

X



reviewer3@nptel.iitm.ac.in ▼

Courses » Applied Optimization for Wireless, Machine Learning, Big-Data

Announcements Course Ask a Question Progress Mentor FAQ

# Unit 13 - Week 11 : Application: Radar for target detection, Array Processing, MUSIC, MIMO-Radar Schemes for Enhanced Target Detection

## Course outline

How to access the portal

Week 1 : Introduction to properties of Vectors, Norms, Positive Semi-Definite matrices and Gaussian Random Vectors

DOWNLOAD VIDEOS

Week 2: Introduction to Convex Optimization – Convex sets, Hyperplanes/ Half-spaces etc. Application: Power constraints in Wireless Systems

Week 3 : Convex/ Concave Functions, Examples, Conditions for

## Assignment-11

The due date for submitting this assignment has passed. As per our records you have not submitted this assignment. **Due on 2018-10-17, 23:59 IST.**

1) Consider the matrix **A** given below 1 point

$$\mathbf{A} = \begin{bmatrix} 1 & 1 & 1 \\ -1 & 2 & 0 \\ 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 5 \end{bmatrix} \begin{bmatrix} 1 & -1 & 1 \\ 1 & 2 & 1 \\ 1 & 0 & -1 \end{bmatrix}$$

The solution to the problem  $\max \bar{\mathbf{v}}^T \mathbf{A} \bar{\mathbf{v}}$ , s.t.  $\|\bar{\mathbf{v}}\| \leq 1$  is

- 18
- 10
- 15
- 5

No, the answer is incorrect. Score: 0

Accepted Answers: 18

2) Consider the MIMO channel with channel matrix 1 point

$$\mathbf{A} = \begin{bmatrix} 1 & 1 & 1 \\ -1 & 2 & 0 \\ 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 5 \end{bmatrix} \begin{bmatrix} 1 & -1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & -1 \end{bmatrix}$$

© 2014 NPTEL - Privacy & Terms - Honor Code - FAQs -



A project of



In association with



Funded by

Cognitive Radio Systems

Week 4 : Convex Optimization problems, Linear Program, Application: Power allocation in Multi-cell cooperative OFDM

Week 5: Jensen's Inequality, Operations that preserve Convexity, Examples, Beamforming in Multi-antenna Wireless Communication

Week-6: Maximal Ratio Combiner (MRC), Multi-antenna Beamforming with Interfering User, Zero-Forcing (ZF) beamforming, Robust beamformer Design

Week-7: Optimization for signal estimation, LS, WLS, Regularization. Application: Wireless channel estimation, Image Reconstruction-Deblurring, Representation of Convex Optimization problem

Week 8 : Application: Convex optimization for Machine Learning, Principal Component Analysis (PCA), Support Vector Machines

Week 9- Application: Compressive Sensing, Sparse

ce De

$$\begin{bmatrix} \frac{1}{\sqrt{6}} \\ 2 \\ \frac{1}{\sqrt{6}} \end{bmatrix}, \begin{bmatrix} \frac{1}{\sqrt{2}} \\ 1 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ -\frac{1}{\sqrt{2}} \end{bmatrix}, \begin{bmatrix} -\frac{1}{\sqrt{6}} \\ \frac{1}{\sqrt{6}} \\ \sqrt{\frac{2}{3}} \end{bmatrix}$$

$$\begin{bmatrix} \frac{1}{\sqrt{3}} \\ -\frac{1}{\sqrt{3}} \\ 1 \\ \frac{1}{\sqrt{3}} \end{bmatrix}, \begin{bmatrix} \frac{1}{\sqrt{3}} \\ -\frac{1}{\sqrt{3}} \\ 1 \\ \frac{1}{\sqrt{3}} \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$$

No, the answer is incorrect. Score: 0

Accepted Answers:

$$\begin{bmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ -\frac{1}{\sqrt{2}} \end{bmatrix}, \begin{bmatrix} -\frac{1}{\sqrt{6}} \\ \frac{1}{\sqrt{6}} \\ \sqrt{\frac{2}{3}} \end{bmatrix}$$

3) Consider a cooperative communication system with average gains of the source-destination, source-relay and relay-destination gains given by  $\delta_{sd}^2$ ,  $\delta_{sr}^2$ , and  $\delta_{rd}^2$ , respectively. Let  $P_1, P_2$  denote source and relay powers, respectively, with noise power equal to  $\sigma^2$ . Let  $\phi$  denote the event of error at relay. Then,  $\Pr(\phi)\Pr(e|\phi)$  is

1 point

$\frac{3\sigma^4}{4P_1 P_2 \delta_{sd}^2 \delta_{rd}^2}$

$\frac{\sigma^4}{4P_1 P_2 \delta_{sr}^2 \delta_{rd}^2}$

$\frac{\sigma^4}{4P_1^2 \delta_{sd}^2 \delta_{sr}^2}$

Signal Processing, OMP (Orthogonal Matching Pursuit), LASSO (Least Absolute Shrinkage and Selection Operator) for signal estimation, SVM

