Programming assignment: Scale an image

It is recommended to initially work on this assignment using Google Colaboratory ("Colab" for short is a free Jupyter notebook environment provided by Google that allows you to run Python in your browser). The introduction videos for Colab will be shared in discussion forum. Being said that, this is a recommended way to do the assignments. You can always directly work on NPTEL website.

Follow these instructions to work on the assignment in google-colab. Click on this Assignment-1 file (https://colab.research.google.com/drive/1TScLDV9PimBwERPjcp8te9Y0Uyqz4-b?usp=sharing). Make a copy of it in your drive. Right click and open the file using Google Colaboratory (You first need to log in to your google account). When you're ready to verify/submit your assignment, paste the missing code snippets.

In this assignment you will perform scaling on an image. The image has already been loaded for you, in the variable named 'cells'. Your task it to scale this image by 0.8 (both horizontally and vertically).

Instructions:

1. You are required to fill in the missing details. The places where you are expected to supply code begin and end with `# <---` and `# -->` respectively.
2. Please read the comments carefully to understand what is being asked of you.
3. Make sure that you always do Target-Source (T-S) mapping.

### Test Case 1

<table>
<thead>
<tr>
<th>Input</th>
<th>Expected Output</th>
<th>Actual Output</th>
<th>Status</th>
</tr>
</thead>
<tbody>
<tr>
<td>cells image</td>
<td>ok</td>
<td>ok</td>
<td>Passed</td>
</tr>
</tbody>
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The due date for submitting this assignment has passed.

1 out of 1 tests passed.
You scored 100.0/100.

Assignment submitted on 2020-10-06, 09:44 IST

Your last recorded submission was:

```python
import base64
import io

# The image has already been loaded for you, in the variable named 'cells'.
cells_scale_str = b'1VBO9w9K5g0AAAAASABJAAwAwAAAAAAbTJU5YXV4cGFydG8gFSGL6gAAIA8B3RJEm5kMjM2MDd2

image_bytes = base64.b64decode(cells_scale_str)
image_file = io.BytesIO(image_bytes)
import numpy as np
import imageio

def image_size(image):
    if image.ndim == 2:
        return image.shape
    else:
        return image.shape[:1]

def bilinear_interpolation(source_image, source_point):
    # Computes the intensity at 'source_point' by bilinearly interpolating intensities in the immediate 2 X 2 neighborhood of the 'source_point'.
    source_image = np.array(source_image)  # The source image
    source_point = (float, float): The source point
    ...# floor(i) returns the largest integer less than or equal to i
    # floor(j) returns the largest integer less than or equal to j
    ...# i_s and j_s are the indices of the source point
    # (i, j)
    ...# tl = i_s,j_s
    # tr = 1, j_s+1
    # bl = i_s+1, j
    # br = (i_s+1, j_s+1)
```

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def transform(source_image, transformation, target_size=None):
    # Transforms 'source_image' as dictated by 'transformation'.
    
    Note that this function does T-S mapping. So, 'transformation' is actually from Target to Source.

    Args:
    
    source_image (np.array): The source image
    transformation (np.array): 3 x 3 transformation matrix
    target_size (uint, uint): Size of the target_image

    Returns:
    
    target_image (np.array): Scaled image
    
    # When no 'target_size' is supplied, 'target_image' will be the same size as 'source_image'
    target_rows, target_cols = target_size if target_size else (source_rows, source_cols)
    target_image = np.zeros((target_rows, target_cols), dtype=np.uint)

    # We iterate over each pixel in 'target_image' and assign the appropriate intensity
    for i_t in range(target_rows):
        for j_t in range(target_cols):
            # Map each target point (i_t, j_t) through 'transformation'
            i_s, j_s = np.array((i_t, j_t, 1)) @ transformation.T
            i_s = np.floor(i_s / v, j_s / v
            
            # We ignore all target points whose source points lie outside the
            # source image. All these intensities remain 0.
            if i_s <= 0 or i_s <= source_rows - 1 and 0 <= j_s <= source_cols - 1:
                # Assign the intensity value of target image at (i_t, j_t) using the
                # bilinear interpolation function above.
                
                target_image[i_t, j_t] = bilinear_interpolation(source_image, (i_s, j_s))

    return target_image

def scale(source_image, factor):
    # Scales the 'source_image' by 'factor' in both dimensions.

