

## Unit 7 - Week 4: Structural Elements in One Dimensional FEM

Course outline
How does an NPTEL online course work?
MATLAB
Week 0: Prerequisite
Week 1: Variational Calculus and Minimization Problems
Week 2: One dimensional Finite Element Analysis
Week 3: Structural Elements in One Dimensional FEM
Week 4: Structural Elements in One Dimensional FEM
<ul style="list-style-type: none"> <li>Lec 10: Beam Element: Variational statement, Hermite shape function</li> <li>Lec 11: Beam Element: Elemental equation; Matlab implementation with Example</li> <li>Lec 12: Beam Element: Matlab implementation for the example with Non-uniform distributed load</li> </ul>
<ul style="list-style-type: none"> <li>Quiz : Assignment 4</li> <li>Feedback Form</li> <li>Assignment Solution</li> </ul>
Week 5: Structural Elements in One Dimensional FEM and Generalized One Dimensional Finite Element Code in Computer Programming
Week 6: Brief Background of Tensor Calculus
Week 7: Two dimensional Scalar field problems
Week 8: Two dimensional Scalar field problems
Week 9: Two dimensional Scalar and Vector field problems
Week 10: Two dimensional Vector field and Eigen value problems
Week 11: Eigen value problems and Transient problem in 1D & 2D Scalar Valued Problems
Week 12: FEM formulation for 3D Elastic problem and challenges
Live session: Dr. Atanu Banerjee, Date : 16/12/2020 Time : 3:15:00 PM

### Assignment 4

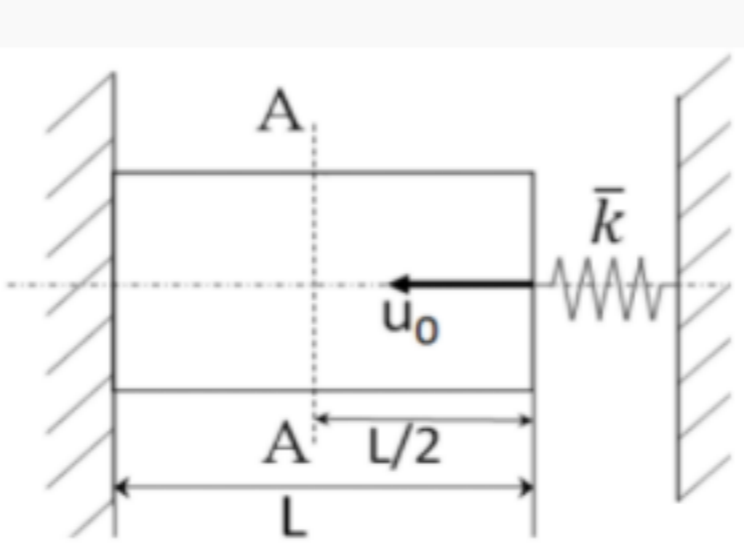
The due date for submitting this assignment has passed. **Due on 2020-10-14, 23:59 IST.**  
As per our records you have not submitted this assignment.

Answer the following question (4 e 1 to 10) with the help of below statement:

A bar has fixed support at one end and it is connected to a linear spring at the other end as shown in Fig. Length  $L$ , Area of the bar are  $0.2\text{ m}$  and  $0.2\text{ m}^2$  respectively. Bar material has Young's modulus of  $70\text{ MPa}$ . The spring has a spring constant of  $k = 10\text{ kN/mm}$ . The connecting point between the bar and the spring is given a displacement of  $u_0 = 5\text{ mm}$  towards left. Consider the left end as node 1, section  $AA$  as node 2 and spring-bar junction point as node 3. Use one quadratic element for the bar for which element stiffness matrix can be expressed as,

$$\frac{dF}{dL} = \begin{bmatrix} 7 & -8 & 1 \\ -8 & 16 & -8 \\ 1 & -8 & 7 \end{bmatrix}$$

where  $A, E, L$  are Area, Young's modulus and Element length respectively for the element.



