

## Course outline

How does an NPTEL online course work?

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week 9

● Lecture 28: Permanent and Determinant Functions

● Lecture 29: Permanent is hard for #P

● Lecture 30: Interactive Proofs

○ Quiz : Assignment 9

● Feedback for Week 9

● Assignment 9 Solution

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# Assignment 9

The due date for submitting this assignment has passed.

**Due on 2021-03-24, 23:59 IST.**

As per our records you have not submitted this assignment.

1) Let  $A$  be an  $n \times n$  matrix with  $\{0,1\}$  entries. We define a bipartite graph  $G_A$  with  $2n$  vertices  $\{u_1, u_2, \dots, u_n\}$  and  $\{v_1, v_2, \dots, v_n\}$  such that there is an edge between  $u_i$  and  $v_j$  if and only if  $A[i,j]$  is 1. Which of the following two statements is/are true? **2 points**

- If  $G_A$  has a perfect matching then permanent of  $A$  is nonzero.
- If  $G_A$  has a perfect matching then determinant of  $A$  is nonzero.

- Only 1  
 Only 2  
 Both 1 and 2  
 Neither 1 nor 2

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Only 1

2) Let  $kIP$  be a deterministic interactive protocol that has  $k$  rounds of interactions, for some  $k > 1$ . Which of the following is known to be true? **2 points**

- $kIP$  is a strict subset of  $dIP$   
  $kIP$  is equals to  $dIP$   
  $kIP$  is equals to  $P$   
  $kIP$  is not equals to  $dIP$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $kIP$  is equals to  $dIP$

3) Let  $A$  be an  $n \times n$  matrix. Which of the following two statements is/are true? **2 points**

- If determinant of  $A$  is nonzero then permanent of  $A$  is also nonzero.
- If permanent of  $A$  is nonzero then determinant of  $A$  is also nonzero.

- Only 1  
 Only 2  
 Both 1 and 2  
 Neither 1 nor 2

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Neither 1 nor 2

4) Consider the following two languages,  
 $BPM = \{ \langle G \rangle \mid G \text{ is an undirected, bipartite graph and } G \text{ has a perfect matching} \}$ ,  
 $CYCOV = \{ \langle G \rangle \mid G \text{ is a directed graph and } G \text{ has a cycle cover} \}$ .  
 Which of the following is known to be true? **3 points**

- $BPM$  is logspace reducible to  $CYCOV$  but  $CYCOV$  is not logspace reducible to  $BPM$ .  
  $CYCOV$  is logspace reducible to  $BPM$  but  $BPM$  is not logspace reducible to  $CYCOV$ .  
 Both are logspace reducible to each other.  
 Neither of them logsapce reducible to other.

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
Both are logspace reducible to each other.

5) Consider the following language,  
 $PerParity = \{ A \mid A \text{ is a matrix and the permanent of } A \text{ is divisible by } 2 \}$ .  
 Which is the smallest known complexity class among following for  $PerParity$ ? **3 points**

- #P  
  $\#P$   
 P  
 NC

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
NC

6) We define a class  $EIP$  which is same as  $IP$  except that the prover in this class is only as powerful as class  $EXP$ . Which of the following is known to be true? **2 points**

- $IP$  is a strict subset of  $EIP$   
  $IP$  is equals to  $EIP$   
  $EIP$  is a strict subset of  $IP$   
  $EIP$  is not equals to  $IP$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $IP$  is equals to  $EIP$

7) Which of the following is known to be true? **3 points**

- $IP[1]$  is a strict subset of  $BPP$   
  $IP[1]$  is equals to  $BPP$   
  $IP[k] = NP$ , where  $k > 0$  is a constant  
  $IP[k] = BPP$ , where  $k > 1$  is a constant

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $IP[1]$  is equals to  $BPP$

8) Assume that there is a polynomial time algorithm to compute permanent of a matrix. What can we conclude from this? **1 point**

- $P = NP$   
  $NP = coNP$   
  $IP = P$   
  $IP = NP$

No, the answer is incorrect.  
Score: 0

Accepted Answers:  
 $P = NP$   
 $NP = coNP$