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Courses » Quantum Information and Computing

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## Unit 5 - Week 4

### Course outline

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Week 4

- Simple Quantum Algorithms-Deutsch Algorithm
- Simple Quantum Algorithms: Deutsch-Jozsa and Bernstein-Vazirani Algorithms
- Simple Quantum Algorithms-Simon Problem
- Grover's Search Algorithm-I
- Grover's Search Algorithm-II
- Grover's Search Algorithm-III
- Grover's Search Algorithm-IV
- Quiz : Week 4 - Assignment 4
- Week 4 - Assignment 4 Solutions

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### Week 4 - Assignment 4

The due date for submitting this assignment has passed. **Due on 2017-08-23, 23:59 IST**. As per our records you have not submitted this assignment.

In the following questions, **ONLY ONE** answer is correct. Choose the most appropriate one. (1X12=12 Marks)

1) In the Deutsch algorithm, the input to the oracle is  $|x\rangle = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$  and  $|y\rangle = |1\rangle$ , and **1 point**

the function is such that  $f(0)=0$ ,  $f(1)=1$ . After being subjected to the oracle, the first qubit is passed through a Hadamard gate. The state of the qubits at this stage (before any measurement is made) is

- $|00\rangle$
- $|01\rangle$
- $|00\rangle + |01\rangle - |10\rangle + |11\rangle$
- $|00\rangle + |01\rangle + |10\rangle + |11\rangle$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$|00\rangle + |01\rangle - |10\rangle + |11\rangle$

2) In the Deutsch algorithm, the input to the oracle is  $x = \frac{|0\rangle + |1\rangle}{\sqrt{2}}$  and  $y = |0\rangle$ , and the **1 point**

function is such that  $f(0)=0$ ,  $f(1)=1$ . After being subjected to the oracle, the first qubit is passed through a Hadamard gate. The state of the qubits at this stage (before any measurement is made) is

- $|00\rangle + |01\rangle$
- $|01\rangle + |11\rangle$
- $|10\rangle + |11\rangle$
- $|00\rangle + |11\rangle$

**No, the answer is incorrect.**

**Score: 0**

**Accepted Answers:**

$|00\rangle + |11\rangle$

3) How many queries are required to determine whether a function **1 point**  
 $f : \{0, 1\}^n \rightarrow \{0, 1\}$  is balanced or is constant in a deterministic classical

Week 7

Week-8

algorithm?

 $n$  $\frac{n}{2} - 1$  $2^{n-1} + 1$  $2^{n-1}$ **No, the answer is incorrect.****Score: 0****Accepted Answers:** $2^{n-1} + 1$ 

4) The following circuit shows Deutsch-Jozsa algorithm:

Take  $n=2$ , i.e. a two qubit input in the first register. If  $f(00)=1$  and  $f(01)=f(10)=f(11)=0$ , then the state  $|\psi_3\rangle$  is $|00\rangle - |01\rangle + |10\rangle + |11\rangle$  $|00\rangle - |01\rangle - |10\rangle - |11\rangle$  $|00\rangle + |01\rangle - |10\rangle + |11\rangle$  $|00\rangle + |01\rangle + |10\rangle - |11\rangle$ **No, the answer is incorrect.****Score: 0****Accepted Answers:** $|00\rangle - |01\rangle - |10\rangle - |11\rangle$ 5) In Deutsch-Jozsa algorithm using a two qubit input, the oracle calculates a balanced function **1 point**  $f(00)=f(01)=0$  and  $f(10)=f(11)=1$ . After execution of the algorithm, the first register is measured. The output is: $|10\rangle$  $|01\rangle$  $|00\rangle$  $|11\rangle$ **No, the answer is incorrect.****Score: 0****Accepted Answers:** $|10\rangle$ 6) A 2 to 1 function  $f(x)$  is such that  $f(x) = f(y)$  iff  $x \oplus y = 11$ . If  $f(100) = f(010)$  then it follows that **1 point** $f(001) = f(111)$  $f(001) = f(101)$  $f(001) = f(000)$  $f(001) = f(110)$ **No, the answer is incorrect.****Score: 0****Accepted Answers:** $f(001) = f(111)$ 

1 point

7) Grover's operator  $2|s\rangle\langle s| - I$ , acting on an arbitrary state  $|\psi\rangle$

1 point

- Flips the sign of the component of  $|\psi\rangle$  parallel to  $|s\rangle$
- Flips the sign of the component of  $|\psi\rangle$  perpendicular to  $|s\rangle$
- Flips the sign of the component of  $|\psi\rangle$  parallel to the marked state  $|w\rangle$
- Flips the sign of  $|\psi\rangle$

No, the answer is incorrect.