- 1) Total number of degree of freedom are? **1 point**
- A. 3  
 B. 2  
 C. 4  
 D. 5

No, the answer is incorrect. Score: 0  
Accepted Answers: A: 3

- 2) What is the global stiffness matrix for the problem before imposition of boundary condition? (Let  $\frac{dF}{dL} = c$ , spring constant =  $k$ ) **2 points**

A.  $\begin{bmatrix} 7c + k & -8c & 1c \\ -8c & 16c & -8c \\ 1c & -8c & 7c \end{bmatrix}$

B.  $\begin{bmatrix} 7c & -8c & 1c \\ -8c & 16c + k & -8c \\ 1c & -8c & 7c \end{bmatrix}$

C.  $\begin{bmatrix} 7c & -8c & 1c \\ -8c & 16c & -8c \\ 1c & -8c & 7c + k \end{bmatrix}$

D.  $\begin{bmatrix} 7c & -8c & 1c \\ -8c & 16c & -8c \\ 1c & -8c & 7c + 2k \end{bmatrix}$

No, the answer is incorrect. Score: 0  
Accepted Answers: A: 3

- 3) After imposing the suitable boundary condition and the displacement of the section  $AA$  is, **3 points**

- A. -3.5 mm  
 B. -2.5 mm  
 C. -7 mm  
 D. -4.5 mm

No, the answer is incorrect. Score: 0  
Accepted Answers: B: -2.5 mm

- 4) The reaction force at the left fixed support (Node 1) is, **2 points**

- A. 75.25 kN  
 B. 200 kN  
 C. 449.95 kN  
 D. 349.95 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: D: 349.95 kN

- 5) The reaction force at the spring-bar junction point (Node 3) is, **2 points**

- A. -85.80 kN  
 B. -400 kN  
 C. -699.95 kN  
 D. -399.95 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: D: -399.95 kN

- 6) If the same problem is refined using three quadratic bar elements, what will be the size of global stiffness matrix before imposition of boundary conditions? **1 point**

- A.  $6 \times 6$   
 B.  $7 \times 7$   
 C.  $8 \times 8$   
 D.  $9 \times 9$

No, the answer is incorrect. Score: 0  
Accepted Answers: B:  $7 \times 7$

- 7) If the same problem is refined using three quadratic bar elements, what will be the size of global stiffness after imposition of boundary conditions? **1 point**

- A.  $3 \times 3$   
 B.  $4 \times 4$   
 C.  $5 \times 5$   
 D.  $6 \times 6$

No, the answer is incorrect. Score: 0  
Accepted Answers: C:  $5 \times 5$

- 8) If spring is eliminated from the stated problem setup then, the displacement of section  $AA$  will **2 points**

- A. Increase  
 B. Remains same  
 C. Decrease

No, the answer is incorrect. Score: 0  
Accepted Answers: B: Remains same

- 9) If the spring constant ( $k$ ) is doubled then, what will be reaction at the left end? **3 points**

- A. 75.25 kN  
 B. 200 kN  
 C. 449.95 kN  
 D. 349.95 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: A: 75.25 kN

- 10) If the spring constant ( $k$ ) is doubled then, what will be reaction at the right end? **3 points**

- A. -449.95 kN  
 B. -400 kN  
 C. -699.95 kN  
 D. -399.95 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: A: -449.95 kN

Answer the following question from "a to b" (e 11 to 24) with the help of below statement:



Let us consider a stepped bar as shown in Fig. of two materials. Young's moduli of the material of left and right portions are  $70\text{ MPa}$  and  $200\text{ MPa}$  respectively. Length and area of the parts are  $L_1 = 7.5\text{ m}$ ,  $L_2 = 6\text{ m}$ ,  $A_1 = 0.4\text{ m}^2$ ,  $A_2 = 0.25\text{ m}^2$  respectively. Consider origin at the left end and x-direction along the axial direction of the stepped bar. Use the data given in Table 1 and Table 2. You may use Matlab for solving the problem.

Table 1: Nodal co-ordinates (in m)

Node	x	y
1	0	0
2	$\frac{L_1}{2}$	0
3	$L_1$	0
4	$L_1 + \frac{L_2}{2}$	0
5	$L_1 + L_2$	0

Table 2: Element connectivity

Element	Node 1	Node 2	Node 3
1	1	2	3
2	3	4	5

If the gap between right end of the bar and the right support is  $\Delta = 4\text{ mm}$ , load  $P = 10\text{ kN}$  and solved using two quadratic bar elements then,

(a) If  $K_{ij}$  represent an element stiffness matrix for element  $e$  and component of the respective element stiffness matrix are given by  $K_{ij}(i, j)$  where  $i = 1, 2, \dots$  number of rows and  $j = 1, 2, \dots$  number of columns.