Week 10- Application: Compressive Sensing, Sparse Signal Processing, OMP (Orthogonal Matching Pursuit), LASSO (Least Absolute Shrinkage and Selection Operator) for signal estimation

Week 11 : Application: Radar for target detection, Array Processing, MUSIC, MIMO-Radar Schemes for Enhanced Target Detection

- Lec 68- Optimal MIMO Power allocation(Waterfilling)-I
- Lec 69- Example problem on Optimal MIMO Power allocation(Waterfilling)
- Lec 70- Linear objective with box constraints, Linear Programming
- Lec 71- Example Problems II
- Lec 72- Examples on Quadratic Optimization
- Lec 73- Examples on Duality: Dual Norm, Dual of Linear

$$\frac{4\sigma^4}{3P_2^2 \delta_{sd}^2 \delta_{rd}^2}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{\sigma^4}{4P_1^2 \delta_{sd}^2 \delta_{sr}^2}$$

4) Consider a cooperative communication system with average gains of the source-destination, source-relay and relay-destination gains given 1 point

by  $\delta_{sd}^2$ ,  $\delta_{sr}^2$ , and  $\delta_{rd}^2$ , respectively. Let  $P_1, P_2$  denote source and relay powers, respectively, with noise power equal to  $\sigma^2$ . Let  $\phi$  denote the event of error at relay.

Then,  $\Pr(e|\bar{\phi})$  is

$$\frac{3\sigma^4}{4P_1 P_2 \delta_{sd}^2 \delta_{rd}^2}$$

$$\frac{\sigma^4}{4P_1 P_2 \delta_{sr}^2 \delta_{rd}^2}$$

$$\frac{\sigma^4}{4P_1^2 \delta_{sd}^2 \delta_{sr}^2}$$

$$\frac{4\sigma^4}{3P_2^2 \delta_{sd}^2 \delta_{rd}^2}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{3\sigma^4}{4P_1 P_2 \delta_{sd}^2 \delta_{rd}^2}$$

5) Consider a cooperative communication system with average gains of the source-destination, source-relay and relay-destination gains given 1 point

by  $\delta_{sd}^2$ ,  $\delta_{sr}^2$  and  $\delta_{rd}^2$ , respectively. Let  $P_1, P_2$  denote source and relay powers, respectively, with noise power equal to  $\sigma^2$ . The optimal power allocation factor alpha where  $P_1 = \alpha P$ ,  $P_2 = (1 - \alpha)P$  is given as

$$\frac{\left(\frac{4}{3} \delta_{sr}^2 - \delta_{rd}^2\right) + \delta_{sr} \sqrt{\frac{8}{3} \delta_{sr}^2 + \delta_{rd}^2}}{4(\delta_{sr}^2 - \delta_{rd}^2)}$$

$$\frac{\left(\delta_{sd}^2 + \frac{1}{3} \delta_{sr}^2\right) + \delta_{rd} \sqrt{\delta_{rd}^2 + \frac{2}{3} \delta_{sd}^2}}{2\left(\frac{1}{3} \delta_{sd}^2 - \delta_{rd}^2\right)}$$

Program(LP)

- Quiz : Assignment-11
- Assignment-11 Solution

**Week 12:**  
**Application:**  
 Convex optimization for Big Data Analytics, Recommender systems, User Rating Prediction and Optimization for Finance

Transcripts

$$\frac{\left(\delta_{rd}^2 + \frac{1}{2} \delta_{sr}^2\right) + \delta_{sd} \sqrt{\delta_{sd}^2 + \frac{1}{4} \delta_{sr}^2}}{3\left(\delta_{rd}^2 - \frac{1}{2} \delta_{sd}^2\right)}$$

$$\frac{\left(\delta_{sr}^2 - \frac{4}{3} \delta_{rd}^2\right) + \delta_{sr} \sqrt{\delta_{sr}^2 + \frac{8}{3} \delta_{rd}^2}}{4\left(\delta_{sr}^2 - \frac{1}{3} \delta_{rd}^2\right)}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\frac{\left(\delta_{sr}^2 - \frac{4}{3} \delta_{rd}^2\right) + \delta_{sr} \sqrt{\delta_{sr}^2 + \frac{8}{3} \delta_{rd}^2}}{4\left(\delta_{sr}^2 - \frac{1}{3} \delta_{rd}^2\right)}$$

6) The compressive sensing problem can be formulated as

1 point

- $\min \|\bar{\mathbf{x}}\|_2$  subject to  $\bar{\mathbf{y}} = \Phi\bar{\mathbf{x}}$
- $\min \|\bar{\mathbf{x}}\|_0$  subject to  $\bar{\mathbf{y}} = \Phi\bar{\mathbf{x}}$
- $\min \|\bar{\mathbf{y}} - \Phi\bar{\mathbf{x}}\|^2$
- $\min \|\bar{\mathbf{x}}\|_2$  subject to  $\bar{\mathbf{y}} \preceq \Phi\bar{\mathbf{x}}$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\min \|\bar{\mathbf{x}}\|_0 \text{ subject to } \bar{\mathbf{y}} = \Phi\bar{\mathbf{x}}$$

7) Consider the sparse signal estimation problem below

1 point

$$\begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{bmatrix} = \begin{bmatrix} 10 \\ 2 \\ 0 \\ 8 \end{bmatrix}$$

The non-zero signal coefficients in the sparse solution are

- $x_2, x_5$
- $x_1, x_4$
- $x_3, x_6$
- $x_3, x_5$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$x_3, x_6$$

8) Consider the sparse signal estimation problem below

1 point

$$\begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{bmatrix} = \begin{bmatrix} 10 \\ 2 \\ 0 \\ 8 \end{bmatrix}$$

The values of the non-zero signal coefficients in the sparse solution are



2, 8



4, 6



3, 5



5, 2

No, the answer is incorrect.

