

## Course outline

How does an NPTEL online course work?

Prerequisite Assignment

Week 1

Week 2

Week 3

Week 4

Week 5

Week 6

Week 7

Hamilton-Jacobi Equations - Part 01

Hamilton-Jacobi Equations - Part 02

Hamilton-Jacobi Equations - Part 03

Hamilton-Jacobi Equations - Part 04

Hamilton-Jacobi Equations - Part 05

Hamilton-Jacobi Equations - Part 06

Quiz : Assignment 7

Variational Calculus and its applications in Control Theory and Nanomechanics : Week 7 Feedback Form

Week 8

Week 9

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Week 12

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# Assignment 7

The due date for submitting this assignment has passed.

**Due on 2021-03-10, 23:59 IST.**

As per our records you have not submitted this assignment.

 1) A particle of mass  $m$  is moving vertically, under the action of gravity and resistive force numerically equal to  $c$  times its velocity  $\dot{y}$ . Which of the following is/are the form of it's Hamilton's principle equation ? **1 point**

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt - \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 - mgy \right) dt + \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt - \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt + \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt - \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt + \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\delta \int_{t_1}^{t_2} \left( \frac{1}{2} m \dot{y}^2 + mgy \right) dt - \int_{t_1}^{t_2} c \dot{y} \delta y dt$$

 2) Three masses are connected in series to a fixed support, by linear springs. Let  $x_i$  represent displacement from equilibrium and  $k_i$  be the spring constants. Assuming that only the spring forces are present, what would be the lagrangian function(s) of the system ? **1 point**

$$L = [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 - k_1 x_1^2 - k_2 (x_2 - x_1)^2 - k_3 (x_3 - x_2)^2] + \text{constant}$$

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 + k_1 x_1^2 + k_2 (x_2 - x_1)^2 + k_3 (x_3 - x_2)^2]$$

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 - k_1 (x_1 - x_3)^2 - k_2 (x_2 - x_1)^2 - k_3 (x_3 - x_2)^2] + \text{constant}$$

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 - k_1 x_1^2 - k_2 (x_2 - x_1)^2 - k_3 (x_3 - x_2)^2] + \text{constant}$$

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 + k_1 x_1^2 - k_2 (x_2 - x_1)^2 + k_3 (x_3 - x_2)^2] + \text{constant}$$

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 - k_1 x_1^2 - k_2 (x_2 - x_1)^2 - k_3 (x_3 - x_2)^2] + \text{constant}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$L = \frac{1}{2} [m_1 \dot{x}_1^2 + m_2 \dot{x}_2^2 + m_3 \dot{x}_3^2 - k_1 x_1^2 - k_2 (x_2 - x_1)^2 - k_3 (x_3 - x_2)^2] + \text{constant}$$

 3) A particle moves on the surface  $\phi(x, y, z) = 0$  from the point  $(x_1, y_1, z_1)$  to the point  $(x_2, y_2, z_2)$  in time  $T$ . If it moves in such a way that the integral of it's kinetic energy over that time is minimum, which of the following equations must the coordinates of the particle satisfy ? **1 point**

$$\frac{\ddot{x}}{\phi_x} = \frac{\ddot{y}}{\phi_y} = \frac{\ddot{z}}{\phi_z}$$

$$\frac{\dot{x}}{\phi_x} = \frac{\dot{y}}{\phi_y} = \frac{\dot{z}}{\phi_z}$$

$$\frac{x}{\phi_x} = \frac{y}{\phi_y} = \frac{z}{\phi_z}$$

$$\frac{\ddot{x}}{\phi_x} = \frac{y}{\phi_y} = \frac{z}{\phi_z}$$

$$\frac{x}{\phi_x} = \frac{y}{\phi_y} = \frac{\ddot{z}}{\phi_z}$$

$$\frac{x}{\phi_x} = \frac{\ddot{y}}{\phi_y} = \frac{z}{\phi_z}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{\ddot{x}}{\phi_x} = \frac{\ddot{y}}{\phi_y} = \frac{\ddot{z}}{\phi_z}$$