- 11) The  $K_{11}(1, 1)^{\text{th}}$  component of element stiffness matrix (in N/m) is **1 point**

- A.  $1.99 \times 10^7$   
 B.  $8.7 \times 10^6$   
 C.  $-9.95 \times 10^6$   
 D.  $1.24 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: B:  $8.7 \times 10^6$

- 12) The  $K_{13}(3, 2)^{\text{th}}$  component of element stiffness matrix (in N/m) is **1 point**

- A.  $1.99 \times 10^7$   
 B.  $8.7 \times 10^6$   
 C.  $-9.95 \times 10^6$   
 D.  $1.24 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: C:  $-9.95 \times 10^6$

- 13) The  $K_{12}(2, 2)^{\text{th}}$  component of element stiffness matrix (in N/m) is **1 point**

- A.  $1.99 \times 10^7$   
 B.  $8.7 \times 10^6$   
 C.  $-9.95 \times 10^6$   
 D.  $1.24 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: A:  $1.99 \times 10^7$

- 14) The  $K_{12}(2, 3)^{\text{th}}$  component of element stiffness matrix (in N/m) is **1 point**

- A.  $1.94 \times 10^7$   
 B.  $4.44 \times 10^7$   
 C.  $-2.22 \times 10^7$   
 D.  $2.77 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: C:  $-2.22 \times 10^7$

- 15) The  $K_{23}(3, 3)^{\text{th}}$  component of element stiffness matrix (in N/m) is **1 point**

- A.  $1.94 \times 10^7$   
 B.  $4.44 \times 10^7$   
 C.  $-2.22 \times 10^7$   
 D.  $2.77 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: A:  $1.94 \times 10^7$

(b) If  $K$  represent a global stiffness matrix and  $K(i, j)$  are the components of the global stiffness matrix ( $i = \text{row}$  and  $j = \text{column}$ ), then

- 16) The  $K_{11}(1, 1)^{\text{th}}$  component of global stiffness matrix (in N/m) is **2 points**

- A.  $1.99 \times 10^7$   
 B.  $8.7 \times 10^6$   
 C.  $-9.95 \times 10^6$   
 D.  $1.24 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: B:  $8.7 \times 10^6$

- 17) The  $K_{12}(2, 2)^{\text{th}}$  component of global stiffness matrix (in N/m) is **2 points**

- A.  $1.99 \times 10^7$   
 B.  $8.7 \times 10^6$   
 C.  $-9.95 \times 10^6$   
 D.  $1.24 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: A:  $1.99 \times 10^7$

- 18) The  $K_{15}(5, 5)^{\text{th}}$  component of global stiffness matrix (in N/m) is **2 points**

- A.  $4.44 \times 10^7$   
 B.  $-2.22 \times 10^7$   
 C.  $2.77 \times 10^6$   
 D.  $1.94 \times 10^7$

No, the answer is incorrect. Score: 0  
Accepted Answers: D:  $1.94 \times 10^7$

- 19) The  $K_{13}(3, 3)^{\text{th}}$  component of global stiffness matrix (in N/m) is **2 points**

- A.  $4.44 \times 10^7$   
 B.  $2.81 \times 10^7$   
 C.  $-2.22 \times 10^7$   
 D.  $2.77 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: B:  $2.81 \times 10^7$

- 20) The  $K_{13}(3, 4)^{\text{th}}$  component of global stiffness matrix (in N/m) is **2 points**

- A.  $4.44 \times 10^7$   
 B.  $2.81 \times 10^7$   
 C.  $-2.22 \times 10^7$   
 D.  $2.77 \times 10^6$

No, the answer is incorrect. Score: 0  
Accepted Answers: C:  $-2.22 \times 10^7$

- 21) The displacement at material junction is **2 points**

- A. 2.7 mm  
 B. 4.8 mm  
 C. 2.2 mm  
 D. 1.1 mm

No, the answer is incorrect. Score: 0  
Accepted Answers: A: 2.7 mm

- 22) The displacement at right end is **2 points**

- A. 3.7 mm  
 B. 2.7 mm  
 C. 5 mm  
 D. 2.2 mm

No, the answer is incorrect. Score: 0  
Accepted Answers: B: 2.7 mm

- 23) The reaction force at left end is **2 points**

- A. -15 kN  
 B. -1 kN  
 C. -10 kN  
 D. -13 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: C: -10 kN

- 24) What should be load  $P$  such that the gap is just filled without any reaction at the other end? **2 points**

- A. 18.052 kN  
 B. 25 kN  
 C. 14.933 kN  
 D. 8.971 kN

No, the answer is incorrect. Score: 0  
Accepted Answers: C: 14.933 kN