Score: 0

Accepted Answers:

2, 8

9) Consider two sets of points  $\bar{\mathbf{x}}_i, \bar{\mathbf{y}}_i, 1 \leq i \leq N$ . The two hyperplanes which separate them with maximum distance of separation between them are given as the solution to the optimization problem

1 point



$$\begin{aligned} & \max 1 \\ & \text{s.t. } \bar{\mathbf{a}}^T \bar{\mathbf{x}}_i \geq b, 1 \leq i \leq N \\ & \bar{\mathbf{a}}^T \bar{\mathbf{y}}_i \leq b, 1 \leq i \leq N \end{aligned}$$



$$\begin{aligned} & \min \|\bar{\mathbf{a}}\| \\ & \text{s.t. } \bar{\mathbf{a}}^T \bar{\mathbf{x}}_i \geq b, 1 \leq i \leq N \\ & \bar{\mathbf{a}}^T \bar{\mathbf{y}}_i \leq b, 1 \leq i \leq N \end{aligned}$$



$$\begin{aligned} & \max \|\bar{\mathbf{a}}\| \\ & \text{s.t. } \bar{\mathbf{a}}^T \bar{\mathbf{x}}_i \geq b, 1 \leq i \leq N \\ & \bar{\mathbf{a}}^T \bar{\mathbf{y}}_i \leq b, 1 \leq i \leq N \end{aligned}$$



$$\begin{aligned} & \min \|\bar{\mathbf{a}}\| \\ & \text{s.t. } \bar{\mathbf{a}}^T \bar{\mathbf{x}}_i + b \geq 1, 1 \leq i \leq N \\ & \bar{\mathbf{a}}^T \bar{\mathbf{y}}_i + b \leq -1, 1 \leq i \leq N \end{aligned}$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$\begin{aligned} & \min \|\bar{\mathbf{a}}\| \\ & \text{s.t. } \bar{\mathbf{a}}^T \bar{\mathbf{x}}_i + b \geq 1, 1 \leq i \leq N \\ & \bar{\mathbf{a}}^T \bar{\mathbf{y}}_i + b \leq -1, 1 \leq i \leq N \end{aligned}$$

10) Consider the standard form of the optimization problem given below

1 point

$$\min g_0(\bar{\mathbf{x}})$$

$$\text{s.t. } g_i(\bar{\mathbf{x}}) \leq 0, i = 1, 2, \dots, l$$

$$\tilde{g}_j(\bar{\mathbf{x}}) = 0, j = 1, 2, \dots, m$$

The Lagrangian for the above problem is



$$L(\bar{\mathbf{x}}) = g_0(\bar{\mathbf{x}}) + \sum_{i=1}^l g_i(\bar{\mathbf{x}}) + \sum_{j=1}^m \tilde{g}_j(\bar{\mathbf{x}})$$



$$L(\bar{\mathbf{x}}, \bar{\boldsymbol{\lambda}}) = g_0(\bar{\mathbf{x}}) + \sum_{i=1}^l \lambda_i g_i(\bar{\mathbf{x}}) + \sum_{j=1}^m \tilde{g}_j(\bar{\mathbf{x}})$$



$$L(\bar{\mathbf{x}}, \bar{\boldsymbol{\nu}}) = g_0(\bar{\mathbf{x}}) + \sum_{i=1}^l g_i(\bar{\mathbf{x}}) + \sum_{j=1}^m \nu_j \tilde{g}_j(\bar{\mathbf{x}})$$



$$L(\bar{\mathbf{x}}, \bar{\boldsymbol{\lambda}}, \bar{\boldsymbol{\nu}}) = g_0(\bar{\mathbf{x}}) + \sum_{i=1}^l \lambda_i g_i(\bar{\mathbf{x}}) + \sum_{j=1}^m \nu_j \tilde{g}_j(\bar{\mathbf{x}})$$

No, the answer is incorrect.

Score: 0

Accepted Answers:

$$L(\bar{\mathbf{x}}, \bar{\boldsymbol{\lambda}}, \bar{\boldsymbol{\nu}}) = g_0(\bar{\mathbf{x}}) + \sum_{i=1}^l \lambda_i g_i(\bar{\mathbf{x}}) + \sum_{j=1}^m \nu_j \tilde{g}_j(\bar{\mathbf{x}})$$

Previous Page

End