    Args:
    
    source_image (np.array): The source image
    factor (float): Scaling factor.

    Returns:
    
    scaled_image (np.array): Scaled image
    
    # Create a variable called 'scaling' which holds a 3 x 3
    # numpy array that corresponds to scaling by factor
    # Note that this matrix should be 1-S, 
    # so it would be the inverse of what you might think of for
    # an S-T scaling matrix.
    
    # scaling = np.array([(1 / factor, 0, 0),
    # (0, 1 / factor, 0),
    # (0, 0, 1)])

    return transform(source_image, scaling)
# Write down the co-ordinates of the remaining three corners
# (Top-right, bottom-left, bottom-right) below.
# Use the variable names 'tr', 'bl', 'br' respectively.
# <---
# tr = [i + 1, j + 1]
# bl = [i + 1, j - 1]
# br = [i - 1, j + 1]
# --->

# Next, we compute the distance of 'source point' from top-left corner along
# vertical and horizontal directions separately.

del_i, del_j = i_s - i, j_s - j
# Create a variable called 'pixel_intensity' and assign the
# pixel value obtained by bilinearly interpolating pixel values
# at tr, fr, bl, br.
# Use 'del_i', 'del_j' computed in the previous step to obtain
# the weights for interpolation.

# --->
pixel_intensity = 
# (1 - del_i) * (1 - del_j) * source_image[tl] + 
# (1 - del_i) * del_j * source_image[tr] + 
# del_i * (1 - del_j) * source_image[bl] + 
# del_i * del_j * source_image[br]
# --->

return np.float64(pixel_intensity)

def transform(source_image, transformation, target_size=None):
    # Transforms 'source_image' as dictated by 'transformation'.
    # Note that this function does T-S mapping. So, 'transformation' is actually from Target to Source.

    Args:
        source_image (np.array): The source image
        transformation (np.array): 3 x 3 transformation matrix
        target_size (uint, uint): Size of the target_image

    Returns:
        np.array: Transformed image

    # When no 'target_size' is supplied, 'target_image' will be the same size as 'source_image'
    # target_rows, target_cols = image_shape(source_image)

    # We iterate over each pixel in 'target_image' and assign the appropriate intensity
    for i_t in range(target_rows):
        for j_t in range(target_cols):
            # Map each target point ('i_t', 'j_t') through 'transformation'
            # to obtain its corresponding source point ('i_s', 'j_s')
            # --->
            1_s, 1_j = np.array([i_t, j_t]) @ transformation.T
            1_s, 1_j = 1_s / v, 1_j / v
            # --->

            # We ignore all target points whose source points lie outside the
            # source image. All these intensities remain 0.
            if 0 <= 1_s < source_rows - 1 and 0 <= 1_j < source_cols - 1:
                # Assign the intensity value of target image at(i_t, j_t) using the
                # bilinear interpolation function above.
                # --->
                target_image[i_t, j_t] = bilinear_interpolation_c(source_image, (1_s, 1_j))
                # --->

    return target_image

def scale(source_image, factor):
    # Scales the 'source_image' by 'factor' in both dimensions.

    Args:
        source_image (np.array): The source image
        factor (float): Scaling factor.

    Returns:
        np.array: Scaled image

    # Create a variable called 'scaling' which holds a 3 x 3
    # numpy array that corresponds to scaling by factor
    # Note that this matrix should be 1's,
    # so it would be the inverse of what you might think of for
    # an S-T scaling matrix.
    # --->
    scaling = np.array([[1 / factor, 0, 0],
                        [0, 1 / factor, 0],
                        [0, 0, 1]])
    # --->

    return transform(source_image, scaling)

cells_scaled_c = scale_c(cells, 0.8)

if np.mean((cells_scaled_c - cells_scaled)**2) < 5:
    print('ok', end='
')
else:
    print('not ok', end='
')