{1}{\sqrt{2}}$

$\tilde{f}_0 = \frac{3}{\sqrt{2}}$

$\tilde{f}_0 = \frac{\sqrt{3}}{2}$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$\tilde{f}_0 = \frac{3}{\sqrt{2}}$

2) Quantum Fourier Transform of  $\frac{|0\rangle - |1\rangle}{\sqrt{2}}$  is **1 point**

$|0\rangle$

$|1\rangle$

$\frac{|0\rangle + |1\rangle}{\sqrt{2}}$

$\frac{|0\rangle - |1\rangle}{\sqrt{2}}$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$|1\rangle$

3) Quantum Fourier Transform of the Bell state  $\frac{|01\rangle + |10\rangle}{\sqrt{2}}$  is

1 point

- $\frac{1}{2\sqrt{2}} [2|00\rangle - (1 - i)|01\rangle - (1 + i)|11\rangle]$
- $\frac{1}{2\sqrt{2}} [2|00\rangle - (1 - i)|01\rangle + |10\rangle + (1 + i)|11\rangle]$
- $\frac{1}{2\sqrt{2}} [2|00\rangle - (1 + i)|01\rangle - (1 - i)|11\rangle]$
- $\frac{1}{2\sqrt{2}} [|00\rangle - |01\rangle + |10\rangle - |11\rangle]$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{1}{2\sqrt{2}} [2|00\rangle - (1 - i)|01\rangle - (1 + i)|11\rangle]$$

4) If an operator  $S$  acting a state  $|x\rangle$  gives the state  $|x + 1, \text{mod } N\rangle$ , then  $S$  acting on its QFT,  $|\tilde{x}\rangle$ , gives

1 point

- $S|\tilde{x}\rangle = |\tilde{x} + 1, \text{mod } N\rangle$
- $S|\tilde{x}\rangle = |\tilde{x} - 1, \text{mod } N\rangle$
- $S|\tilde{x}\rangle = \exp(-2\pi i \tilde{x}/N) |\tilde{x}, \text{mod } N\rangle$
- $S|\tilde{x}\rangle = \exp(-2\pi i \tilde{x}/N) |\tilde{x} + 1, \text{mod } N\rangle$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$S|\tilde{x}\rangle = \exp(-2\pi i \tilde{x}/N) |\tilde{x}, \text{mod } N\rangle$$

5) The circuit shown below gives an output given by

1 point

- $|10\rangle$
- $|01\rangle$
- $-|10\rangle$
- $-|11\rangle$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$-|11\rangle$$

6) The order of 4 mod 35 is

1 point

- 2
- 4
- 6
- 8

No, the answer is incorrect.

Score: 0

Accepted Answers:

6

7) The continued fraction representation of 3.1415 is

1 point

- [3,7]  
 [3,7,7]  
 [3,7,14,1]  
 [3,7,14,1,8,2]

No, the answer is incorrect.

Score: 0

Accepted Answers:

[3,7,14,1,8,2]

8) In factorizing  $N = 15$  to illustrate Shor's algorithm, a coprime integer  $m = 7$  is chosen to obtain its period. Choose a pair of  $l$  qubit registers such that  $N^2 \leq 2^l \leq 2N^2$ . Modular exponentiation is done and the second register contains  $f(x)$  corresponding to various values of  $x$ . A measurement of the second register now yields  $f(x) = 7$ . We now apply QFT on the first register. A measurement of the first register gives the state  $|128\rangle$ . The probability of obtaining this outcome is

- 0.25  
 0.125  
 0.0625  
 0.0312

No, the answer is incorrect.

Score: 0

Accepted Answers:

0.25

9) In factorizing  $N = 21$  to illustrate Shor's algorithm, a coprime integer  $m = 11$  is chosen to obtain its period. Choose a pair of qubit registers such that  $N^2 \leq 2^l \leq 2N^2$ . Modular exponentiation is done and the second register contains  $f(x)$  corresponding to various values of  $x$ . A measurement of the second register now yields  $f(x) = 16$ . How many states are there in the first register at this stage?

- 84  
 85  
 86  
 512

No, the answer is incorrect.

Score: 0

Accepted Answers:

85

**In the following questions, ONE or MORE answer(s) is(are) correct. Choose all the appropriate ones. (2X3=6 Marks)**

10) Which of the following is (are) properties satisfied by Discrete Integral Transform (DIT)?

2 points

- The inverse transform always exists.  
 The kernel of the transform is unitary

If  $f$  is a function defined on a set of integers  $S_n = \{0, 1, \dots, N-1\}$ , then the kernel  $K$  can be represented by an  $N \times N$  matrix.

If the kernel  $K$  is unitary, then Parseval's theorem:  $\sum_{x=0}^{N-1} |f(x)|^2 = \sum_{y=0}^{N-1} |f(y)|^2$  holds

No, the answer is incorrect.

Score: 0



**Accepted Answers:**

If  $f$  is a function defined on a set of integers  $S_n = \{0, 1, \dots, N-1\}$ , then the kernel  $K$  can be represented by an  $N \times N$  matrix.

If the kernel  $K$  is unitary, then Parseval's theorem :  $\sum_{x=0}^{N-1} |f(x)|^2 = \sum_{y=0}^{N-1} |f(y)|^2$  holds

11) Suppose in a period finding algorithm with  $n$  qubit registers,  $f(x)$  is a periodic function with a **2 points** period  $P$ . Oracle is used to calculate  $f(x)$  and store it in the output register. A QFT is applied on the first register. Then on measuring the first register, the possible values are

- 0
- $N/2P$
- $2N/2P$
- $3N/2P$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

0

$2N/2P$

12) In using Shor's algorithm to factorize  $N = 187$ , which of the following numbers may be used **2 points** to determine period of  $m^a$ ?

- 3
- 5
- 7
- 11

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

3

5

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