Score: 0

Accepted Answers:

*Flips the sign of the component of  $|\psi\rangle$  perpendicular to  $|s\rangle$*

8) How many iterations are required by Grover's algorithm to find one marked item out of 100 in an unstructured database?

- 10
- 9
- 8
- 7

No, the answer is incorrect.

Score: 0

Accepted Answers:

8

9) Consider Grover algorithm for  $N=16$  out of which one item is to be searched. The probability of success after two iterations of the algorithm is

- 0.067
- 0.481
- 0.958
- 0.997

No, the answer is incorrect.

Score: 0

Accepted Answers:

0.481

10) For Deutsch-Jozsa algorithm with 2 qubit inputs how many functions are constant functions?

- 1
- 2
- 6
- 8

No, the answer is incorrect.

Score: 0

Accepted Answers:

2

11) Supposing you write a program for classical deterministic algorithm for Deutsch-Jozsa problem to determine whether a given function is constant or is balanced. What is the minimum number of function evaluation after which such a program may terminate?

- 2
- 3
- $n/2$
- $2^{n-1}$

No, the answer is incorrect.

Score: 0

Accepted Answers:



2

12) In Bernstein-Vazirani problem with  $n$  qubit inputs  $x \in \{0, 1\}^n$  and a classical program which calculates  $f(x) = a \cdot x$ , where  $a \cdot x = a_{n-1}x_{n-1} + a_{n-2}x_{n-2} + \dots + a_0x_0 \pmod{2}$ , how many queries do we need to determine the unknown string? 1 point

- $n$
- $\frac{n}{2} + 1$
- $2^{n-1} + 1$
- $2^n$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$n$



In the following questions, ONE or MORE answer(s) is(are) correct. Choose all the appropriate ones. (2X4=8 Marks)

13) If, in the Deutsch algorithm, the input to the oracle is  $|x\rangle = (|0\rangle + |1\rangle)/\sqrt{2}$  and  $|y\rangle = |0\rangle$ , then 2 points

- If the function is constant, we would get  $|0\rangle$  on measuring the first qubit
- If the function is constant, we would get  $|1\rangle$  on measuring the first qubit
- If the function is balanced, on measuring the first qubit, we would get  $|0\rangle$  50% of time and  $|1\rangle$  50% of time
- If on measuring the first qubit, we get  $|1\rangle$ , the function must be balanced

No, the answer is incorrect.

Score: 0

Accepted Answers:

If the function is constant, we would get  $|0\rangle$  on measuring the first qubit

If the function is balanced, on measuring the first qubit, we would get  $|0\rangle$  50% of time and  $|1\rangle$  50% of time

If on measuring the first qubit, we get  $|1\rangle$ , the function must be balanced

14) In Deutsch-Jozsa algorithm taking  $x = 2^{n-1}x_{n-1} + 2^{n-2}x_{n-2} + \dots + 2^0x_0$ , which of the following are examples of a constant function? 2 points

- $\left\lfloor \frac{x}{2^n} \right\rfloor$ , where  $\lfloor \cdot \rfloor$  represents the greatest integer function
- $\sin(\pi x)$
- $\cos(\pi x)$
- $|\cos(\pi x)|$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$\left\lfloor \frac{x}{2^n} \right\rfloor$ , where  $\lfloor \cdot \rfloor$  represents the greatest integer function

$\sin(\pi x)$

$|\cos(\pi x)|$

15) Grover's rotation  $R_G$  operator is 2 points

- Unitary
- Hermitian
- Orthogonal
- Symmetric

No, the answer is incorrect.

Score: 0

Accepted Answers:

*Unitary*

*Orthogonal*

16 For a database of 16 items, if a measurement of the state is made after 'n' iterations of Grover's algorithm, find the probability 'p', that it will fail to identify the marked state corresponding to 'n' 2 points

- n=1, p=375/256
- n=2, p=375/4096
- n=2, p=735/4096
- n=1, p=135/256

No, the answer is incorrect.

Score: 0

Accepted Answers:

*n=2, p=375/4096*

*n=1, p=135/256*



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