

Unit 13 - Week 12: Complex Variables, Functions, Differentiation and Integration

Assignment 12

1) The form of the complex number $4-3i$ in polar variables is

1 point

- $5e^{i\pi/3}$
- $5e^{i2\pi/3}$
- $\sqrt{7}\exp(\arctan(-4/3))$
- None of the above

Accepted Answers:

None of the above

2) The principal value of $\log(e^2 + i)$ is

1 point

- 2
- 2
- $2 + i\pi/2$
- None of the above

Accepted Answers:

None of the above

3) The principal value of the complex number $\log(-3)$ is

1 point

- $\log(3) + 3i\pi/2$
- ∞
- $\log 3 + i\pi$
- None of the above

Accepted Answers: $\log 3 + i\pi$

4) Consider the complex function given by

1 point

$$f(z) = \frac{e^z}{z(z^2+z+1)}$$

The pole(s) of this function is(are) located at

- 0
- 0, $0.5 + i\sqrt{0.75}$, $0.5 - i\sqrt{0.75}$
- 0.5, -0.5
- $1 + i\sqrt{3}$, $1 - i\sqrt{3}$, 0

Accepted Answers: $0, 0.5 + i\sqrt{0.75}, 0.5 - i\sqrt{0.75}$

5) Consider a complex function given by

1 point

$$f(z) = \frac{1+z^2}{z(z-i)}$$

The point $z = i$ is a

- simple pole
- pole of order 2
- regular point
- None of the above

Accepted Answers:*regular point*

6) The contour integral

1 point

$$\int_C \frac{e^z}{2z} dz$$

where C is a clockwise unit circle centered at $z=2$ is equal to

- 0
- $i\pi e^2/2$
- $-i\pi e^2/2$
- None of the above

Accepted Answers:

0

7) The contour integral

1 point

$$\int_C \frac{z^2}{(z+i/2)} dz$$

where C is a clockwise unit circle centered at $z=0$ is equal to

- 0
- 1/16
- $i\pi/2$
- None of the above

Accepted Answers:

$$i\pi/2$$

8) The contour integral of the function

1 point

$$\int_C \frac{z+2}{z^2(z+0.5)} dz$$

where C is the counterclockwise unit circle centered at $z=0$ is equal to

- 0

 $12\pi i$

 $-6\pi i$
 None of the above

Accepted Answers:

$$0$$

9) The integral

1 point

$$\int_{-\infty}^{\infty} \frac{e^{ix}}{x^2+4} dx$$

is equal to

- 0

 $\frac{\pi}{2e^2}$

 $i\pi/2$
 None of the above

Accepted Answers:

$$\frac{\pi}{2e^2}$$

